# Meta Reinforcement Learning

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# Outline

- Motivation for meta-reinforcement learning
- Problem setups (RL, meta learning, meta-RL)
- Common approaches
  - Black-box adaptation (based on recurrent policies)
  - Optimization-based methods
  - Inference-based methods (solving equivalent POMDP)
- Comparison
- Task design (unsupervised meta-RL)
- Summary and conclusions

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#### Why do we care about meta-rl?



Deepmind. Grandmaster level in StarCraft II using multi-agent reinforcement learning [2019]

RoboschoolHumanoid-v0



- Humans can learn new skills very quickly, efficiently adapting to new environments and tasks.
- Can we design algorithms that **learn to** reinforcement learn?

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#### The reinforcement learning problem

*Markov Decision Process* :  $M = \{S, \mathcal{A}, \mathcal{P}, r\}$ 

S: state space  $\Re$ : action space  $\Re$ : transition probability,  $p: S \times \Re \rightarrow S$ r: reward function,  $r: S \times \Re \rightarrow \mathbb{R}$ 

 $\pi(a|s)$ : the policy,  $\pi: S \to \Delta(\mathcal{A})$  or  $\pi: S \to \mathcal{A}$ 

*Transitions* :  $\{s_t, a_t, r_t, s_{t+1}\}_i$ *Trajectory* :  $\tau = \{s_0, a_0, r_0, s_1, a_1, r_1, ..., s_T, a_T, r_T\}$ 



# The reinforcement learning problem

#### Goal :

learn a policy that maximizes the expected (discounted) sum of rewards

Parameterized policy (infinite horizon):

$$\theta^* = \arg \max_{\theta} \mathbb{E}_{\pi_{\theta}} \left[ \sum_{t=0}^{\infty} \gamma^t r(s_t, a_t) \right]$$

Expectation over (discounted) state visitation distribution  $\theta^* = \arg \max_{\theta} \mathbb{E}_{\pi_{\theta}(s,a)}[r(s,a)]$ 

# General procedure



1. get initial state  $s_0 \sim p(s)$ 

2. choose an action from policy  $a_t \sim \pi_{\theta}(\cdot | s_t)$ 

3. observe reward  $r_t = r(s_t, a_t)$  and new state  $s_{t+1} \sim p(\cdot | s_t, a_t)$ 

4. optimize  $\theta^* = \arg \max_{\theta} \mathbb{E}_{\pi_{\theta}}[R(\tau)]$ 

5. store experiences  $(s_t, a_t, s_{t+1}, r_t)$  in replay buffer

6. repeat until convergence

How do we optimize our policy?

policy gradient
 value function or Q function estimation
 model learning + MPC

## The meta learning problem

 $\theta$  : meta parameter  $\phi_i$  : task specific adaptation parameter p(D) : a distribution over meta training dataset (or tasks)

*learn*  $\theta$  *such that*  $\phi_i = f_{\theta}(\mathfrak{D}_i^{tr})$  *fits*  $\mathfrak{D}_i^{ts}$  *well* 

Probabilistic view :

$$\theta^* = \arg \max_{\theta} \sum logp(\phi_i | \mathcal{D}_i^{ts})$$

Deterministic view :

$$\theta^* = \arg \min_{\theta} \sum \mathcal{L}_i(\phi_i, \mathcal{D}_i^{ts})$$

# Meta learning + RL

Traditional (supervised) learning:  $\theta^* = \arg \min_{\theta} \mathcal{L}(\theta, \mathcal{D})$ Traditional (supervised) meta learning:  $\theta^* = \arg \min_{\theta} \sum \mathcal{L}_i(\phi_i, \mathcal{D}_i^{ts})$  where  $\phi_i = f_{\theta}(\mathcal{D}_i^{tr})$ 

 $\mathfrak{D}_{meta-train} = \left\{ \left( D_0^{tr}, D_0^{ts} \right), \left( D_1^{tr}, D_1^{ts} \right), \dots \right\}$ 



