

Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich



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## Distributed Systems Part II

Exercise Sheet 11

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| Quiz |  |  |
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## 1 Clock Synchronization

- a) Prove or disprove the following statement: If the average local skew is smaller than x, then so is the average global skew.
- b) Prove or disprove the following statement: If the average global skew is smaller than x, then so is the average local skew.

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| Basic |  |  |  |

## 2 Time Difference of Arrival

Assume you are located on a line y = -x + 8km in the two dimensional plane. You also receive the GPS signals from two satellites A and B. Both signals were transmitted exactly at the same time t by both satellites. You receive the signal from satellite A 3.3 $\mu s$  before the signal of satellite B. You also know that satellite A is located at  $p^A = (6km, 6km)$  and satellite B is located at  $p^B = (2km, 1km)$ , i.e. in the plane.

- a) Formulate the least squares problem to find your location.
- b) Are you more likely to be at position (2km,6km) or (4km,4km)?
- c) What is the time when receiving the signal from satellite B?

## 3 Clock Synchronization: Spanning Tree

Common clock synchronization algorithms (e.g. TPSN, FTSP) rely on a spanning tree to perform clock synchronization. In the TPSN protocol sender-receiver synchronization is performed along the edges of the tree while FTSP is flooding synchronization messages along a tree rooted at the reference node. Finding a good spanning tree for clock synchronization is not trivial. Nodes which are neighbors in the network graph should also be close-by in the resulting tree. Show that in a grid of  $n = m \times m$  nodes there exists at least a pair of nodes with a stretch of at least m. The stretch is defined as the hop distance in the tree divided by the distance in the grid.