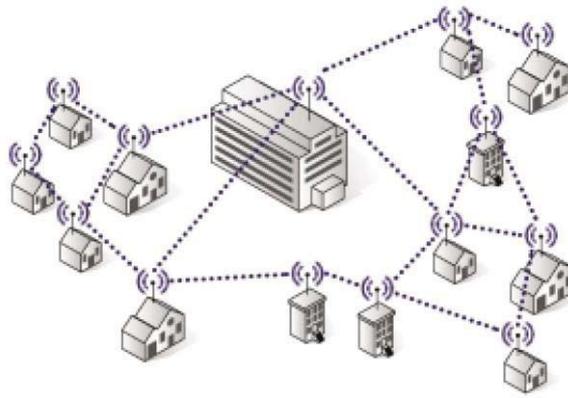


# Geo-Routing

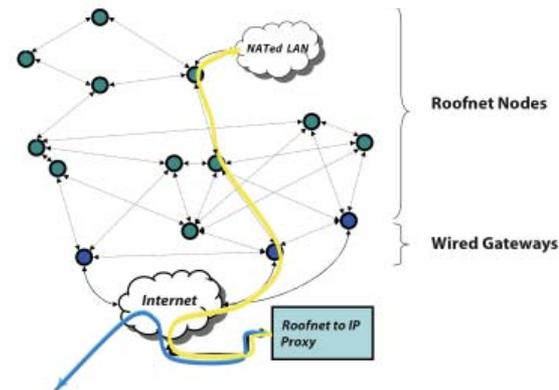
## Chapter 2



# Application of the Week: Mesh Networking (Roofnet)



- Sharing Internet access
- Cheaper for everybody
- Several gateways → fault-tolerance
- Possible data backup
- Community add-ons
  - I borrow your hammer, you copy my homework
  - Get to know your neighbors



# Rating

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- Area maturity

First steps

Text book

- Practical importance

No apps

Mission critical

- Theory appeal

Booooooring

Exciting



# Overview

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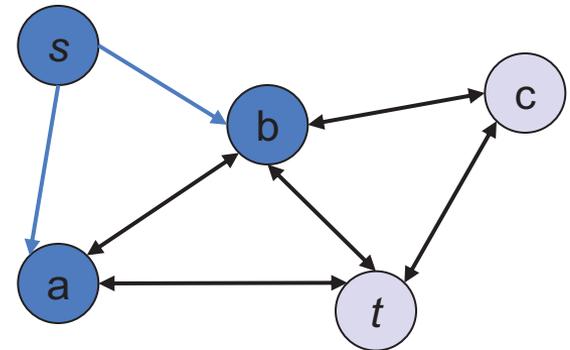
- Classic routing overview
- Geo-routing
- Greedy geo-routing
  
- Euclidean and Planar graphs
- Face Routing
- Greedy and Face Routing
- 3D Geo-Routing



# Classic Routing 1: Flooding

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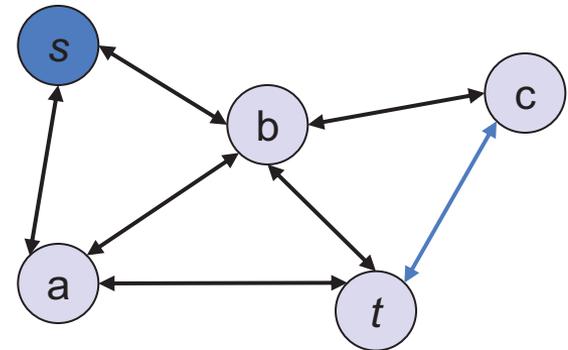
- What is Routing?
- „Routing is the act of moving information across a network from a source to a destination.“ (CISCO)
- The simplest form of routing is “flooding”: a source  $s$  sends the message to all its neighbors; when a node other than destination  $t$  receives the message the first time it re-sends it to all its neighbors.
- + simple (sequence numbers)
- a node might see the same message more than once. (How often?)
- what if the network is huge but the target  $t$  sits just next to the source  $s$ ?
- We need a smarter routing algorithm



# Classic Routing 2: Link-State Routing Protocols

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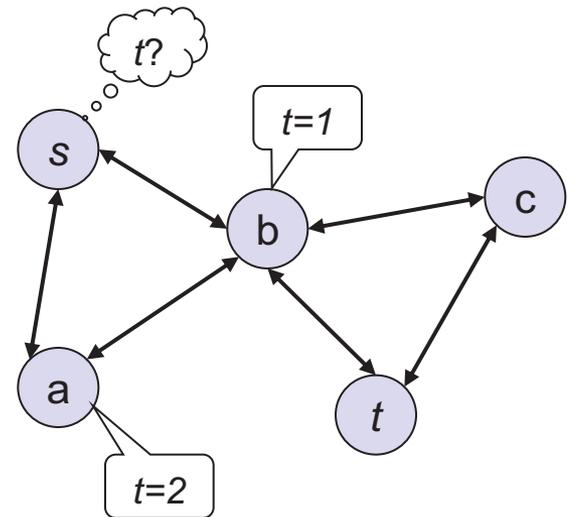
- Link-state routing protocols are a preferred iBGP method (within an autonomous system) in the Internet
- Idea: periodic notification of all nodes about the complete graph
- Routers then forward a message along (for example) the shortest path in the graph
- + message follows shortest path
- every node needs to store whole graph, even links that are not on any path
- every node needs to send and receive messages that describe the whole graph regularly



# Classic Routing 3: Distance Vector Routing Protocols

- The predominant method for wired networks
  - Idea: each node stores a routing table that has an entry to each destination (destination, distance, neighbor)
  - If a router notices a change in its neighborhood or receives an update message from a neighbor, it updates its routing table accordingly and sends an update to all its neighbors
- + message follows shortest path
- + only send updates when topology changes
- most topology changes are irrelevant for a given source/destination pair
  - every node needs to store a big table
  - count-to-infinity problem

Dest	Dir	Dst
<i>a</i>	<i>a</i>	1
<i>b</i>	<i>b</i>	1
<i>c</i>	<i>b</i>	2
<i>t</i>	<i>b</i>	2



# Discussion of Classic Routing Protocols

---

- **Proactive** Routing Protocols
  - Both link-state and distance vector are “proactive,” that is, routes are established and updated even if they are never needed.
  - If there is **almost no mobility**, proactive algorithms are superior because they never have to exchange information and find optimal routes easily.
- **Reactive** Routing Protocols
  - Flooding is “reactive,” but does not scale
  - If **mobility is high** and data transmission rare, reactive algorithms are superior; in the extreme case of almost no data and very much mobility the simple flooding protocol might be a good choice.

There is **no “optimal” routing protocol**; the choice of the routing protocol depends on the circumstances. Of particular importance is the mobility/data ratio.



