

Partial Observability in DRL

Part 1: POMDPs, (A)DRQN & DVRL

Most of the World is only Partially Observable

Occlusions



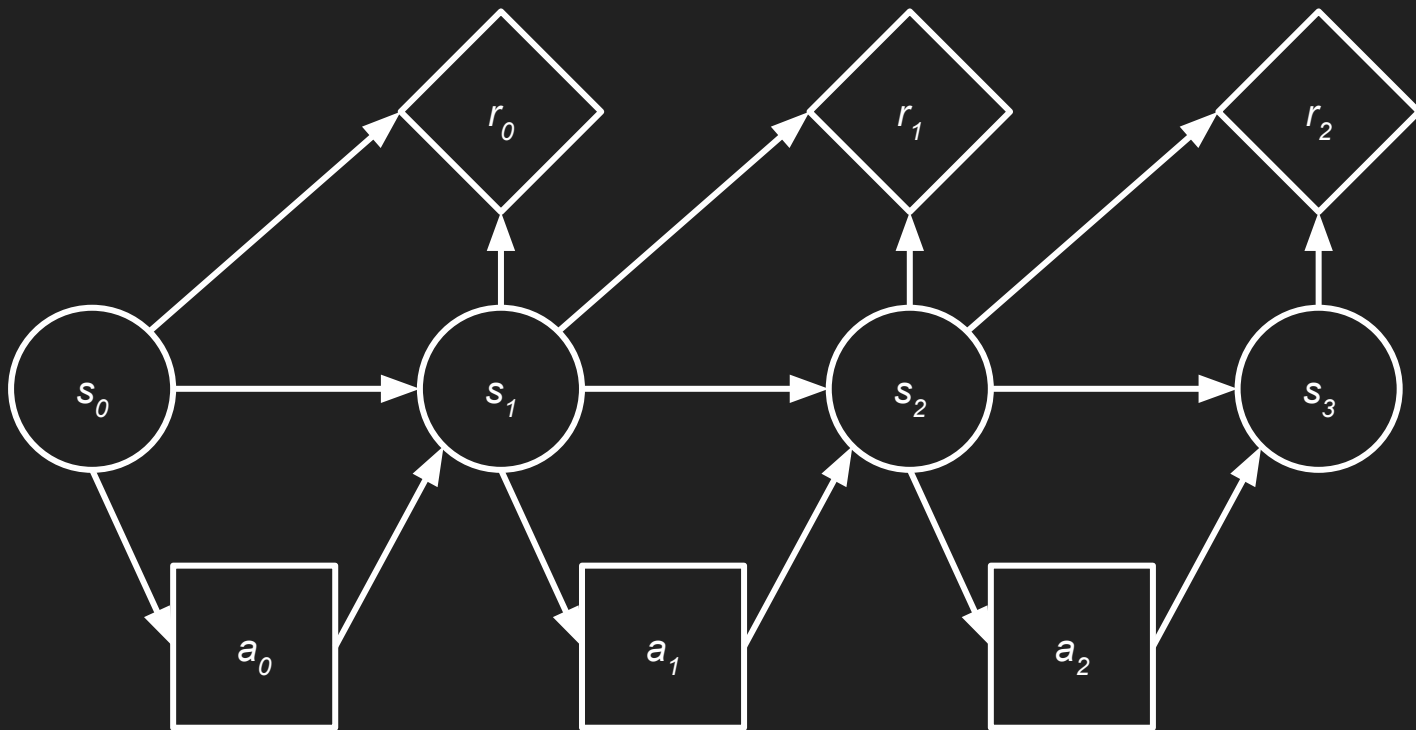
Latent Causes



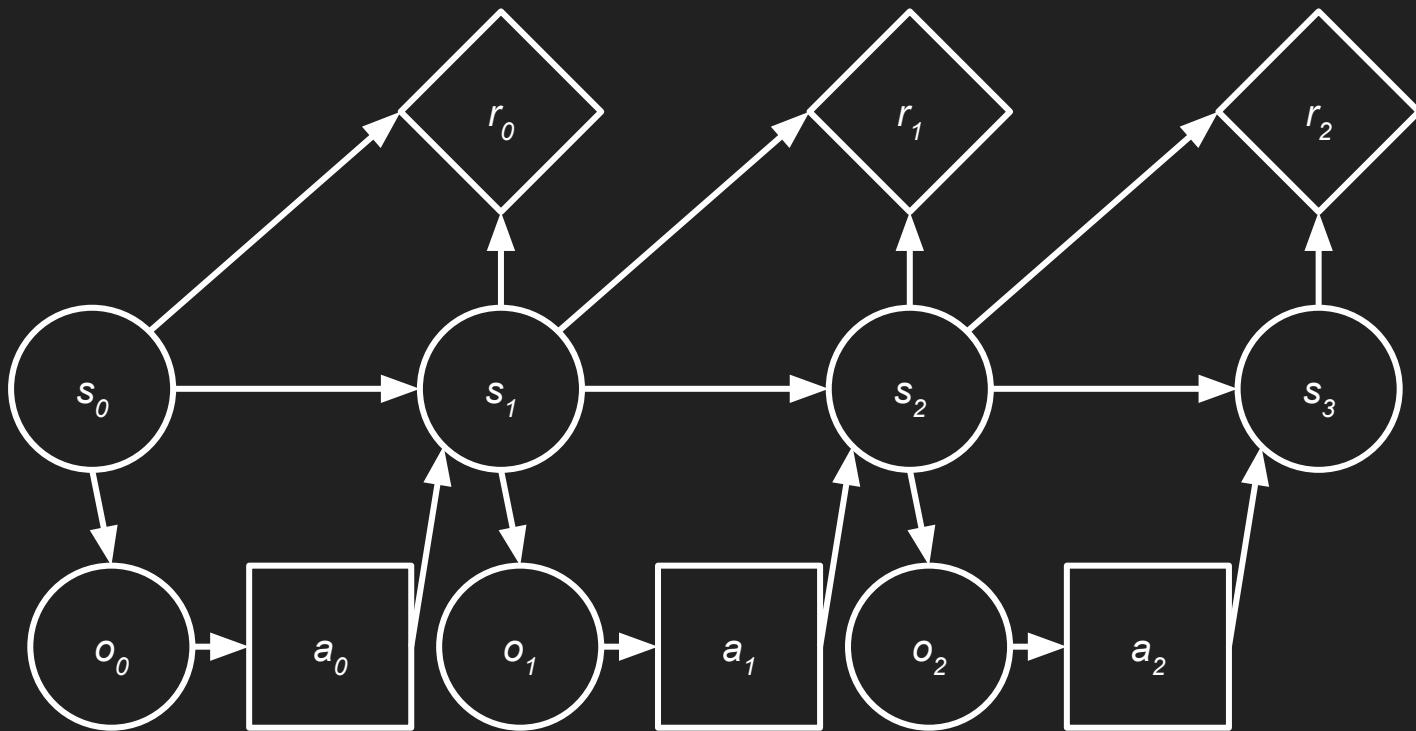
Intentions



From MDP to ...



From MDP to POMDP



Slightly more formal

7-Tuple: $(S, A, T, R, \Omega, O, \gamma)$

$s \in S$ is a state from the set of States

$a \in A$ is an action set of Actions

$T(s_{t+1} | s_t, a_t)$ is the transition probabilities

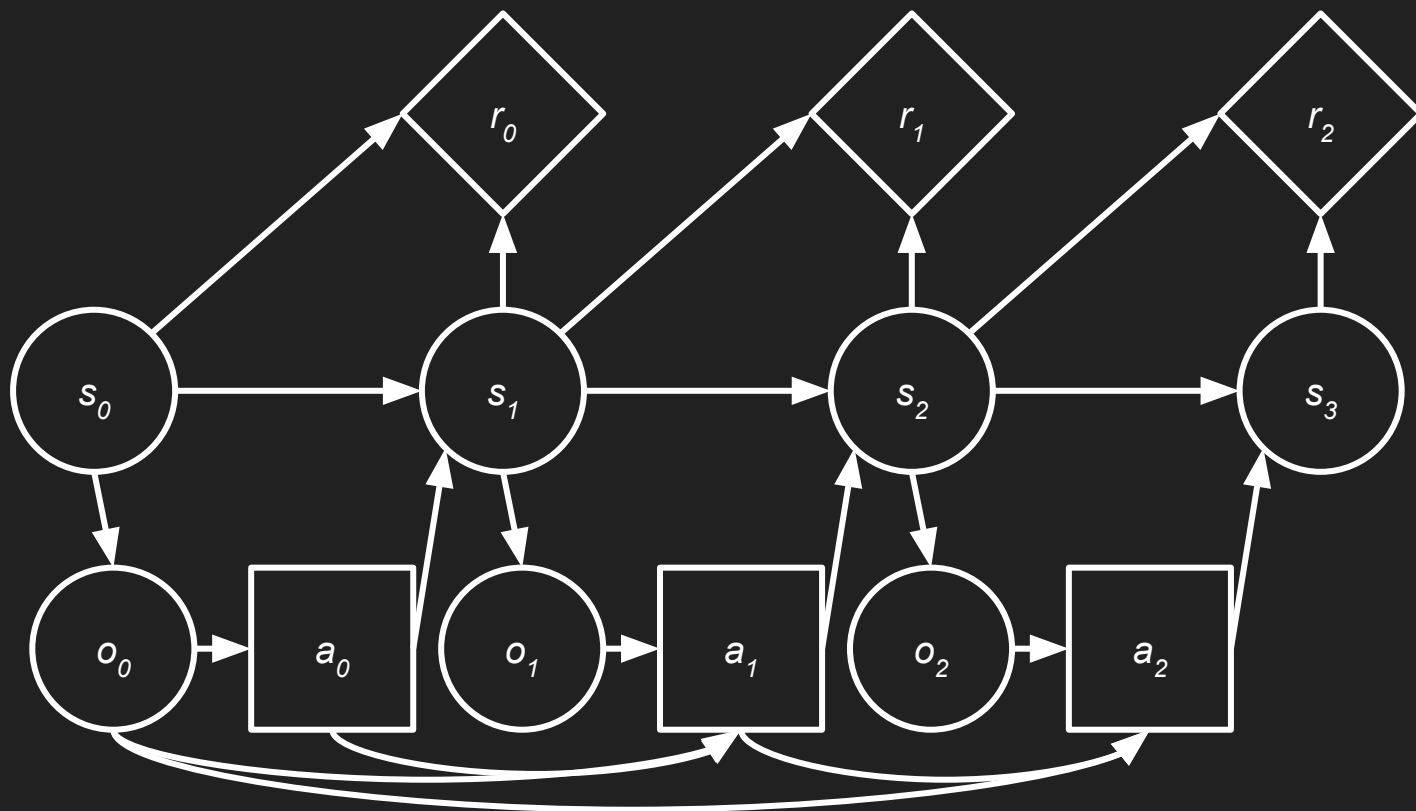
$R: S \times A \rightarrow \mathbb{R}$, reward function