Reinforcement learning :  $\theta^* = \arg \max_{\theta} \mathbb{E}_{\tau \sim \pi_{\theta}}[R(\tau)] = f_{RL}(\mathcal{M})$ Meta reinforcement learning :

 $\theta^* = \arg \max_{\theta} \sum \mathbb{E}_{\tau \sim \pi_{\phi_i}} [R(\tau)] \text{ where } \phi_i = f_{\theta}(M_i)$  $\mathfrak{D}_{meta-train} = \{M_0, M_1, \dots\}$ 



Graph: ICML 2019 tutorial on meta learning

#### Meta learning RL procedure

- 1. [initialization] given a distribution over MDPs p(M), draw  $M_i \sim p(M)$
- 2. [task adaptation] get our policy  $\pi_{\phi_i}$  by the meta learner  $f_{\theta}(\mathcal{M}_i)$
- 3. [data collection] explore or exploit  $M_i$  with  $\pi_{\phi_i}$  and collect experiences
- 4. [meta learning] maximize the meta parameter  $\theta$  with collected data 5. repeat

#### Core problem

$$\theta^* = \arg \max_{\theta} \sum \mathbb{E}_{\tau \sim \pi_{\phi_i}}[R(\tau)] \text{ where } \phi_i = f_{\theta}(M_i)$$

How do we design  $f_{\theta}(M_i)$ ? What does  $f_{\theta}(M_i)$  do?

- 1.  $f_{\theta}$  improves the policy with experiences from  $M_i$
- 2.  $f_{\theta}$  can also choose how to interact with  $M_i$  (exploration vs exploitation)

### Popular approaches to meta-rl

- Memory-based approach (black-box adaptation)
  - Recurrent policy (RNN, LSTM)
  - Attention + temporal convolution
  - Mean field assumption
- Optimization-based approach
  - MAML and its variants
- POMDP perspective
  - Task inferences and embedding

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- Key idea: in order to learn a **"good"** prior, we need to somehow 1) **"memorize"** experiences we've seen so far, 2) and to "**adapt**" quickly to new tasks with our memory.
- "Good" prior:
  - Internalize the dynamics about the MDP; interactions with previous tasks help future tasks
- "Memorization":
  - Recurrent networks, temporal convolutions + attentions
- "Adapt":
  - Few shot experiences from the test MDP lead to a decent policy

- Key idea: in order to learn a **"good"** prior, we need to somehow 1) **"memorize"** experiences we've seen so far, 2) and to **"adapt"** quickly to new tasks with our memory.
- Recipe:
  - Augmented "observation space": include **past experience (states, actions, rewards)**
  - A policy that takes into account all its past trajectory in a MDP by using this augmented observation (RNN policy for example)



- Key idea: in order to learn a **"good"** prior, we need to somehow 1) **"memorize"** experiences we've seen so far, 2) and to "**adapt**" quickly to new tasks with our memory.
- Procedures:
  - Sample a new MDP
  - Reset the hidden state
  - Collect trajectories and update the model by **maximizing total return** (using RL algorithms)



Wang et al. Learning to Reinforcement Learn [2016]



- Key idea: in order to learn a **"good"** prior, we need to somehow 1) **"memorize"** experiences we've seen so far, 2) and to "**adapt**" quickly to new tasks with our memory.
- How to design architectures for the memory?
  - RNN, LSTM, GRU
  - Attention + temporal convolution



Duan et al. RL^2: Fast Reinforcement Learning via Slow Reinforcement Learning [2016]



Mishra, Rohaninejad et al. A Simple Neural Attentive Meta-Learner [2018]

- Problems?
  - **[Learnability]** Memory (gradient vanishing/explosion during BPTT, etc)
  - **[Data efficiency]** Works mostly in conjunction with on-policy RL algorithms
  - **[Optimality]** Trade-offs between exploration and exploitation

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- Most of the works in this category is based on ideas from MAML.
- Learn a proper **initialization** of the parameters so that after **few-shot experiences** from the new MDP, the policy nicely **adapts** to the new task.
- The learned meta parameter lies in the parameter space where it's close to the optimal task specific parameters on average.
- The meta parameters and the task-specific parameters coincide.