# Routing in Ad-Hoc Networks

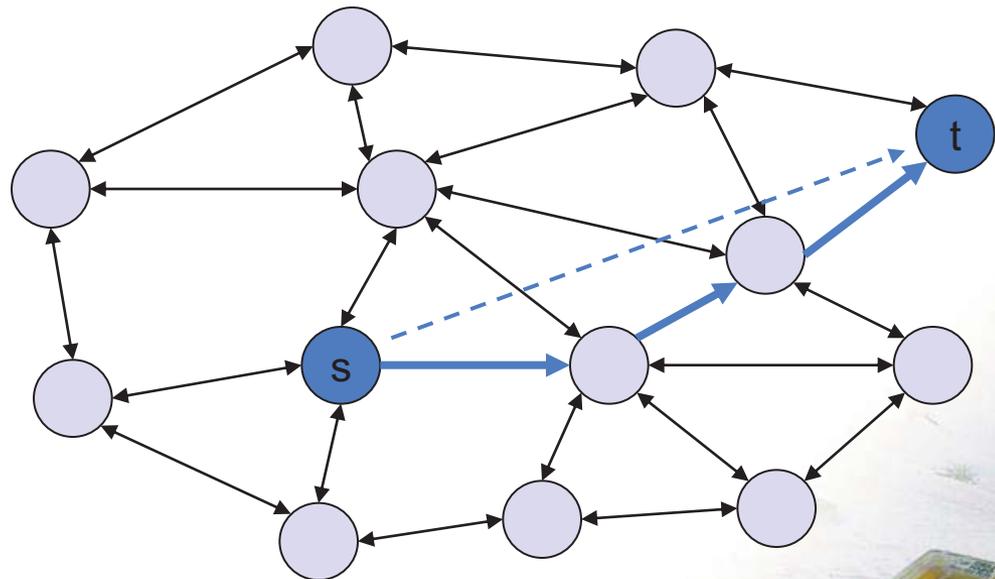
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- **Reliability**
  - Nodes in an ad-hoc network are not 100% reliable
  - Algorithms need to find alternate routes when nodes are failing
- **Mobile Ad-Hoc Network (MANET)**
  - It is often assumed that the nodes are mobile (“Car2Car”)
- 10 Tricks  $\rightarrow$   $2^{10}$  routing algorithms
- In reality there are almost that many proposals!
- Q: How good are these routing algorithms?!? **Any hard results?**
- A: Almost none! Method-of-choice is simulation...
- “If you simulate three times, you get three different results”



# Geometric (geographic, directional, position-based) routing

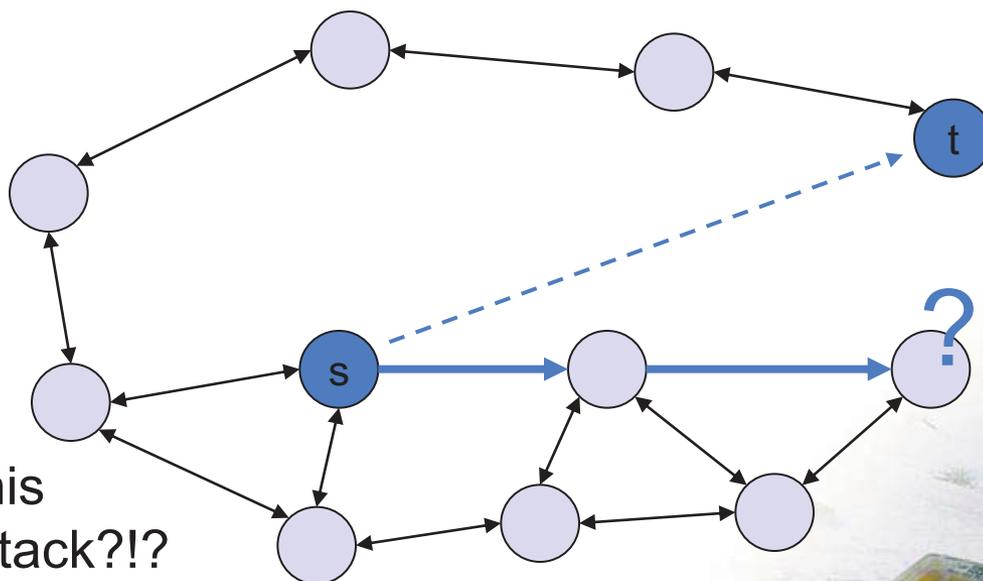
- ...even with all the tricks there will be flooding every now and then.
- In this chapter we will assume that the nodes are location aware (they have GPS, Galileo, or an ad-hoc way to figure out their coordinates), and that we know where the destination is.
- Then we simply route towards the destination



# Geometric routing

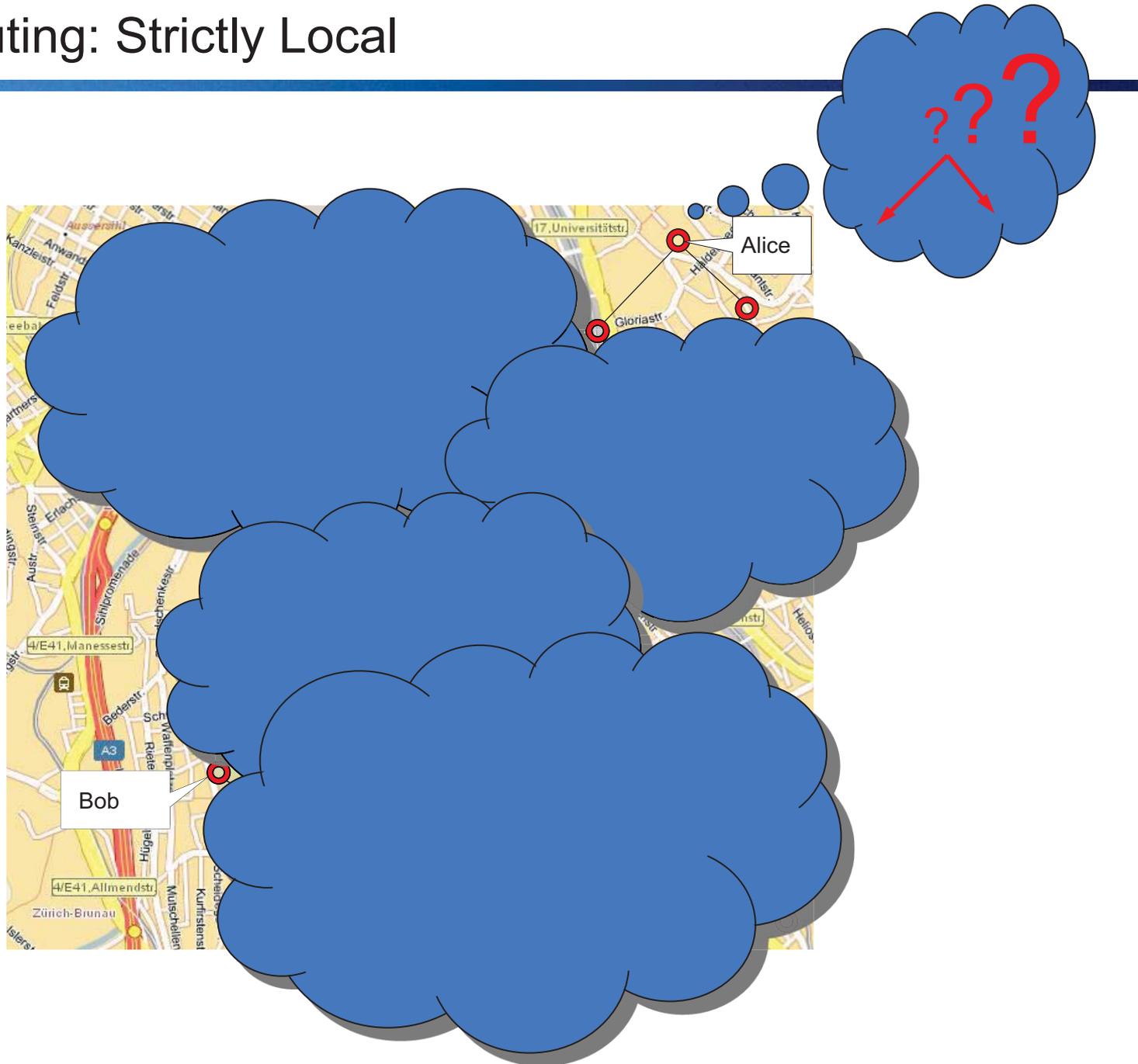
- Problem: What if there is no path in the right direction?
- We need a guaranteed way to reach a destination even in the case when there is no directional path...