$o \in \Omega$, an observation from the set of observations

$O(o_{t+1} | s_{t+1}, a_t)$ is the conditional observation probabilities

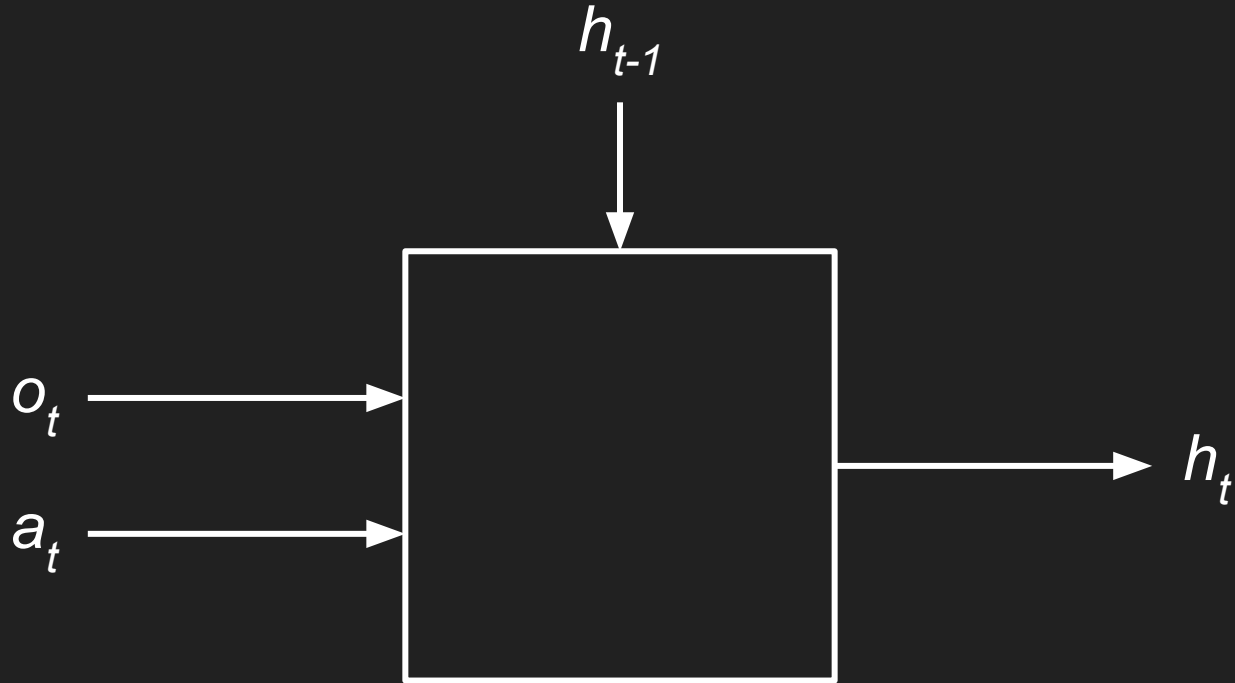
$\gamma \in [0,1]$ is the discount factor

From MDP to POMDP: A Problem



How to act on *all* past information?

Option 1: Remember (RNN)



How to act on all past information?

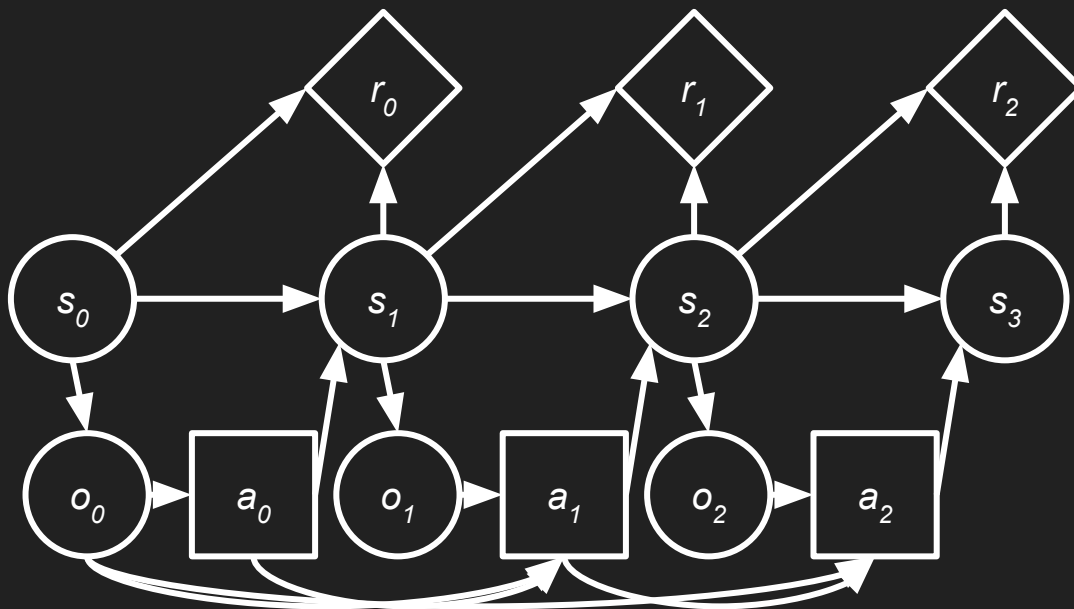
Option 1: Remember (RNN)

- Generalization can be hard.
- No notion of stochasticity.
- Continuous cases are hard.

Option 2: Belief

$$b_t := p_\theta(s_t | o_{\leq t}, a_{\leq t})$$

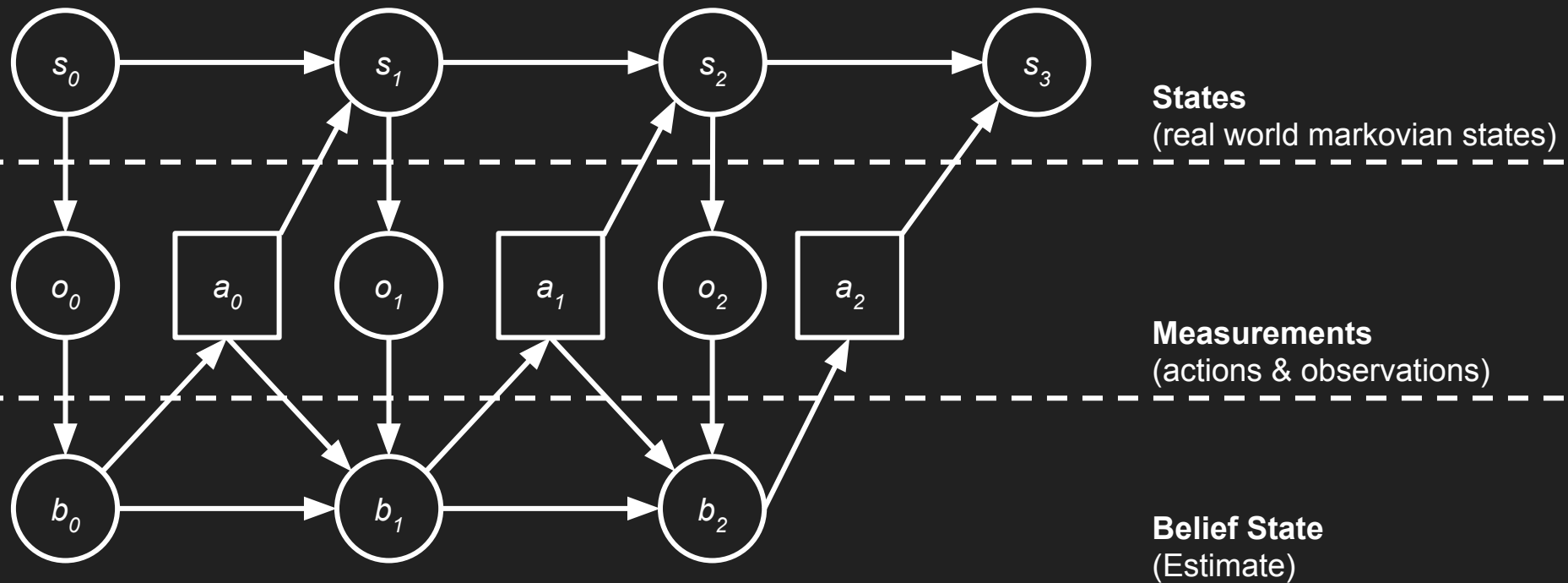
Belief state



Option 2: Belief

$$b_t := p_\theta(s_t | o_{\leq t}, a_{\leq t})$$

Belief state



Option 2: Belief

$T = p_{\theta}(s_t | s_{t-1}, a_{t-1})$ Transition Matrix

$O = p_{\theta}(o_t | s_t, a_{t-1})$ Observation Matrix

$b_t := p_{\theta}(s_t | o_{\leq t}, a_{\leq t})$ Belief state

$$b_t(s_t) = \frac{O(o_t | s_t, a_{t-1}) \sum_{s_{t-1} \in S} T(s_t | s_{t-1}, a_{t-1}) b(s_{t-1})}{\text{Normalization Factor}}$$

How to act on all past information?

Option 1: Remember (RNN)

- Generalization can be hard.
- No notion of stochasticity.
- Continuous cases are hard.

Option 2: Belief

- Computationally Expensive.
- Requires model.
- Provides stochasticity.
- Tends to generalize.