• A quick recap of MAML (meta-rl as an optimization problem)

Meta reinforcement learning goal :

 $\theta^* = \arg \max_{\theta} \sum \mathbb{E}_{\tau \sim \pi_{\phi_i}}[R(\tau)] \text{ where } \phi_i = f_{\theta}^{generic}(\mathcal{M}_i)$ 

In MAML we have  $\theta \equiv \phi$ , so the goal of MAML RL:  $\theta^* = \arg \max_{\theta} \sum \mathbb{E}_{\tau \sim \pi_{\theta_i}}[R(\tau)]$  where  $\theta_i = f_{\theta}^{MAML}(M_i)$ 

Where the meta learner takes a specific form :  $f_{\theta}^{MAML}(\mathbf{M}_i) = \theta + \alpha \nabla_{\theta} J_i(\theta)$ 

When in the context of reinforcement learning:  $J_i(\theta) = \mathbb{E}_{\tau \sim \pi_{\theta}}[R(\tau)]$ , the expected sum of rewards in  $M_i$ 

*Which can be estimated by interacting with*  $M_i$ 



Recipe:

*In traditional RL, we optimize our parameter via* :  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$ 

In MAML, we optimize our parameter via :

 $\theta \leftarrow \theta + \beta \underbrace{\sum_{i}}_{over \ all \ tasks} \nabla_{\theta} J_i \underbrace{\left( \underbrace{\theta + \alpha \nabla_{\theta} J_i(\theta)}_{per \ task \ adaptation} \right)}_{per \ task \ adaptation}$ 

• Interpretations:

 $\begin{array}{c} & ---- \text{meta-learning} \\ & ---- \text{learning/adaptation} \\ & \nabla \mathcal{L}_3 \\ & \nabla \mathcal{L}_2 \\ & \nabla \mathcal{L}_1 \\ & & \nabla \mathcal{L}_2 \\ & & & \Theta_3^* \\ & & & & \Theta_2^* \end{array}$ 

- Run one iteration of ascent and update our parameter based on how much such one step optimization can help with the task.
- We want to optimize the parameter so that when we later do one step gradient ascent (task adaptation) on the test task, the objective is maximized in expectation (over the task distribution)

Recipe:

*In traditional RL, we optimize our parameter via* :  $\theta \leftarrow \theta + \alpha \nabla_{\theta} J(\theta)$ 

In MAML, we optimize our parameter via :

$$\theta \leftarrow \theta + \beta \underbrace{\sum_{i}}_{over \ all \ tasks} \nabla_{\theta} J_i \left( \underbrace{\theta + \alpha \nabla_{\theta} J_i(\theta)}_{per \ task \ adaptation} \right)$$

- Procedure:
  - Pick a random task i
  - Make one (or more) gradient step(s) to find its adapted parameter  $\theta + \alpha \nabla_{\theta} J_i(\theta)$
  - Optimize the objective based on how good this adapted parameter performs  $\nabla_{\theta} J_i(\theta + \alpha \nabla_{\theta} J_i(\theta))$
  - So the final parameter results in policy that performs well on average







- Procedure:
  - Pick a random task i
  - Make one (or more) gradient step(s) to find its adapted parameter  $\theta + \alpha \nabla_{\theta} J_i(\theta)$
  - Optimize the objective based on how good this adapted parameter performs  $\nabla_{\theta} I_i(\theta + \alpha \nabla_{\theta} I_i(\theta))$
  - So the final parameter results in policy that performs well on average

- One (or few) shot learning with new sampled goals in robotic controls
  - Major drawbacks
    - Requires Hessian calculation. Tricks for approximation or acceleration?
    - What if the optimal parameters are not in the vicinity of each other in the parameter space? Do we have guarantees on the generalization and adaptation power?