- Hack: as in flooding nodes keep track of the messages they have already seen, and then they backtrack\* from there



\*backtracking? Does this mean that we need a stack?!?

# Geo-Routing: Strictly Local





# Greedy Geo-Routing?



# What is Geographic Routing?

---

- A.k.a. geometric, location-based, position-based, etc.

- Each node knows its own position and position of neighbors
- Source knows the position of the destination
- **No routing tables stored in nodes!**

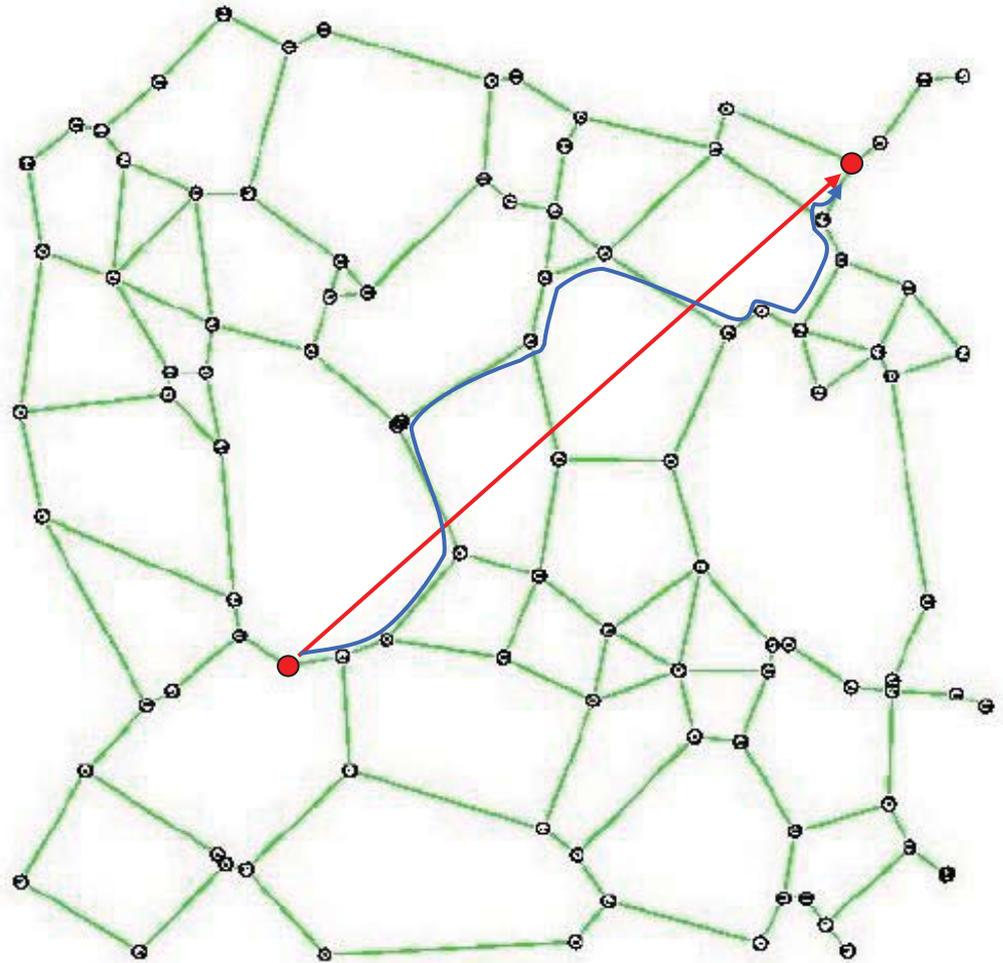
- Geographic routing makes sense
  - Own position: GPS/Galileo, local positioning algorithms
  - Destination: Geocasting, location services, source routing++
  - **Learn about ad-hoc routing in general**



# Greedy routing

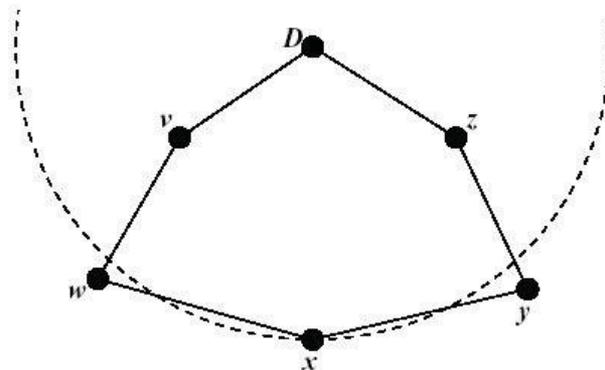
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- Greedy routing looks promising.
- Maybe there is a way to choose the next neighbor and a particular graph where we always reach the destination?