Not as clear

Model free

RNN
(A)DRQN

**Explicit
Belief tracking**

DVRL

**Implicit
Belief tracking**

Next Session

Not as clear

Model free

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Next Session

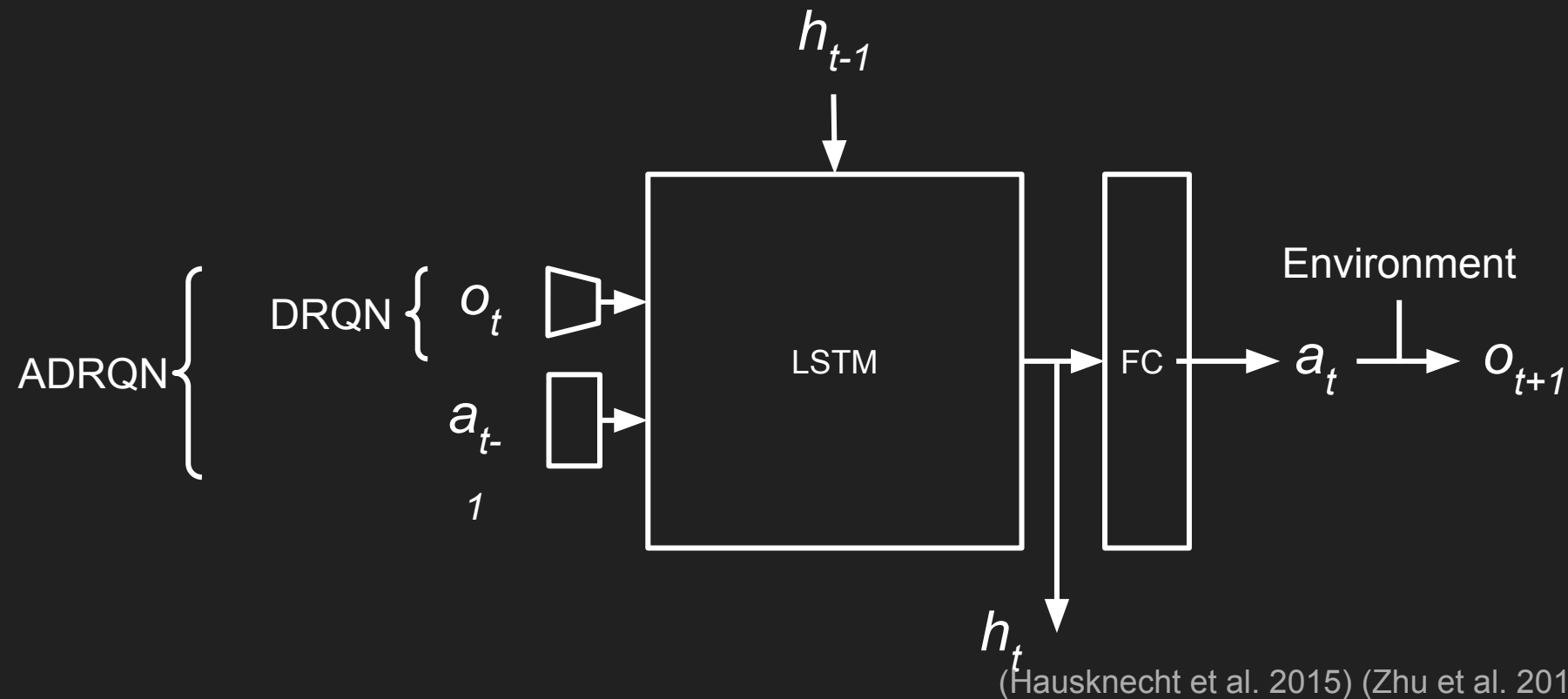
Deep Q-learning approaches for POMDPs

| Model | Input | Problem Addressed |
|-------|--|-------------------|
| DQN | s_t | model-free POMDP |
| DBQN | b_t | Model-based POMDP |
| DRQN | $\langle o_1, o_2, \dots, o_t \rangle$ | Model-free POMDP |
| DDRQN | $\langle a_0, a_1, \dots, a_{t-1} \rangle$ $\langle o_1, o_2, \dots, o_t \rangle$ | Model-free POMDP |
| ADRQN | $\langle (a_0, o_1), (a_1, o_2), \dots, (a_{t-1}, o_t) \rangle$ | Model-free POMDP |

Deep Q-learning approaches for POMDPs

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| ADRQN | $\langle (a_0, o_1), (a_1, o_2), \dots, (a_{t-1}, o_t) \rangle$ | Model-free POMDP |

(Action-specific) Deep Recurrent Q-Learning: (A)DRQN



Flickering Frostbite and Pong



(A)DQRN: Results

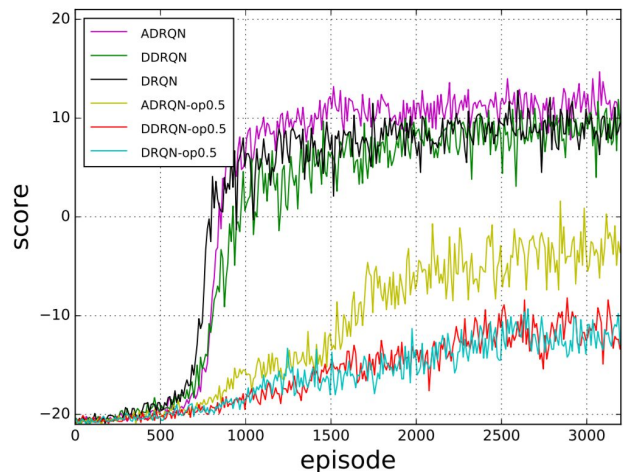


Figure 2: Training results for Pong

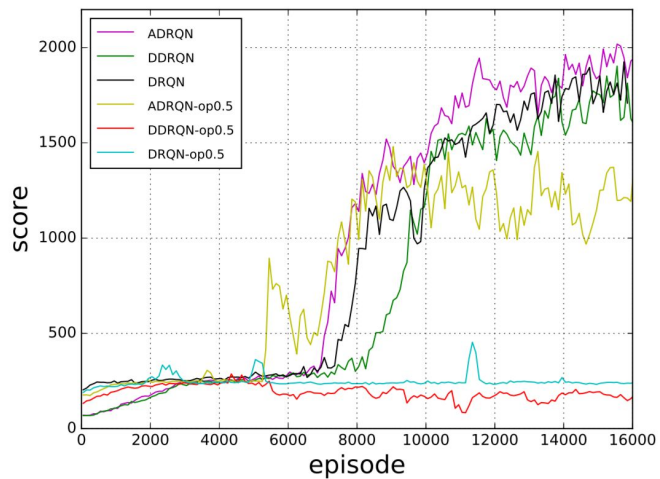
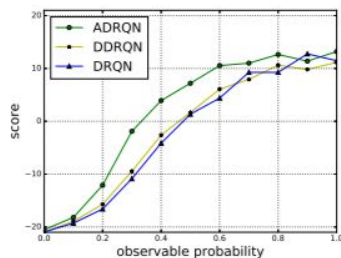
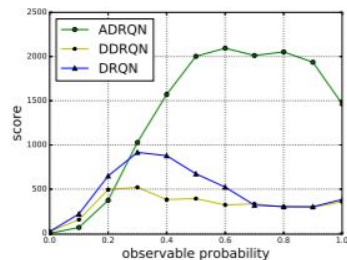


Figure 3: Training results for Frostbite

(A)DQRN: Results

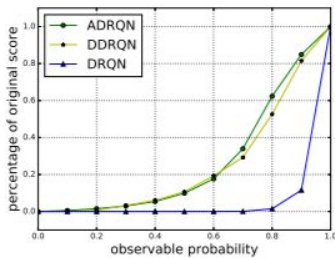


(a) Game Pong

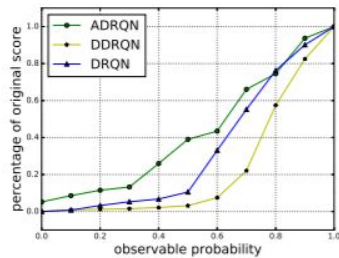


(b) Game Frostbite

Train on POMDP, test on MDP



(a) Game Pong



(b) Game Frostbite

Train on MDP, test on POMDP

(A)DQRN: Critique

Model-free & Blackbox:

