## Distributed Systems Part II

## Exercise Sheet 11

## Quiz

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## 1 Clock Synchronization

a) Prove or disprove the following statement: If the average local skew is smaller than $x$, then so is the average global skew.
b) Prove or disprove the following statement: If the average global skew is smaller than $x$, then so is the average local skew.

## Basic

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## 2 Time Difference of Arrival

Assume you are located on a line $y=-x+8 k m$ in the two dimensional plane. You also receive the GPS signals from two satellites $A$ and $B$. Both signals were transmitted exactly at the same time $t$ by both satellites. You receive the signal from satellite $A 3.3 \mu s$ before the signal of satellite $B$. You also know that satellite $A$ is located at $p^{A}=(6 \mathrm{~km}, 6 \mathrm{~km})$ and satellite $B$ is located at $p^{B}=(2 k m, 1 k m)$, i.e. in the plane.
a) Formulate the least squares problem to find your location.
b) Are you more likely to be at position $(2 \mathrm{~km}, 6 \mathrm{~km})$ or ( $4 \mathrm{~km}, 4 \mathrm{~km}$ ) ?
c) What is the time when receiving the signal from satellite $B$ ?

## Advanced

## 3 Clock Synchronization: Spanning Tree

Common clock synchronization algorithms (e.g. TPSN, FTSP) rely on a spanning tree to perform clock synchronization. In the TPSN protocol sender-receiver synchronization is performed along the edges of the tree while FTSP is flooding synchronization messages along a tree rooted at the reference node. Finding a good spanning tree for clock synchronization is not trivial. Nodes which are neighbors in the network graph should also be close-by in the resulting tree. Show that in a grid of $n=m \times m$ nodes there exists at least a pair of nodes with a stretch of at least $m$. The stretch is defined as the hop distance in the tree divided by the distance in the grid.