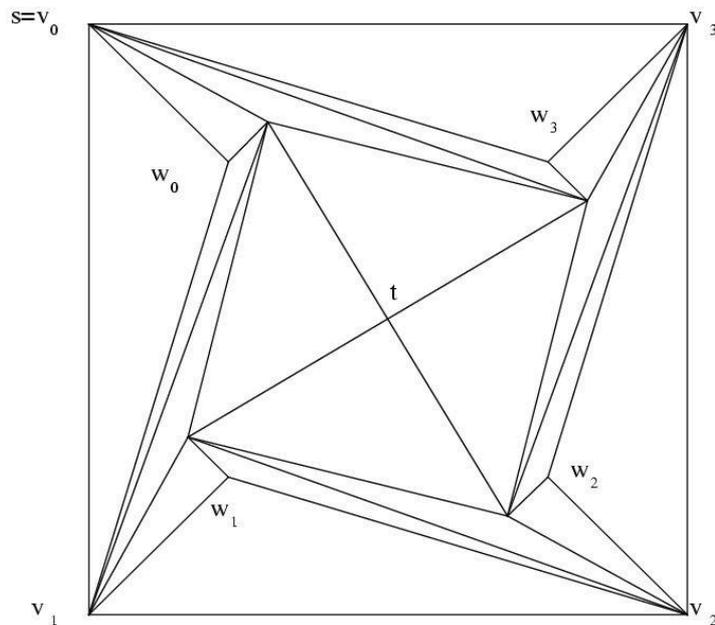


# Examples why greedy algorithms fail

- We greedily route to the neighbor which is closest to the destination:  
But both neighbors of  $x$  are not closer to destination  $D$



- Also the best angle approach might fail, even in a triangulation:  
if, in the example on the right, you always follow the edge with the narrowest angle to destination  $t$ , you will forward on a loop  $V_0, W_0, V_1, W_1, \dots, V_3, W_3, V_0, \dots$

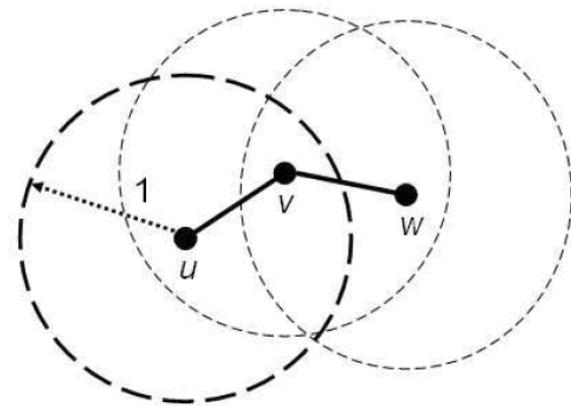


# Euclidean and Planar Graphs

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- Euclidean: Points in the plane, with coordinates, e.g. UDG
- UDG: Classic computational geometry model, special case of disk graphs

- All nodes are points in the plane, two nodes are connected iff (if and only if) their distance is at most 1, that is  $\{u,v\} \in E \Leftrightarrow |u,v| \leq 1$

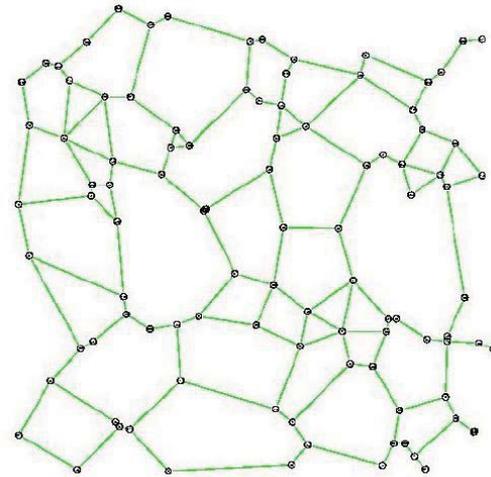
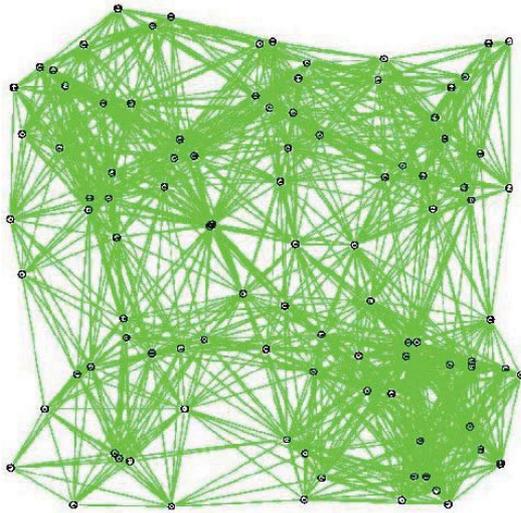


- + Very simple, allows for strong analysis
- Not realistic: “If you gave me \$100 for each paper written with the unit disk assumption, I still could not buy a radio that is unit disk!”
- Particularly bad in obstructed environments (walls, hills, etc.)
- Natural extension: 3D UDG

# Euclidean and Planar Graphs

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- Planar: can be drawn without “edge crossings” in a plane