likely to summarize and not generalize

Next

Model free

RNN
(A)DRQN

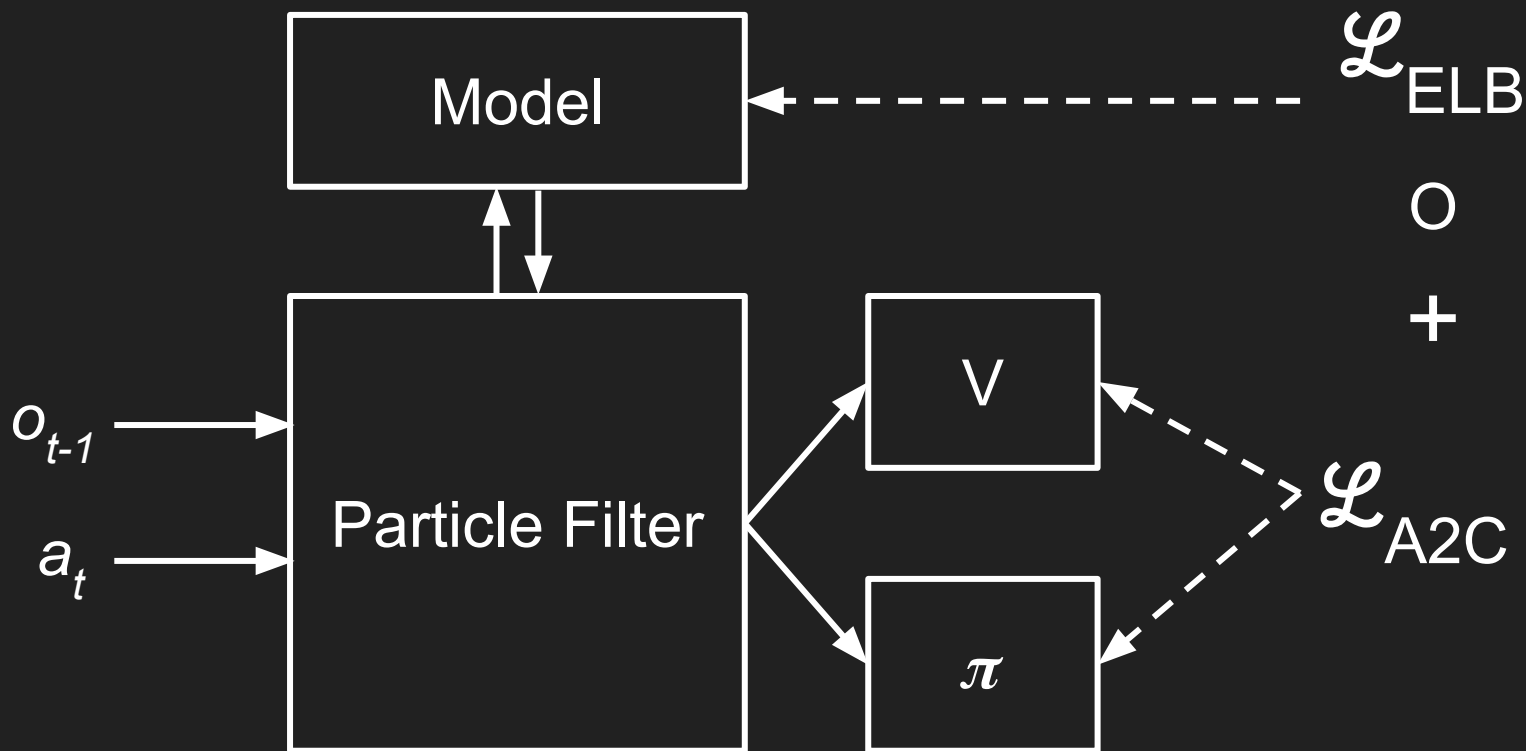
**Explicit
Belief tracking**

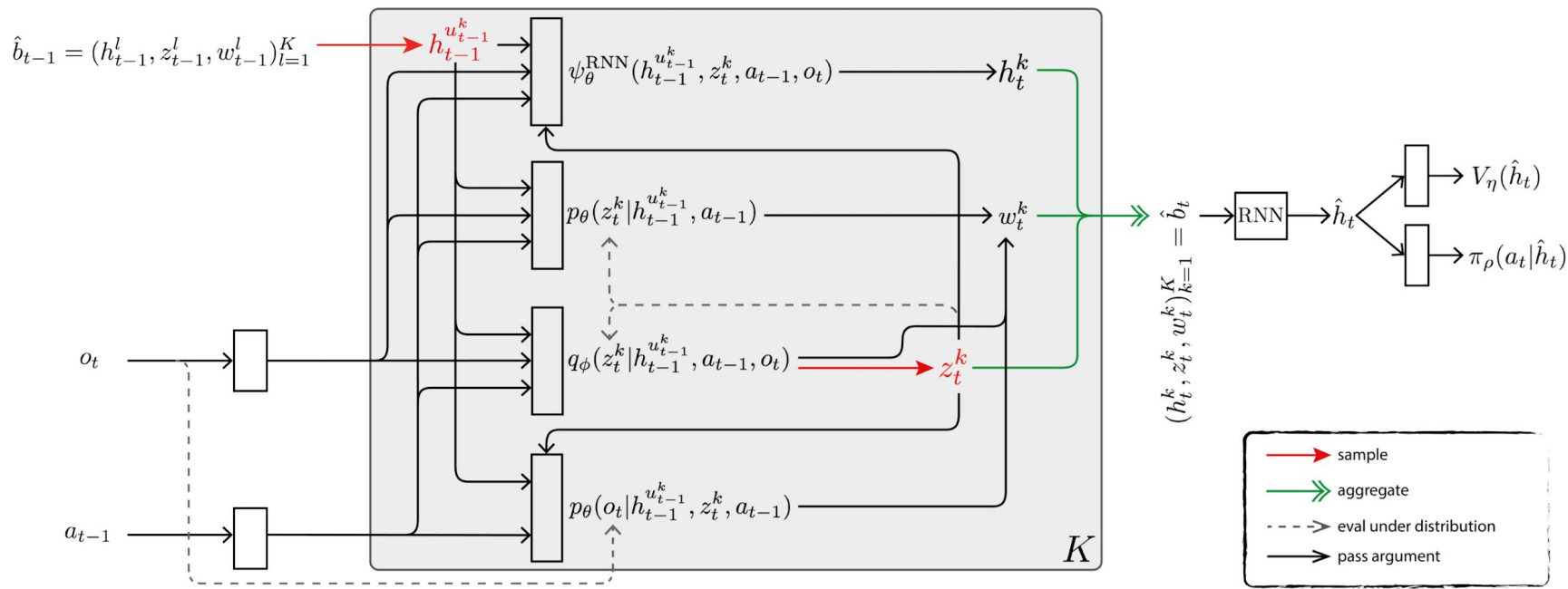
DVRL

**Implicit
Belief tracking**

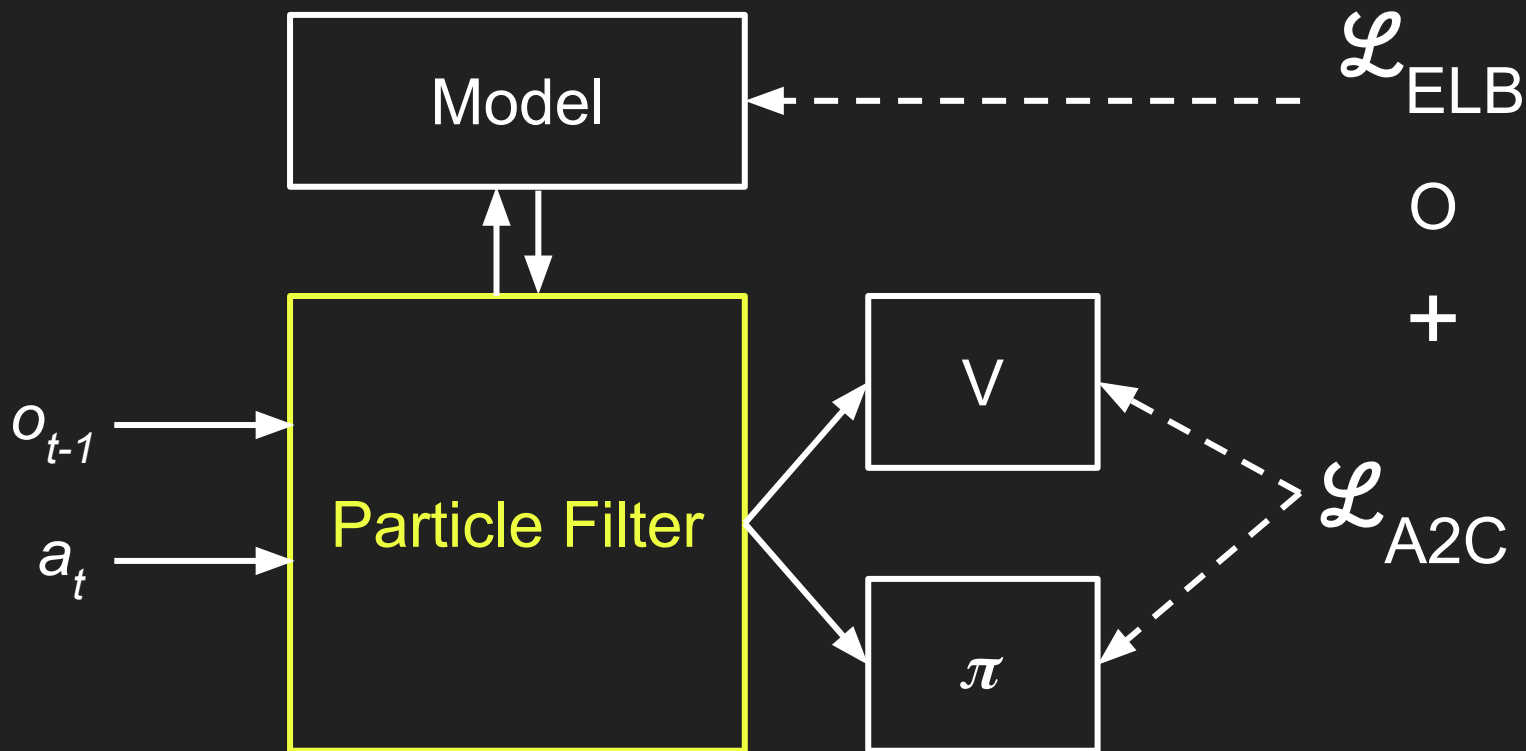
Next Session

Deep Variational Reinforcement Learning (DVRL)