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- How is meta-rl fundamentally different from generic reinforcement learning?
- Or is it different?
- In fact, meta-rl can be seen as a regular reinforcement learning except that the state has to be partially observable.

• A quick recap of partially observed Markov decision process

Augment a regular MDP with observation space and emission probability

 $M = \{S, \mathcal{A}, \mathcal{P}, r, \mathcal{E}, \mathbf{O}\} where \\ \mathbf{O}: observation space \\ \mathbf{\mathcal{E}}: emission probability, i.e. p(o_t|s_t)$ 







- Under POMDPs, policy can only **act on observations** instead of the underlying states.
- POMDPs are known to be **extremely difficult to solve** as it requires reasoning about true states.
- Typically, to solve POMDPs:
  - **State estimations**: model the distribution of states given the observations (history), and apply usual RL procedures to find the optimal policy.
  - **Use policies with memory**: implicitly infer the internal dynamics of the MDP based on previous experiences.

- Meta-rl in the lens of regular rl in POMDPs:
- Key idea:
  - 1. encapsulate task-specific information with a latent variable on which the policy depends
  - 2. Learning involves inferring the task context variable and optimizing the policy



The agents can **grab and move** obje in front of them. The agents can **lock** objects in place. Only the team that locked an object can unlock it.

Regular RL : 1.  $MDP : M = \{S, \mathcal{A}, \mathcal{P}, r\}$ 2.  $policy : \pi_{\theta}(a|s)$  Meta RL in the lens of POMDPs: 1. POMDP:  $\widetilde{M} = \left\{ \widetilde{S}, \mathcal{A}, \widetilde{P}, r, \varepsilon, \mathbf{0} \right\}$  where

 $\widetilde{\mathbf{S}} = \mathbf{S} \times \mathbf{Z}, \text{ the concatenation of the state space and the task context}$   $\widetilde{\mathbf{P}} = p(\widetilde{s}_{t+1} | \widetilde{s}_t, a_t), \text{ the new transition function on the new state space}$   $\mathbf{O} = \mathbf{S}$   $\mathbf{\delta} = p(o_t | \widetilde{s}_t)$ 2. policy:  $\pi_{\theta}(a|s, \mathbf{Z})$  $\overset{\text{gif: DeepMind. Emergent Tool Use from Multi-agent Auto}_{Curricula [2020]}$ 

task context

Meta RL in the lens of POMDPs :

1. POMDP:  $\widetilde{M} = \left\{ \widetilde{S}, \mathcal{A}, \widetilde{P}, r, \varepsilon, \mathbf{0} \right\}$  where

 $\widetilde{\mathbf{S}} = \mathbf{S} \times \mathbf{Z}, \text{ the concatenation of the state space and the task context} \\ \widetilde{\mathbf{P}} = p(\widetilde{s}_{t+1} | \widetilde{s}_t, a_t), \text{ the new transition function on the new state space} \\ \mathbf{O} = \mathbf{S} \\ \mathbf{\delta} = p(o_t | \widetilde{s}_t) \\ \mathbf{2}. \text{ policy} : \pi_{\theta}(a | s, \underbrace{\mathbf{Z}}_{task \text{ context}})$ 

- Remember, typically, to solve POMDPs:
  - State estimations: model the distribution of states given the observations (history), and apply usual RL procedures to find the optimal policy
  - **Use policies with memory**: implicitly infer the internal dynamics of the MDP based on previous experiences.