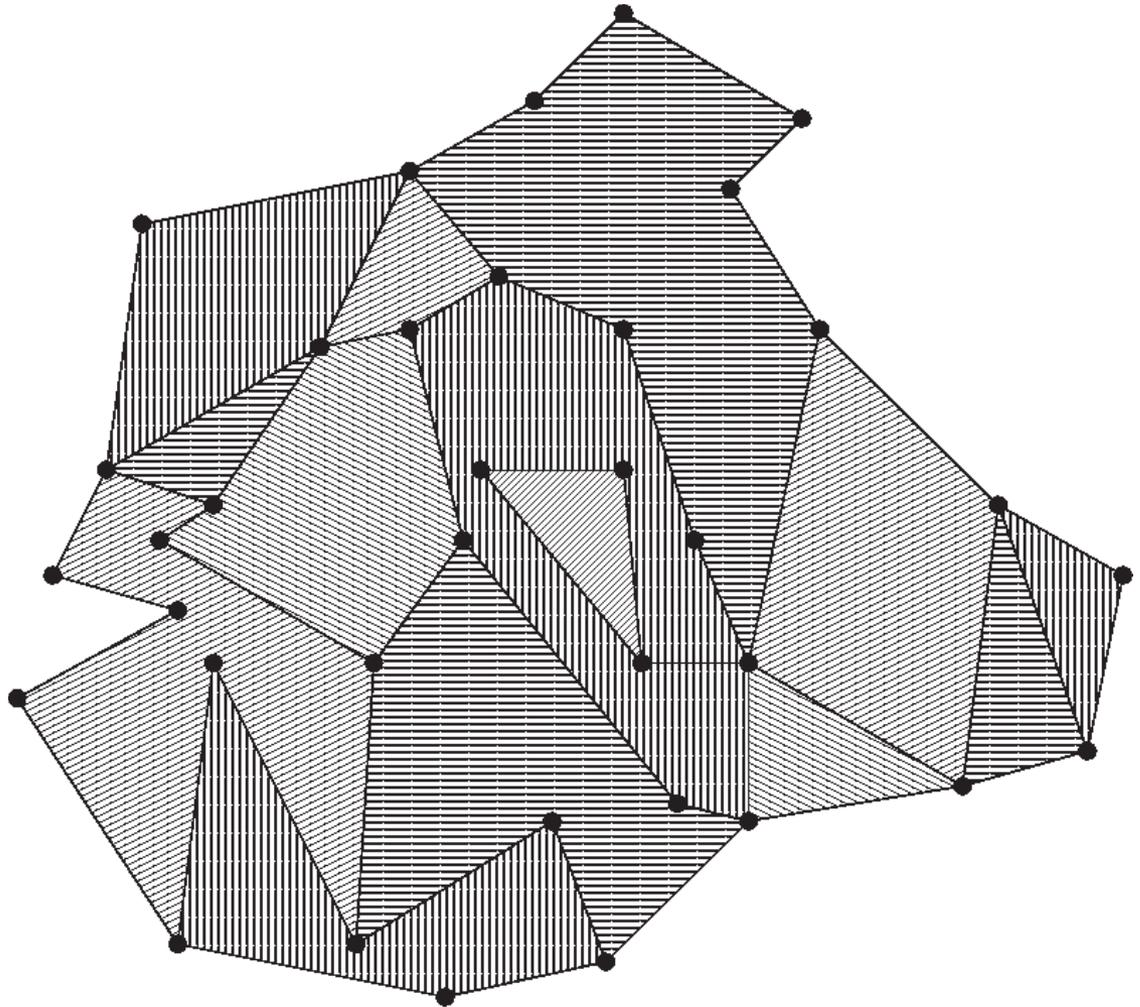


- A planar graph already drawn in the plane without edge intersections is called a **plane graph**. In the next chapter we will see how to make a Euclidean graph planar.

# Breakthrough idea: route on faces

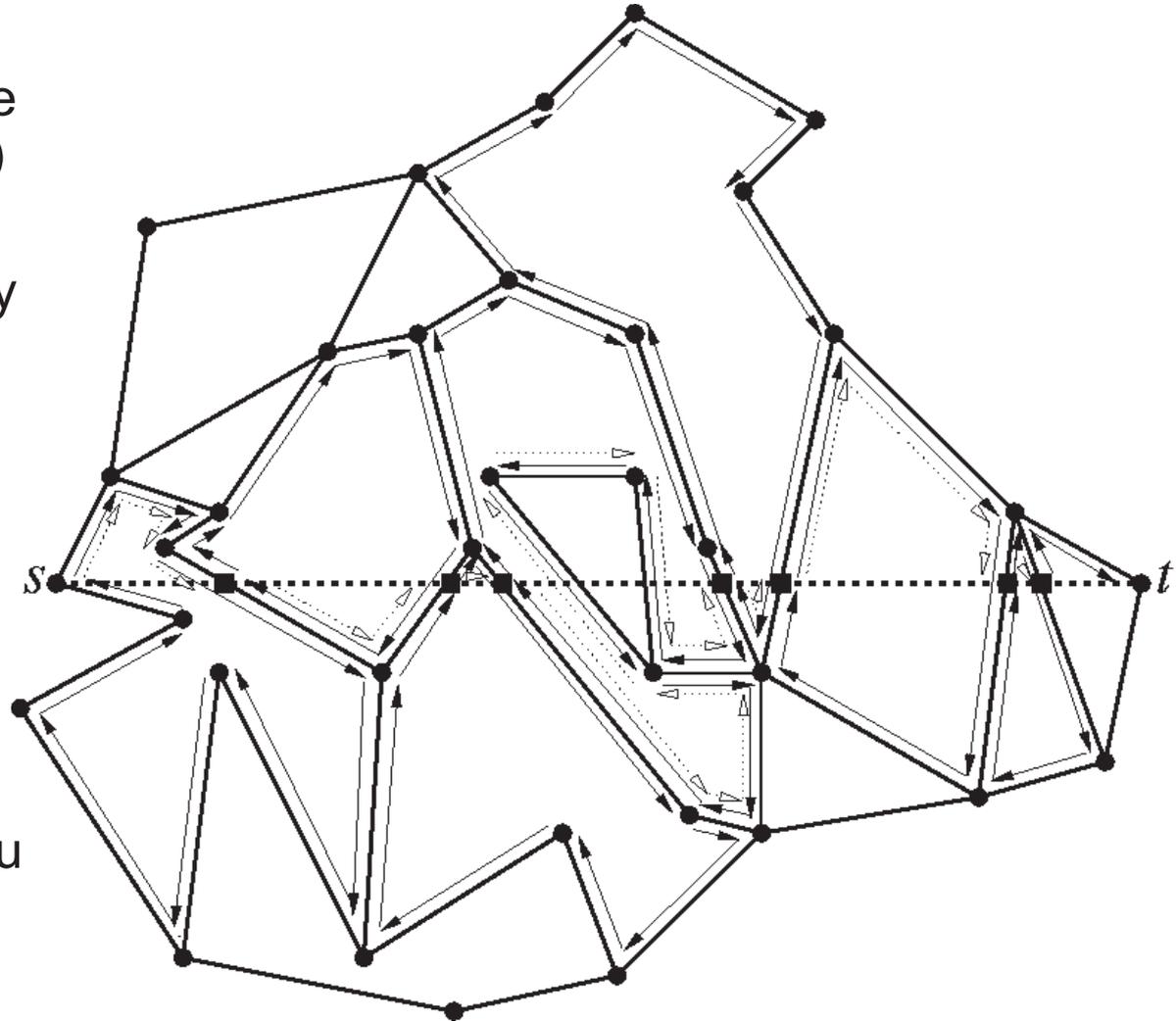
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- Remember the faces...
- Idea:  
Route along the boundaries of the faces that lie on the source–destination line



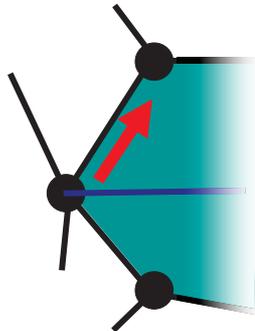
# Face Routing

0. Let  $f$  be the face incident to the source  $s$ , intersected by  $(s,t)$
1. Explore the boundary of  $f$ ; remember the point  $p$  where the boundary intersects with  $(s,t)$  which is nearest to  $t$ ; after traversing the whole boundary, go back to  $p$ , switch the face, and repeat 1 until you hit destination  $t$ .