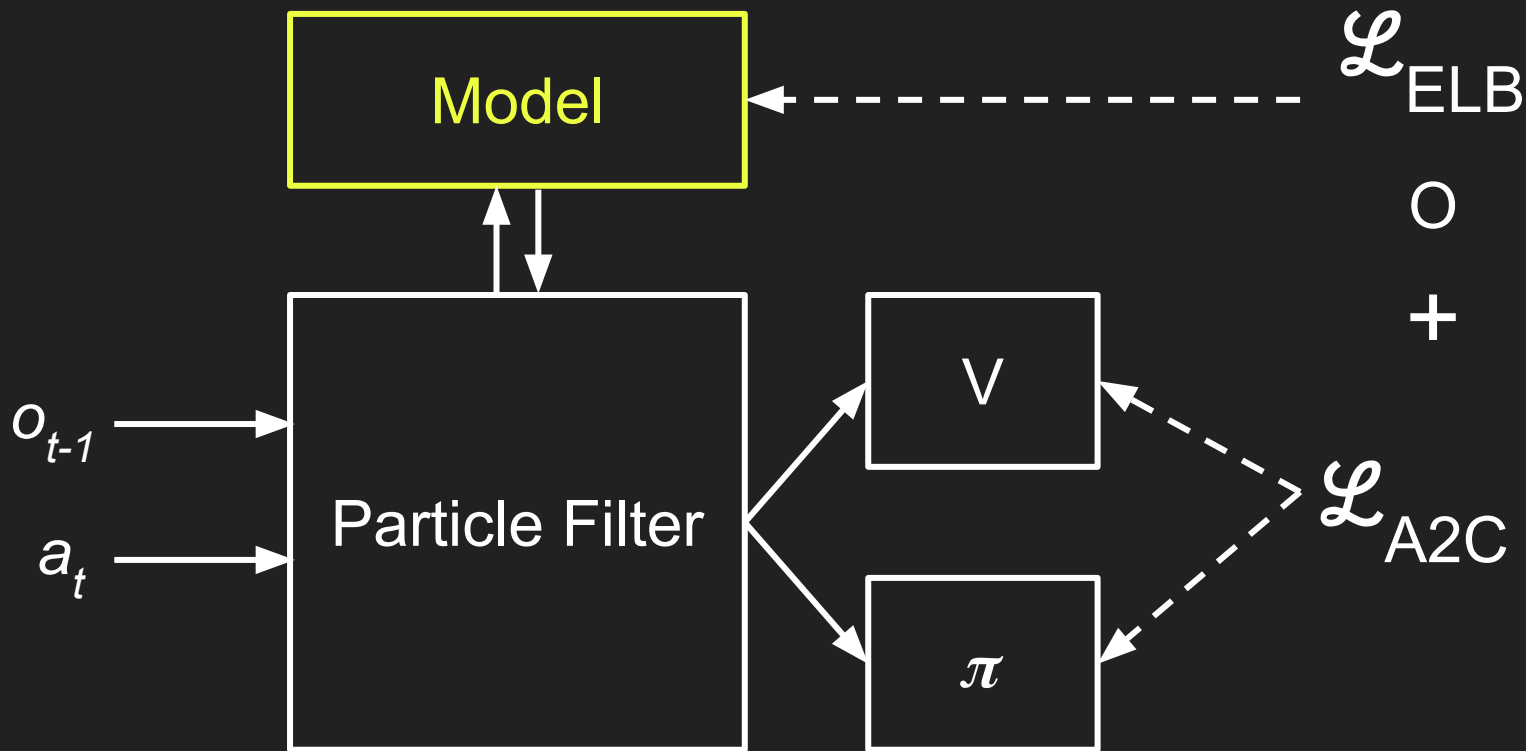




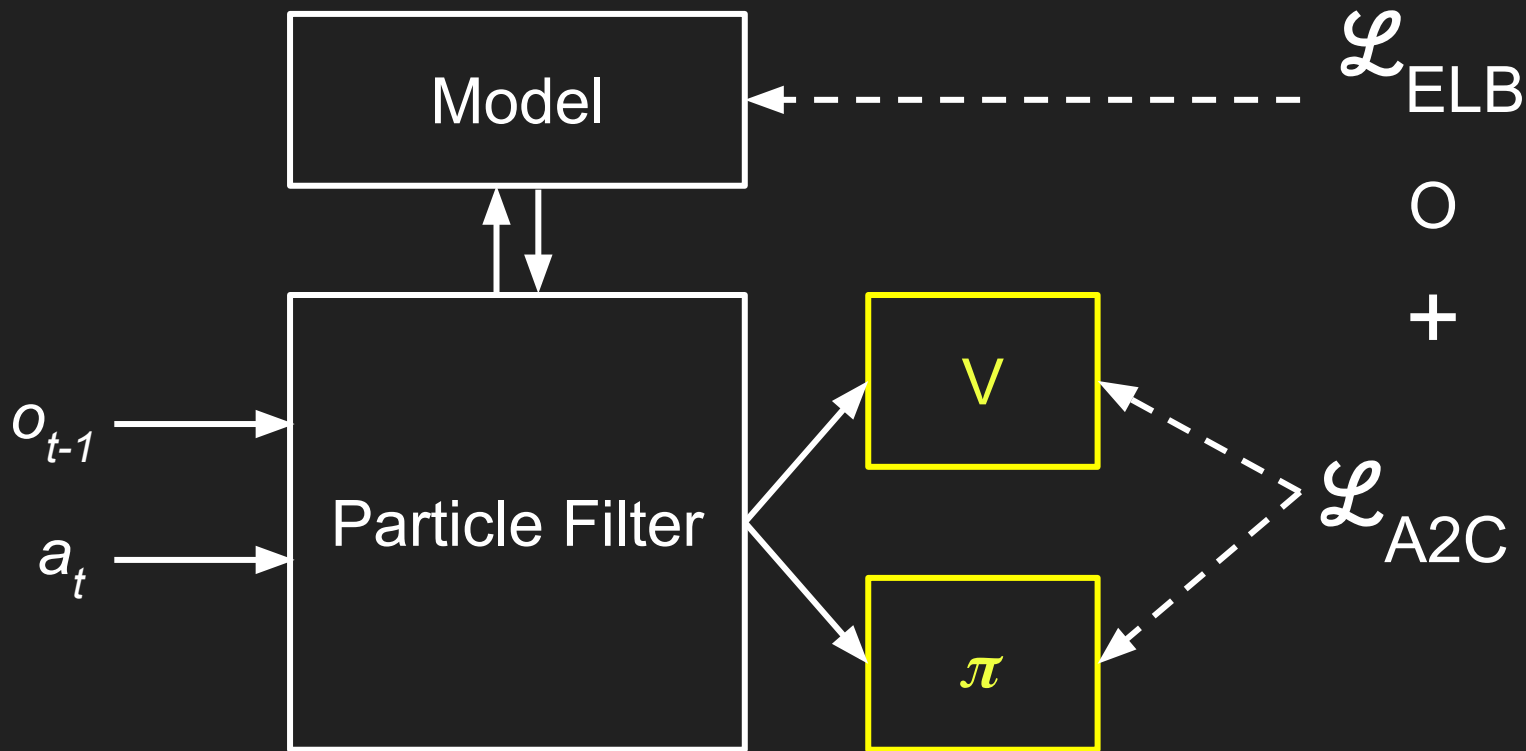
Deep Variational Reinforcement Learning (DVRL)



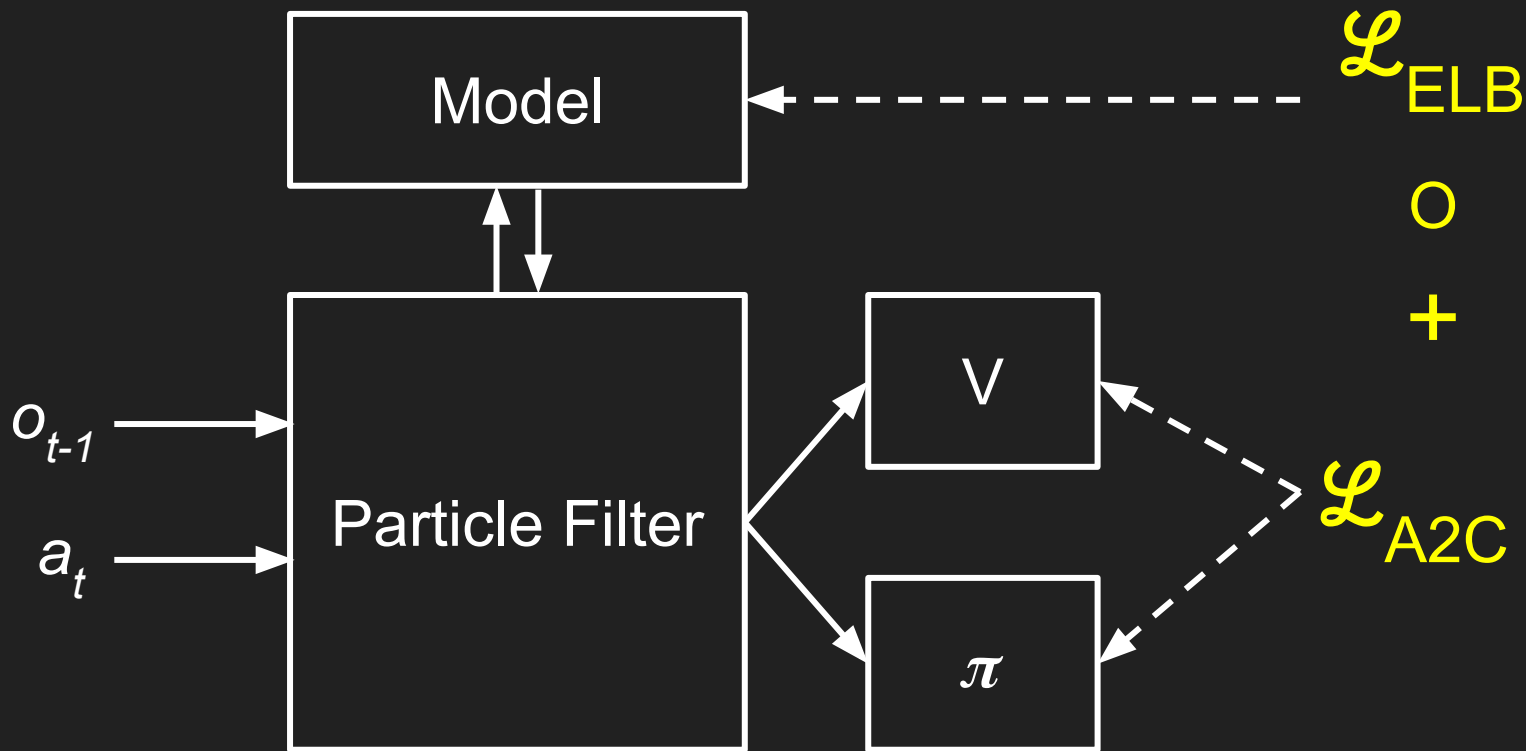
Deep Variational Reinforcement Learning (DVRL)



Deep Variational Reinforcement Learning (DVRL)



Deep Variational Reinforcement Learning (DVRL)



Brief note on notation

a_t = action at time t

o_t = observation at time t

k in $[1, K]$ = number of particles

$b_t = (h_t, z_t, w_t)$ belief at time t

z_t = an additional stochastic latent state

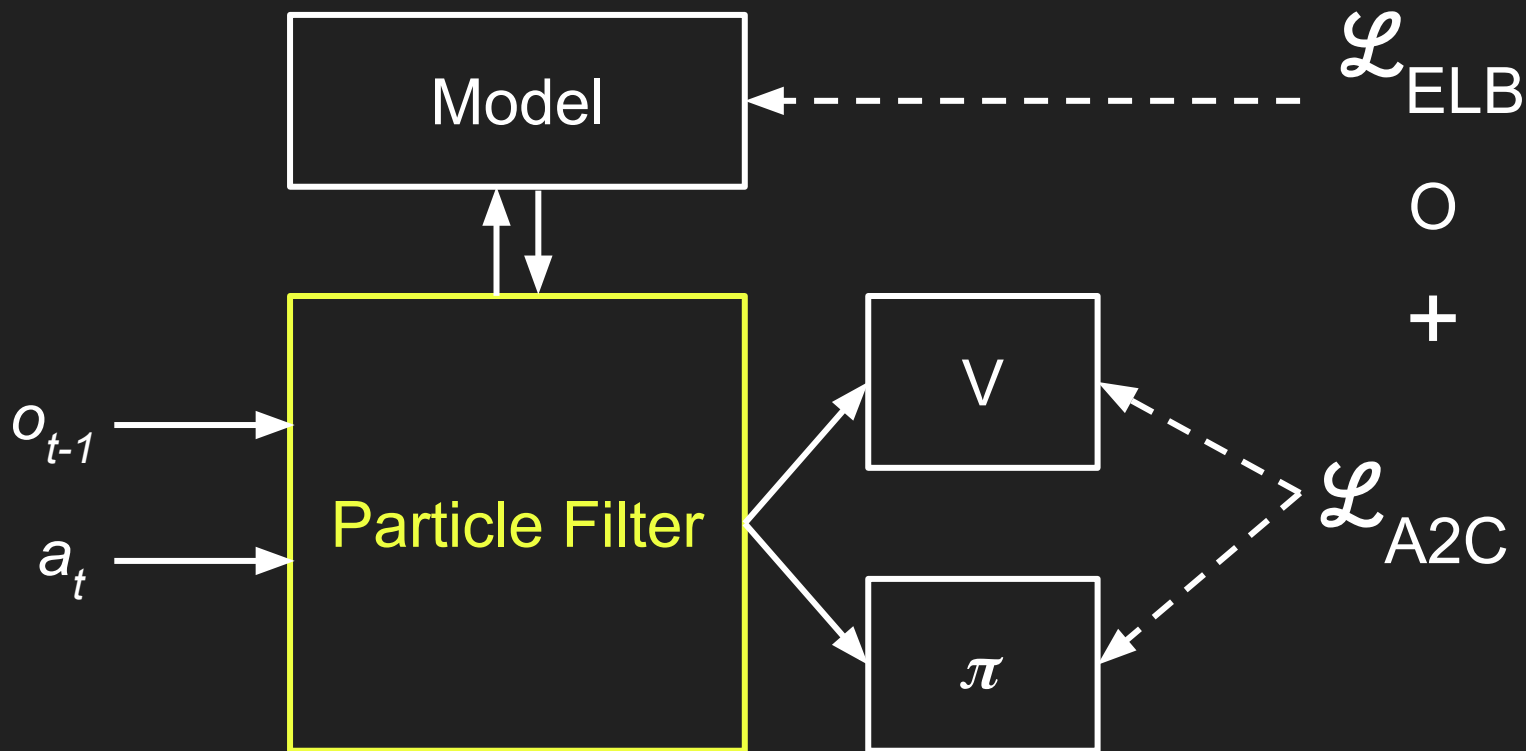
h_t = latent state of a RNN (in a particle)

w_t = importance weight of a particle.