 $POMDP: \widetilde{M} = \left\{ \widetilde{S}, \mathcal{A}, \widetilde{P}, r, \varepsilon, 0 \right\}, policy: \pi_{\theta}(a|s, \underbrace{z}_{task \ context})$ The goal is to estimate the posterior probability of the task context variable given experiences  $p(\underbrace{z_{t}}_{task \ context} | \underbrace{s_{1:t}, a_{1:t}, r_{1:t}}_{experiences \ from \ tha \ task})$ 



Use locked objects to block the room

 $POMDP: \widetilde{M} = \left\{ \widetilde{S}, \mathcal{A}, \widetilde{P}, r, \varepsilon, \mathbf{0} \right\}, policy: \pi_{\theta} \left( a | s, \underbrace{z}_{task \ context} \right)$ The goal is to estimate the posterior probability of the task context variable given experiences  $p(\underbrace{z_{t}}_{task \ context} | \underbrace{s_{1:t}, a_{1:t}, r_{1:t}}_{experiences \ from \ tha \ task} \right)$ 

posterior sampling with latent context :

1. sample the latent variable with our current model  $z \sim \tilde{p}(z_t | s_{1:t}, a_{1:t}, r_{1:t})$ 

2. act according to  $\pi_{\theta}(a|s, z)$  to collect more data

- Comments on posterior sampling:
  Often uses variational inference to approximate the posterior
  - Enables exploration
  - Not optimal
  - Works well in practice

*Goal* : optimize both the policy  $\pi_{\theta}(a_t|s_t, z_t)$  and the posterior context variable  $q_{\lambda}(z_t|\tau_{1:t})$  *Optimization* :



• Comments:

- We can think of the return as the likelihood as in VI, which means we want to find the task context variable that makes high trajectory rewards more likely.
- This is actually an important design choice.

- How do we optimize the policy?
- How do we parameterize the variational family?

• Can we choose other "likelihood" function?

- How do we optimize the policy?
  - Using soft actor critic (SAC)
- How do we parameterize the variational family?
  - Mean-field assumption (permutation invariance of MDP encoding)
  - Accept variable length of history
- Can we choose other "likelihood" function?
  - Maximize the return (as mentioned before)
  - **Reconstruction of the MDP** (reward and dynamics modeling)
  - Model state, or state-action value functions
- PEARL = all above



Rakelly, Zhou et al. Efficient Off-Policy Meta-Reinforcement Learning via Probabilistic Context Variables [2019]

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#### Model-free meta-rl perspectives summary

Recipes for three model free perspectives :

1. memory based :  $f_{\theta}(\mathcal{M}_i) := RNN(\tau_{1:t})$  $:= TemporalConvAttentive(\tau_{1:t})$ 

2. bi level optimization :  $f_{\theta}(\mathcal{M}_i) := \theta + \alpha \nabla_{\theta} J_i(\theta)$ 

3. POMDP and posterior inference : task context aware policy  $\pi_{\theta}(a|s, z)$ posterior  $p(z_t|\tau_{1:t})$ 

- Relationships:
  - 3 is the stochastic version of 1 where the task context variable z is the adaptation parameter.
  - 2 is the same as 1 and 3 conceptually except that it chooses a specific form of the meta learner than a black-box function approximator.

#### Model-free meta-rl perspectives summary

Recipes for three model free perspectives :

1. memory based :  $f_{\theta}(\mathcal{M}_i) := RNN(\tau_{1:t})$  $:= TemporalConvAttentive(\tau_{1:t})$ 

2. bi level optimization :  $f_{\theta}(\mathcal{M}_i) := \theta + \alpha \nabla_{\theta} J_i(\theta)$ 

3. POMDP and posterior inference : task context aware policy  $\pi_{\theta}(a|s, z)$ posterior  $p(z_t|\tau_{1:t})$  **1. memory based :** *simple to understand and implement vulnerable to meta over fitting optimization challenges* 

2. bi level optimization : consistency poor sample efficiency

**3. POMDP and posterior inference :** *ef fective exploration special perspective same problems as memory based approaches* 

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#### How to design the meta training tasks?

- All the methods we talked about so far take as granted a distribution of tasks (MDPs).
- In lots of scenarios, the performance of the meta testing heavily depends on this distribution:
  - Are the tasks structurally related?
  - Is the testing task in-distribution or similar to tasks from the meta training distribution?
  - Are the tasks rich enough to provide powerful prior?
  - How to systematically design such tasks for different problem?
  - o ...
- Successful applications of these methods often are coupled with hand-crafted tasks.
- Can we **automate** task designing while maintaining the power of meta RL?