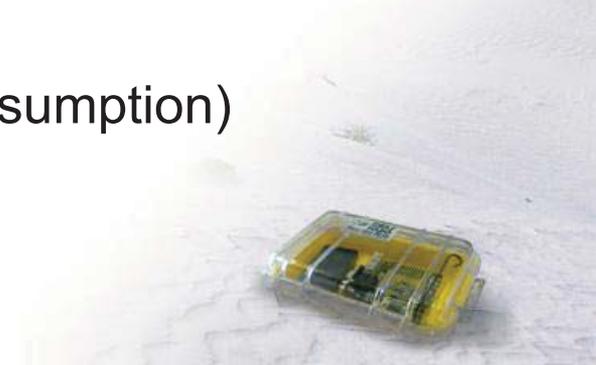


# Face Routing Properties

- All necessary information is stored in the message
  - Source and destination positions
  - Point of transition to next face
- Completely local:
  - Knowledge about direct neighbors' positions sufficient
  - Faces are **implicit**



- **Planarity** of graph is **computed** locally (not an assumption)
  - Computation for instance with Gabriel Graph



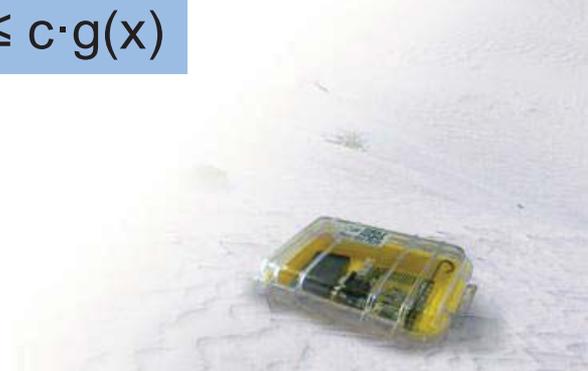


# Face routing is correct

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- Theorem: Face routing terminates on any simple planar graph in  $O(n)$  steps, where  $n$  is the number of nodes in the network
- Proof: A simple planar graph has at most  $3n-6$  edges. You leave each face at the point that is closest to the destination, that is, you never visit a face twice, because you can order the faces that intersect the source—destination line on the exit point. Each edge is in at most 2 faces. Therefore each edge is visited at most 4 times. The algorithm terminates in  $O(n)$  steps.

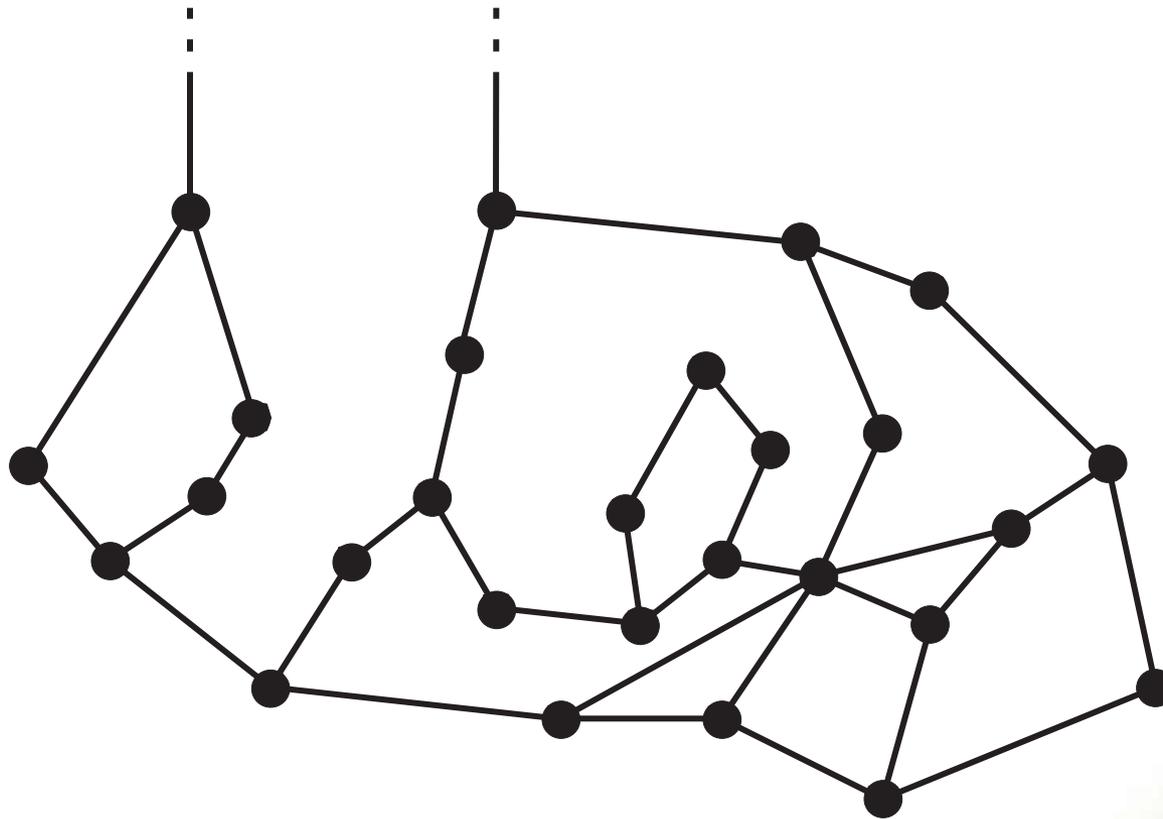
Definition:  $f \in O(g) \rightarrow \exists c > 0, \forall x > x_0: f(x) \leq c \cdot g(x)$



# Face Routing

---

- Theorem: Face Routing reaches destination in  $O(n)$  steps
- But: Can be very bad compared to the optimal route



# Is there something better than Face Routing?

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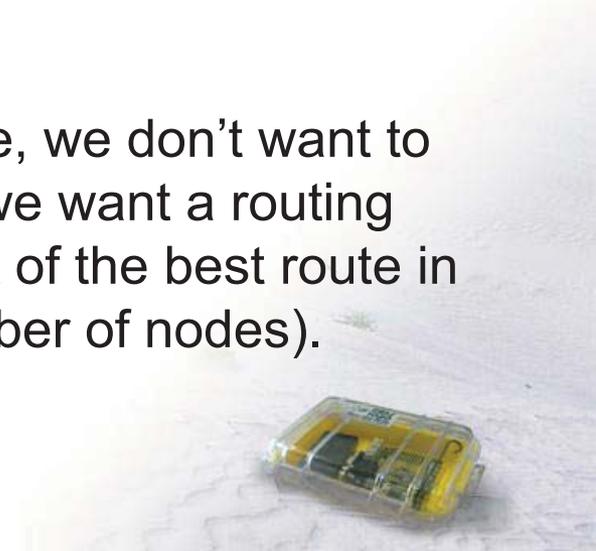
How can we improve Face Routing?