} Latent Summary of state

} Likelihood of that latent state

Deep Variational Reinforcement Learning (DVRL)



DVRL: Particle Filter - Approximating b_t

Previous Belief

$$b_{t-1} = (h_{t-1}^k, z_{t-1}^k, w_{t-1}^k)_{k=1}^K$$

Sample new values

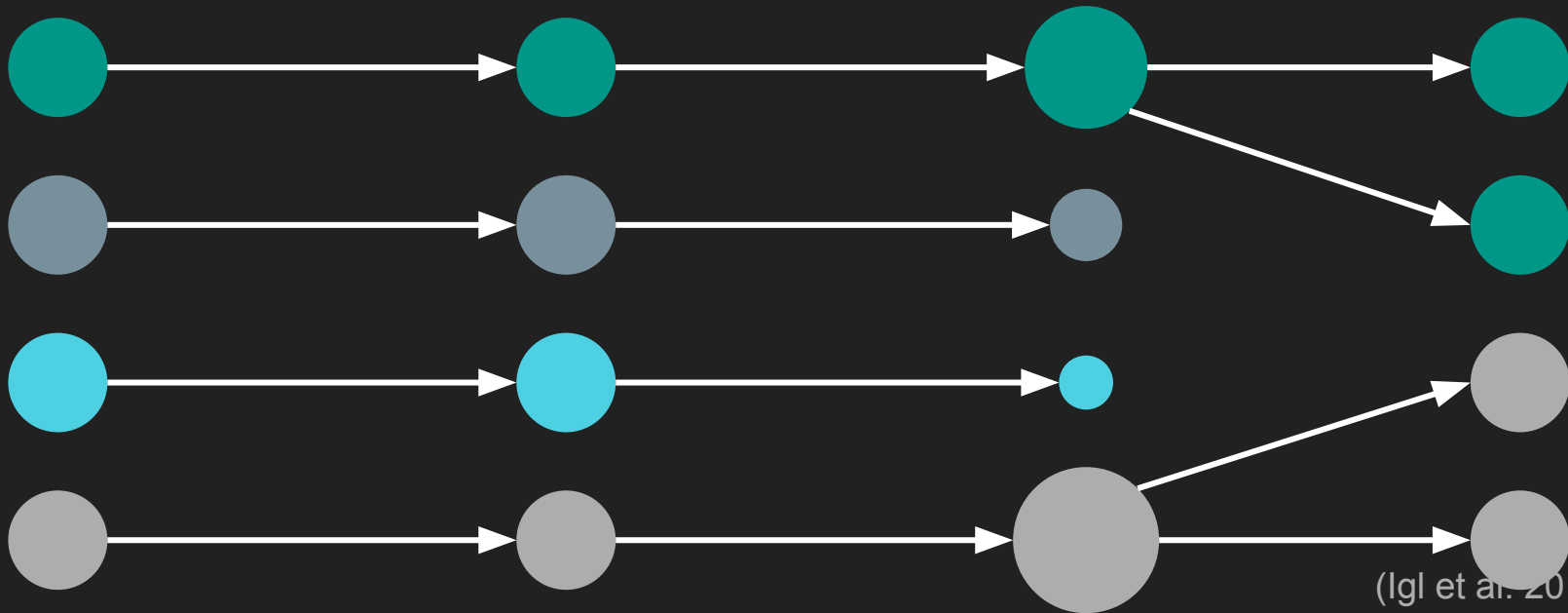
$$z_t \sim q_\phi(z_t | h_{t-1}, a_{t-1}, o_t)$$
$$h_t = \psi_\theta^{RNN}(z_t, h_{t-1}, a_{t-1}, o_t)$$

re-weight

$$w_t = \frac{p_\theta(z_t | h_{t-1}, a_{t-1}) p_\theta(o_t | h_{t-1}, z_t, a_{t-1})}{q_\phi(z_t | h_{t-1}, a_{t-1}, o_t)}$$

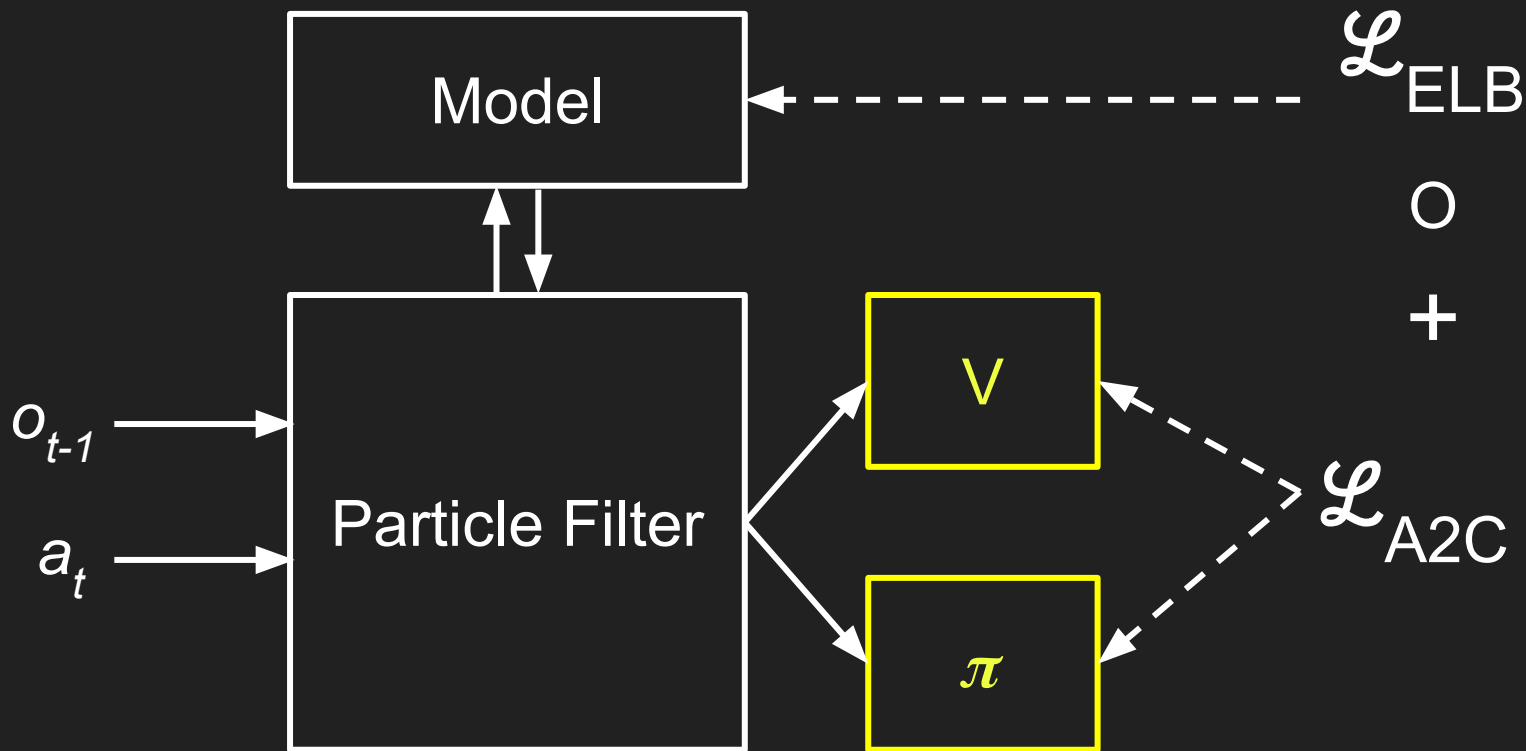
resample

$$b_t = (h_t^k, z_t^k, w_t^k)_{k=1}^K$$

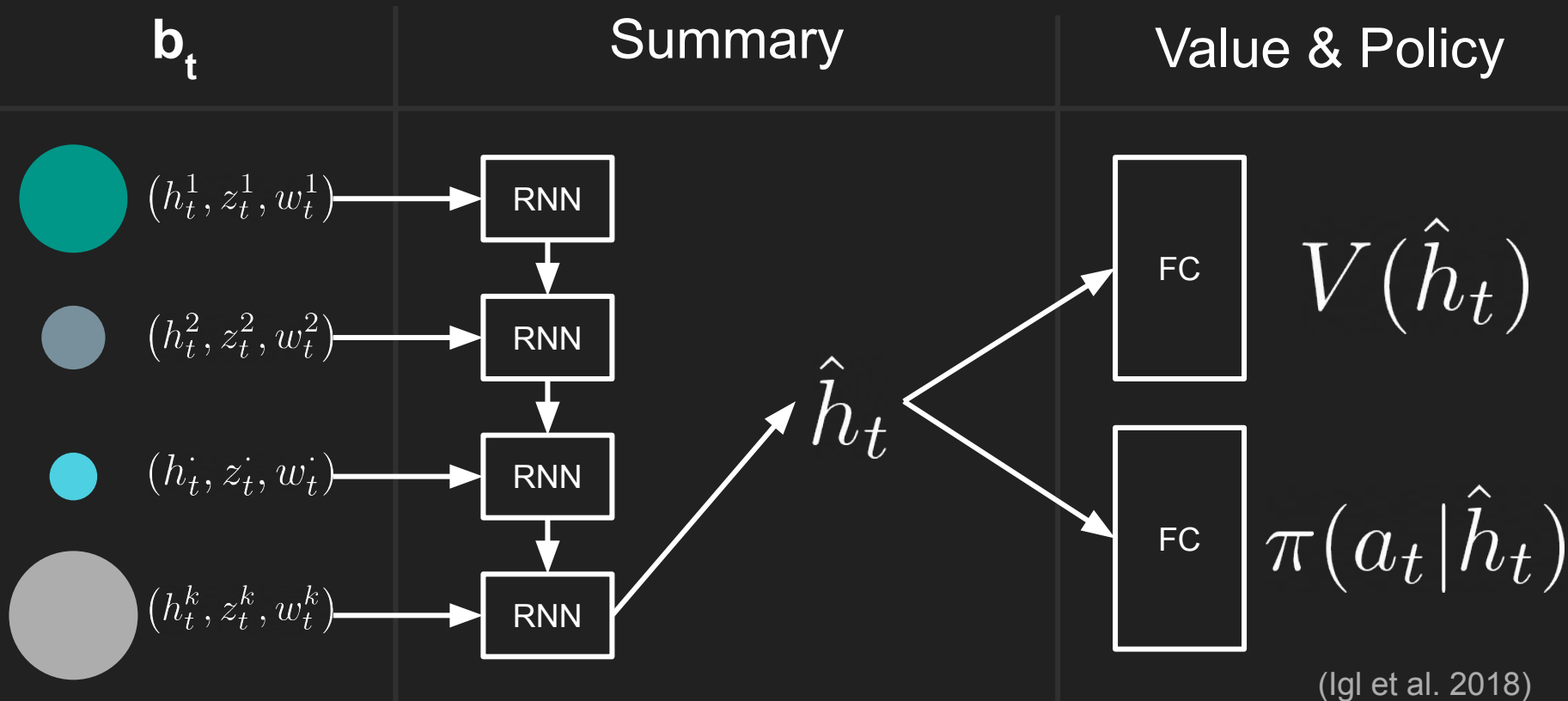


(Igl et al. 2018)