- Designing general task proposal algorithm can be infeasible.
- We restrict our attention to the setting where all tasks only differ in the reward function.
  - In this case, the dynamics of the environment serves as the supervision for our task proposal algorithm

Train



Yu, Quillen, He, Julian, Narayan et al. Meta-World: A Benchmark and Evaluation for Multi-Task and Meta Reinforcement Learning [2019]

- In essence, the **optimal unsupervised meta RL learner** for a **Controlled Markov process** (MDP without reward functions) is the procedure producing the **policy which achieves the minimal worst case regret.** (Appendix for rigorous definition)
  - Worst case over all possible reward distribution (task distribution).
  - Minimal regret on expectation over the worst-case reward function distribution.
- Use a latent variable to control the reward function.
- Therefore, the most important design decision is the mapping from the latent variable to the reward function.

• A practical implementation of the unsupervised reinforcement learning algorithm

Given a CMP

- 1. obtain the reward proposal procedure
- 2. sample latent task variable  $z \sim p(z)$
- 3. *define task reward*  $r_z$  *using the reward proposal procedure and* z
- 4. use standard meta learning algorithm with  $r_z$

- Reward proposal procedure can be defined in many ways
  - Randomly initialized
  - Or optimized with some objective
- Latent task variable can be simple distribution
- The proposal procedure takes in the value of the latent variable and produces a family of reward functions

DIAYN: a method for learning useful skills without a reward function

DIAYN does not depend on the rewards and only uses dyanmics as supervision.

Given  $D_{\theta}(z|s)$ , define reward function  $r_z(s, a) := log(D_{\theta}(z|s))$ 

Use DIAYN to optimize the mutual information by training a discriminator  $D_{\theta}(z|s)$  which predicts which latent variable was used to generate the rollout according to the policy  $\pi(a|s, z)$ .

Gupta, Eysenbach et al. Unsupervised Meta-Learning for Reinforcement Learning. [2019]

Eysenbach et al. Diversity is All You Need: Learning Skills without a Reward Function [2018]



# Summary

- What we've covered:
  - Model free meta reinforcement learning
    - Black-box adaptation
    - Optimization based methods
    - Inference on POMDP
  - Unsupervised Task designs (kinda of)
- What we haven't covered:
  - Model based meta reinforcement learning
  - Hybrid methods
  - Enhanced exploration
  - Optimization beyond gradient descent (evolution strategies)
  - Heterogeneous architectures to handle different state and action spaces

o ...

## References

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# Thank you!

• Questions are welcome

## Appendix: Unsupervised Meta Reinforcement Learning

Controlled Markov process (CMP)  $C = \{S, \mathcal{A}, \mathcal{P}\}$ 

*A learning procedure (meta learner)*  $f: \mathfrak{D}(\mathcal{M}_i) \to \pi$ 

Evaluation of the meta learner for a specific reward function  $R(f, r_z) = \sum_{i} \mathbb{E}_{\substack{\pi = f(\{\tau_1, \dots, \tau_{i-1}\})\\\tau \sim \pi}} \left[ \sum_{t} r_z(s_t, a_t) \right]$ 

Task distribution ≡ distribution over latent variable z ≡ distribution over reward functions

#### Appendix: Unsupervised Meta Reinforcement Learning

The optimal learning procedure under a specific reward function distribution  $f^* := \arg \max_f \mathbb{E}_{p(r_z)}[R(f, r_z)]$ 

Regret of a learning procedure under a specific reward function distribution  $REGRET(f, p(r_z)) := \mathbb{E}_{p(r_z)} \Big[ R(f^*, r_z) - R(f, r_z) \Big]$ 

Regret of a learning procedure for a CMP REGRET<sub>WC</sub>(f, C) := max<sub> $p(r_z)$ </sub>REGRET( $f, p(r_z)$ )

Optimal unsupervised learning procedure  $f_C^* := \arg \min_f REGRET_{WC}(f, C)$