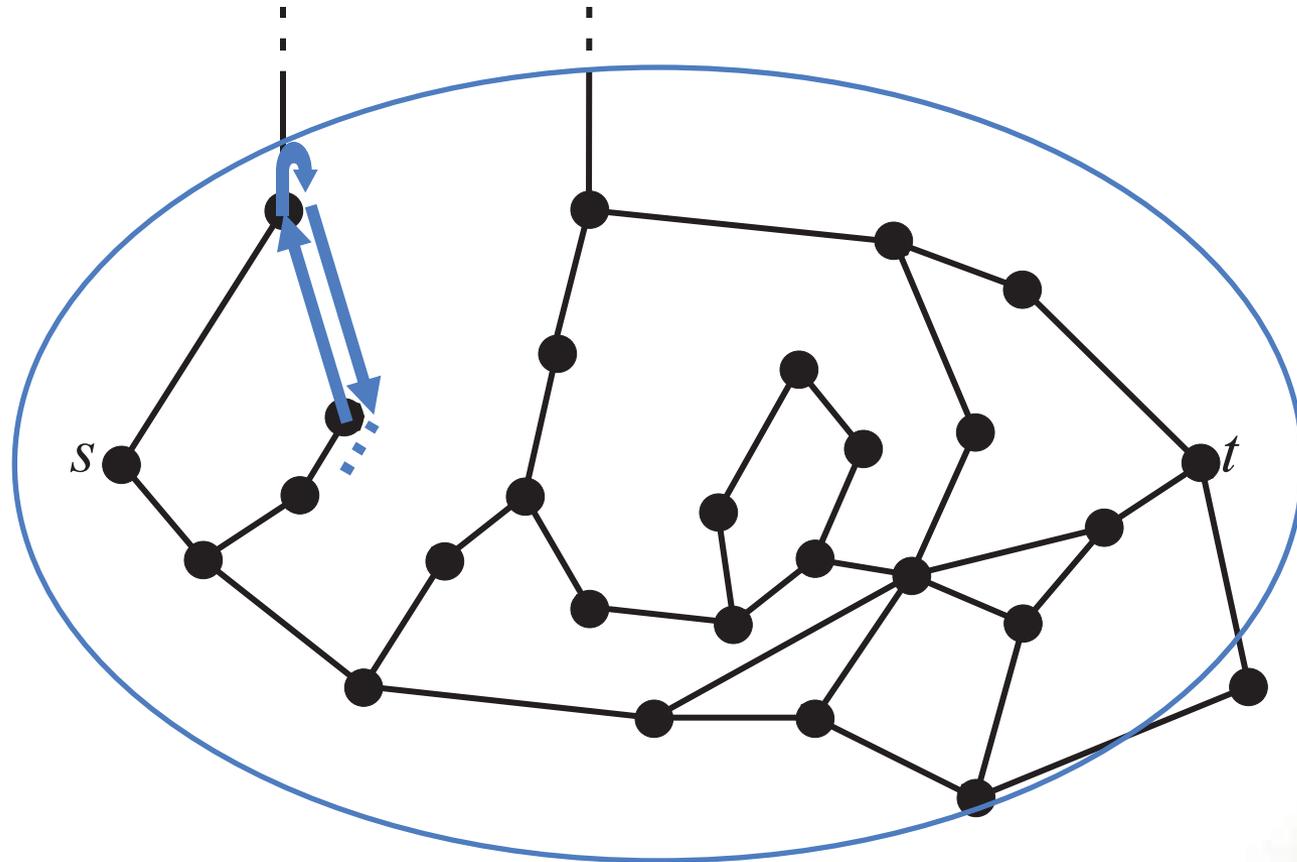
# Is there something better than Face Routing?

---

- How to improve face routing? A proposal called “Face Routing 2”
- Idea: Don’t search a whole face for the best exit point, but take the **first** (better) exit point you find. Then you don’t have to traverse huge faces that point away from the destination.
- Efficiency: Seems to be practically more efficient than face routing. But the theoretical worst case is worse –  $O(n^2)$ .
- Problem: if source and destination are very close, we don’t want to route through all nodes of the network. Instead we want a routing algorithm where the cost is a function of the cost of the best route in the unit disk graph (and independent of the number of nodes).