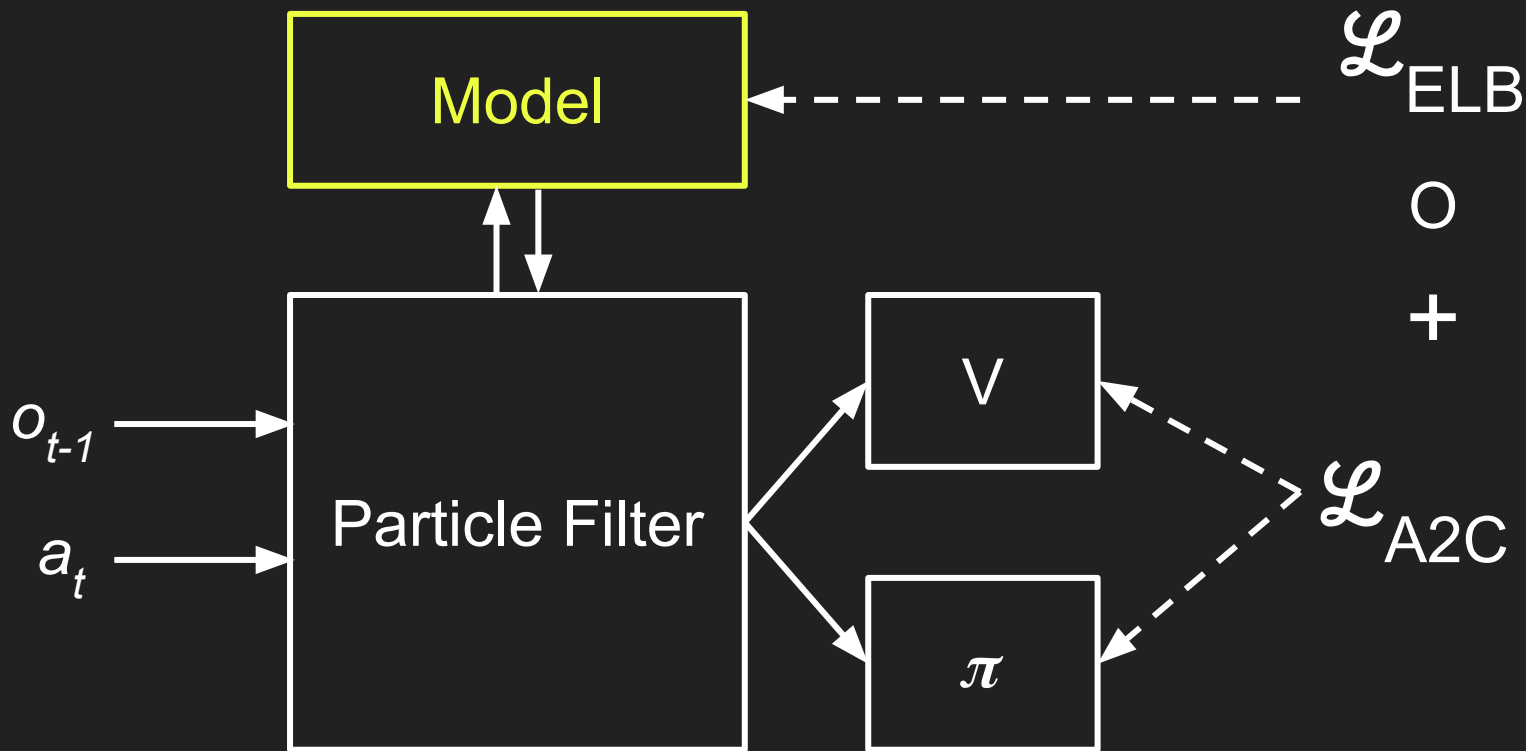
Deep Variational Reinforcement Learning (DVRL)



DVRL: Policy - Summarize the particles



Deep Variational Reinforcement Learning (DVRL)



DVRL: Model

$$w_t = \frac{p_\theta(z_t | h_{t-1}, a_{t-1}) p_\theta(o_t | h_{t-1}, z_t, a_{t-1})}{q_\phi(z_t | h_{t-1}, a_{t-1}, o_t)}$$

$p_\theta(o_t | h_{t-1}, z_t, a_{t-1})$

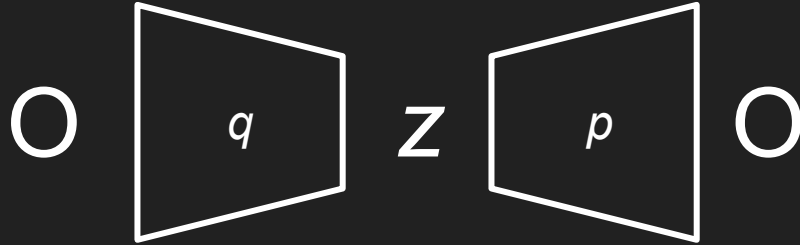
DVRL: Model

$$q_{\phi}(z_t | h_{t-1}, a_{t-1}, o_t) \quad p_{\theta}(o_t | h_{t-1}, z_t, a_{t-1})$$

DVRL: Model

Encoder

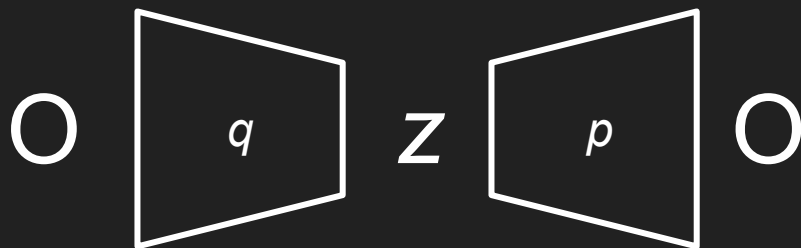
Decoder



$$q_{\phi}(z_t | h_{t-1}, a_{t-1}, o_t)$$

$$p_{\theta}(o_t | h_{t-1}, z_t, a_{t-1})$$

DVRL: Model



Prior

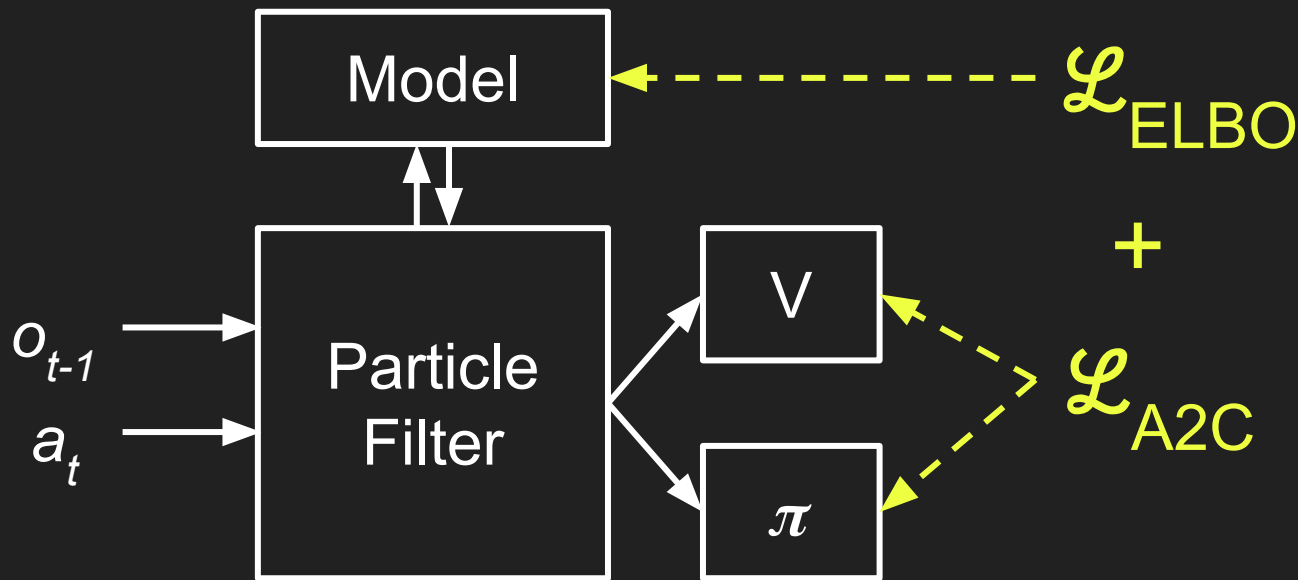
Decoder

$$w_t = \frac{p_\theta(z_t | h_{t-1}, a_{t-1}) p_\theta(o_t | h_{t-1}, z_t, a_{t-1})}{q_\phi(z_t | h_{t-1}, a_{t-1}, o_t)}$$

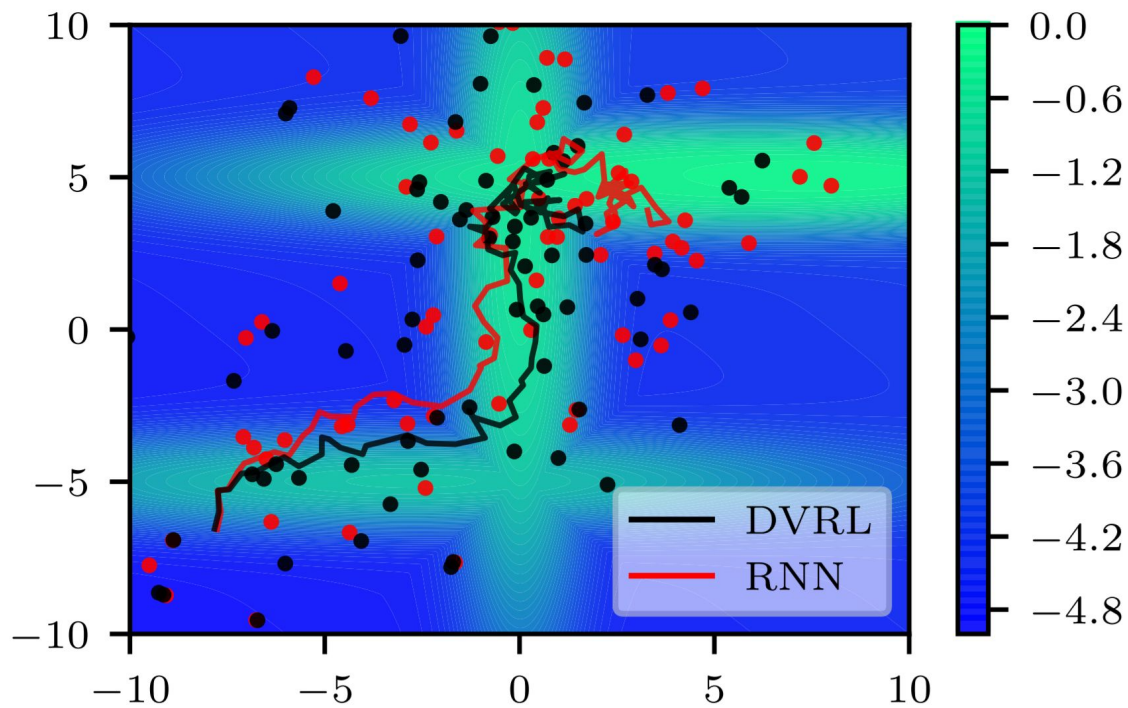
Encoder

$$ELBO(\theta, \phi) \approx \sum_{t=1}^T \log \left(\frac{1}{K} \sum_{k=1}^K w_t^k \right)$$

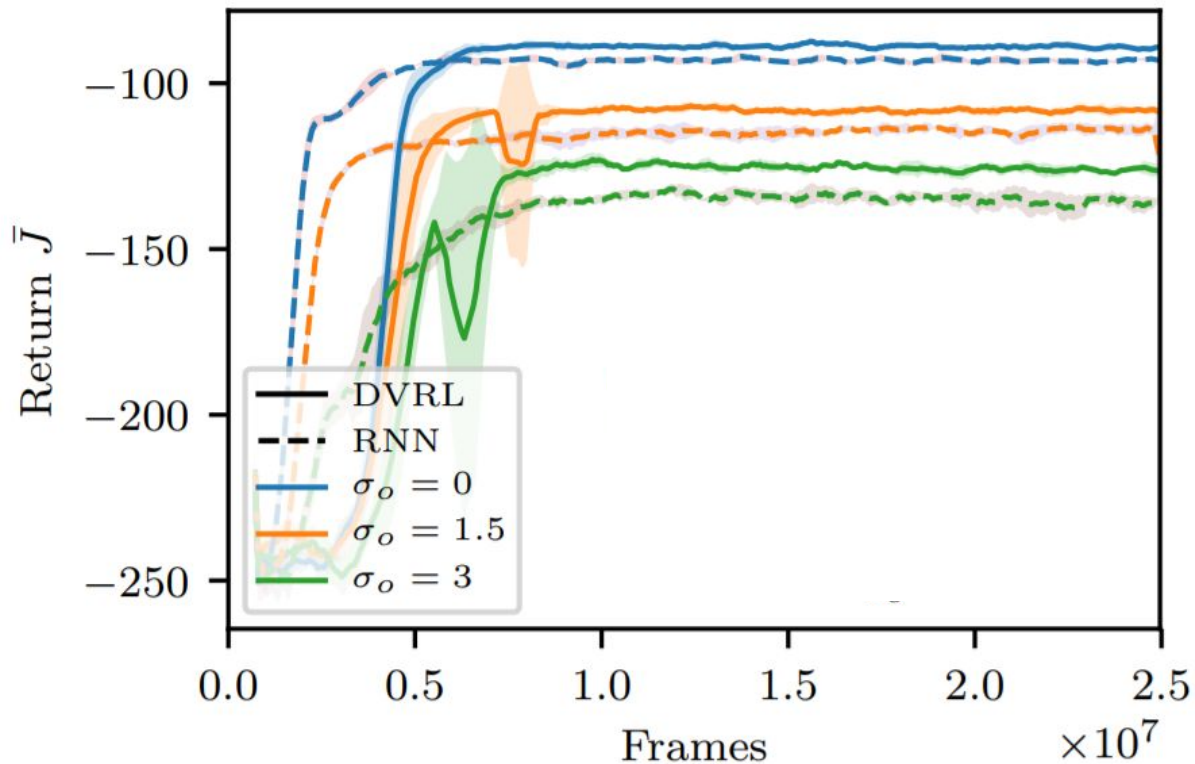
DVRL: Joint Learning



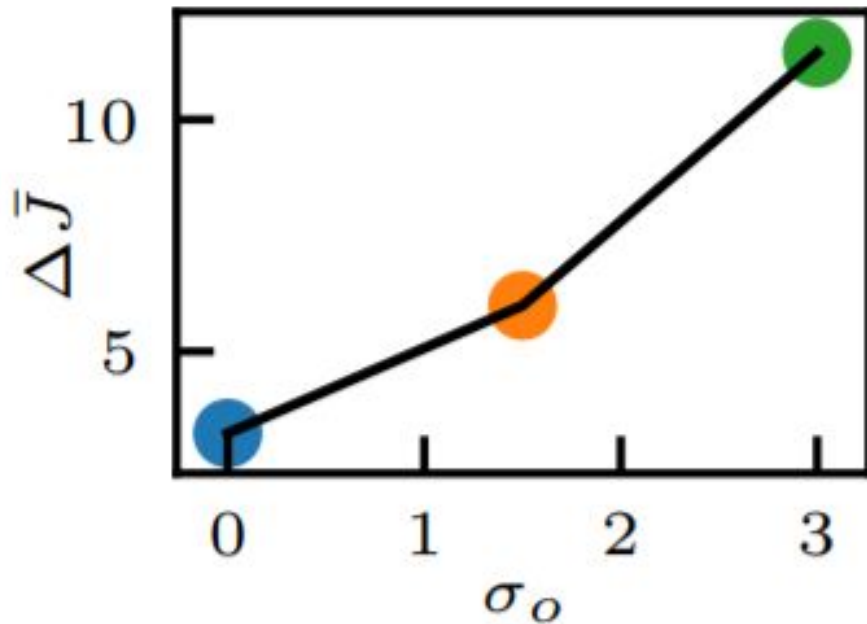
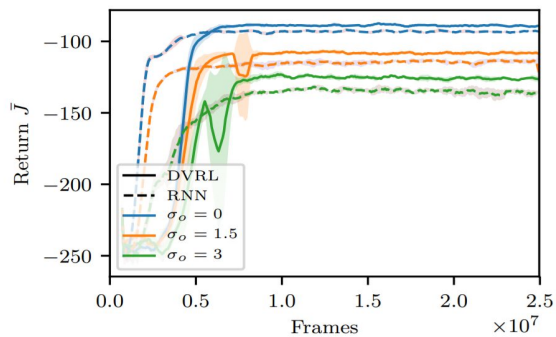
DVRL: Results - noisy MountainHike



DVRL: Results - noisy MountainHike



DVRL: Results - noisy MountainHike

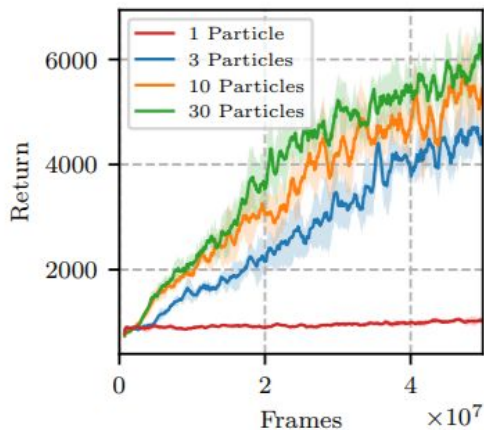


ChopperCommand

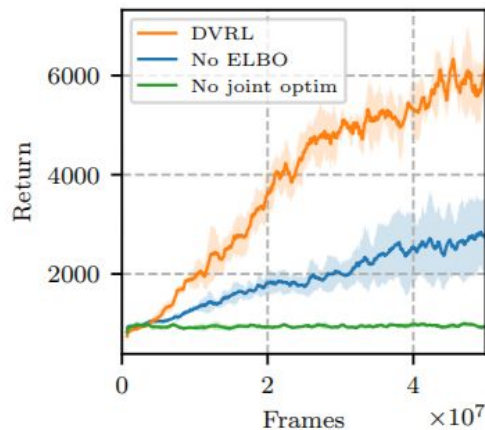


By DePaula

Results: Ablation on Atari



(a) Influence of the particle number on performance for DVRL. Only using one particle is not sufficient to encode enough information in the latent state.



(b) Performance of the full DVRL algorithm compared to setting $\lambda^E = 0$ ("No ELBO") or not backpropagating the policy gradients through the encoder ("No joint optim").

DVRL: Critique

The belief state is still a rough approximation.

Is this really the best way to learn it?

Summary

- Extended MDP to POMDP
- (A)DRQN
- DVRL

Discussion

In a POMDP we still assume full access to the reward.

- 1) This not a realistic case (our perception of the reward depends as much on our observations as the state)
- 2) If it is realistic, our belief should be updated based on the reward.

Next

Model free

RNN
(A)DRQN

**Explicit
Belief tracking**

DVRL
DPFRL

**Implicit
Belief tracking**

VRM

References

Hausknecht, M., & Stone, P. (2015, September). *Deep recurrent q-learning for partially observable mdps*. In 2015 AAAI Fall Symposium Series.

Igl, M., Zintgraf, L., Le, T. A., Wood, F., & Whiteson, S. (2018). *Deep variational reinforcement learning for pomdps*. arXiv preprint arXiv:1806.02426.

Zhu, P., Li, X., Poupart, P., & Miao, G. (2017). *On improving deep reinforcement learning for pomdps*. arXiv preprint arXiv:1704.07978.