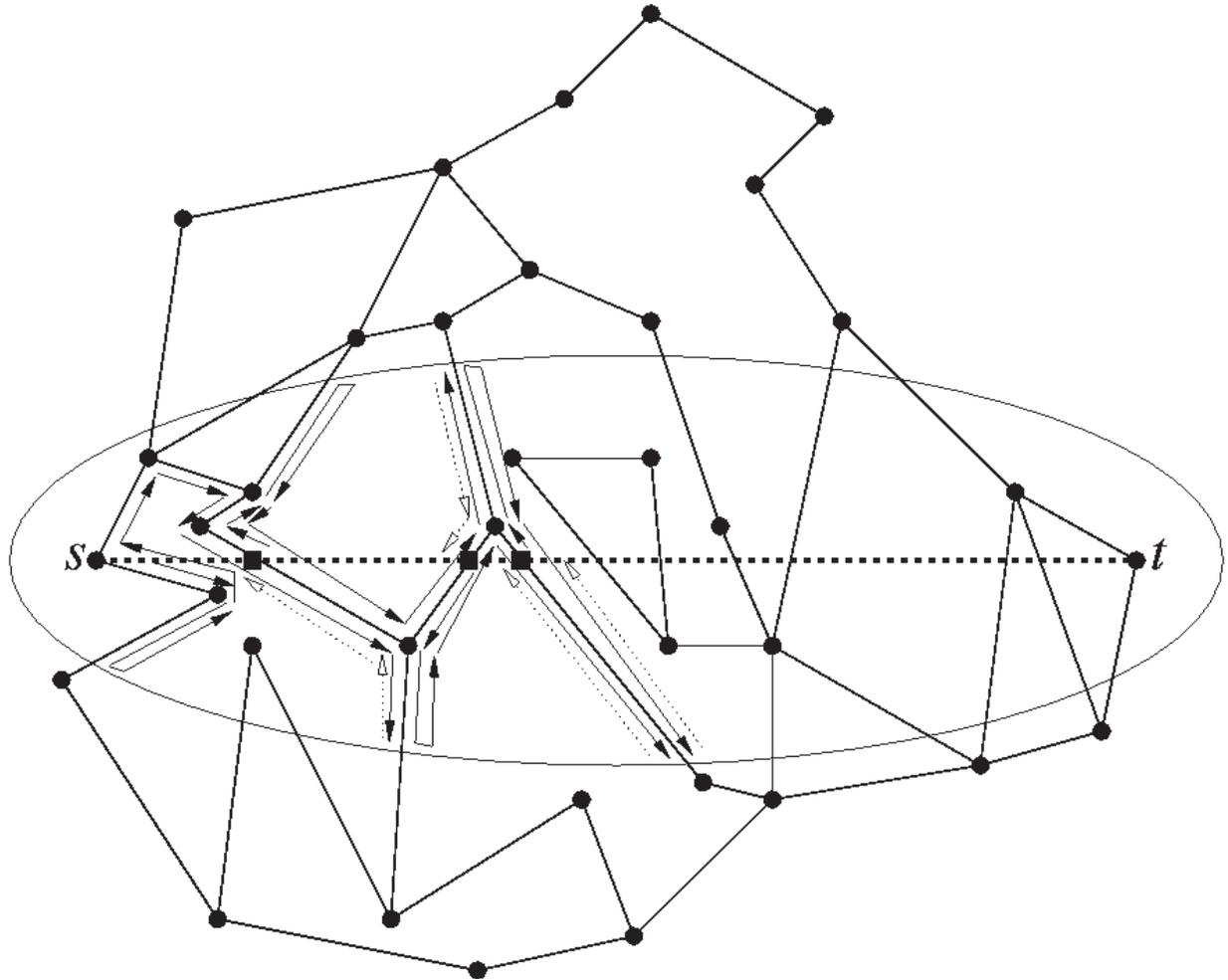


# Bounding Searchable Area



# Adaptive Face Routing (AFR)

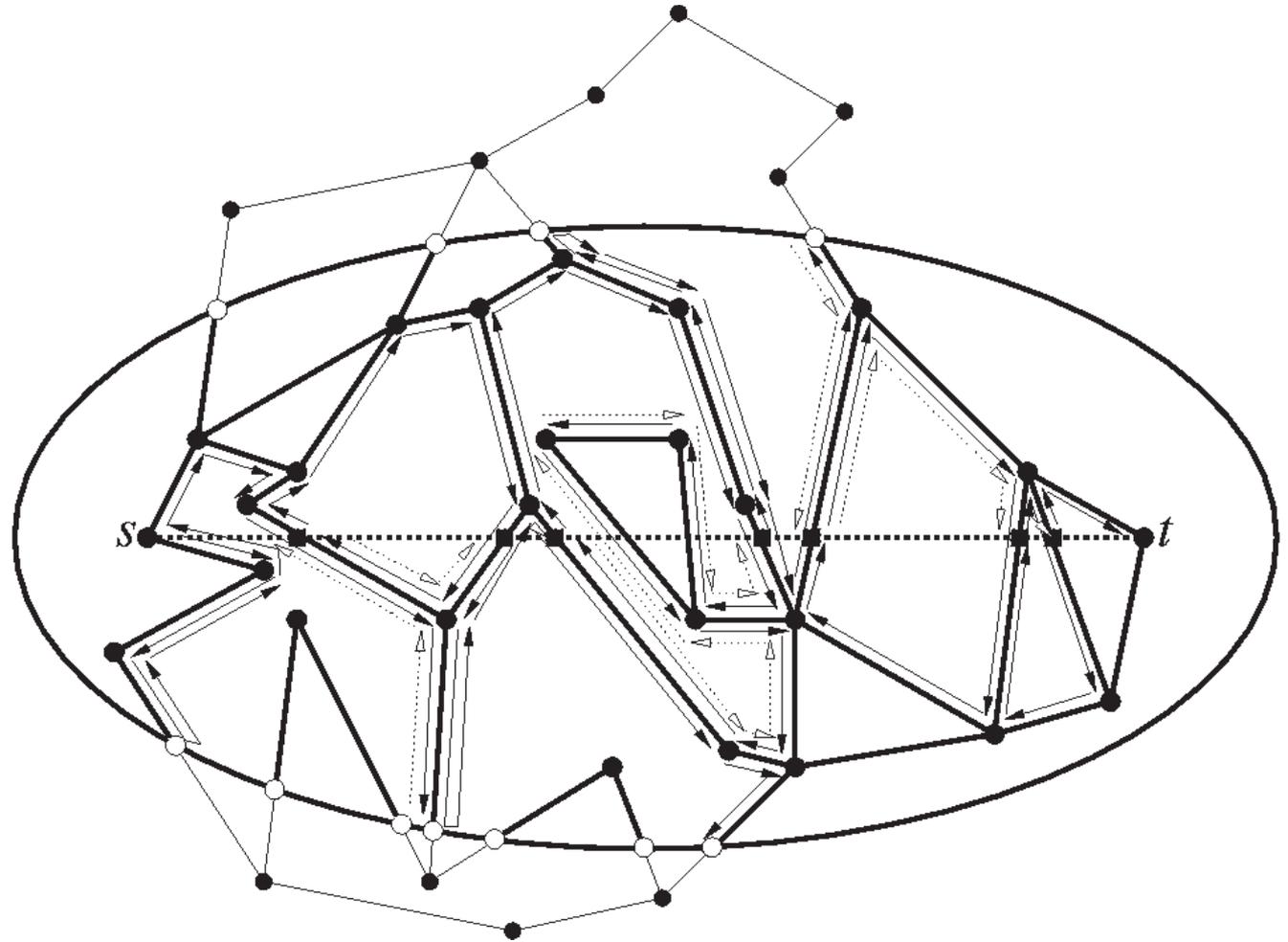
- Idea: Use face routing together with “growing radius” trick:
- That is, don't route beyond some radius  $r$  by branching the planar graph within an ellipse of exponentially growing size.



# AFR Example Continued

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- We grow the ellipse and find a path



# AFR Pseudo-Code

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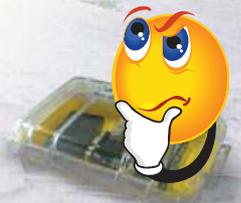
0. Calculate  $G = GG(V) \cap UDG(V)$   
Set  $c$  to be twice the Euclidean source—destination distance.
  1. Nodes  $w \in W$  are nodes where the path  $s-w-t$  is larger than  $c$ . Do face routing on the graph  $G$ , but without visiting nodes in  $W$ . (This is like pruning the graph  $G$  with an ellipse.) You either reach the destination, or you are stuck at a face (that is, you do not find a better exit point.)
  2. If step 1 did not succeed, **double**  $c$  and go back to step 1.
- Note: All the steps can be done completely locally, and the nodes need no local storage.



# The $\Omega(1)$ Model

---

- We simplify the model by assuming that nodes are sufficiently far apart; that is, there is a **constant**  $d_0$  such that all pairs of nodes have at least distance  $d_0$ . We call this the  $\Omega(1)$  model.
- This simplification is natural because nodes with transmission range 1 (the unit disk graph) will usually not “sit right on top of each other”.
- Lemma: In the  $\Omega(1)$  model, all natural cost models (such as the Euclidean distance, the energy metric, the link distance, or hybrids of these) are equal up to a constant factor.
- Remark: The properties we use from the  $\Omega(1)$  model can also be established with a backbone graph construction.



# Analysis of AFR in the $\Omega(1)$ model

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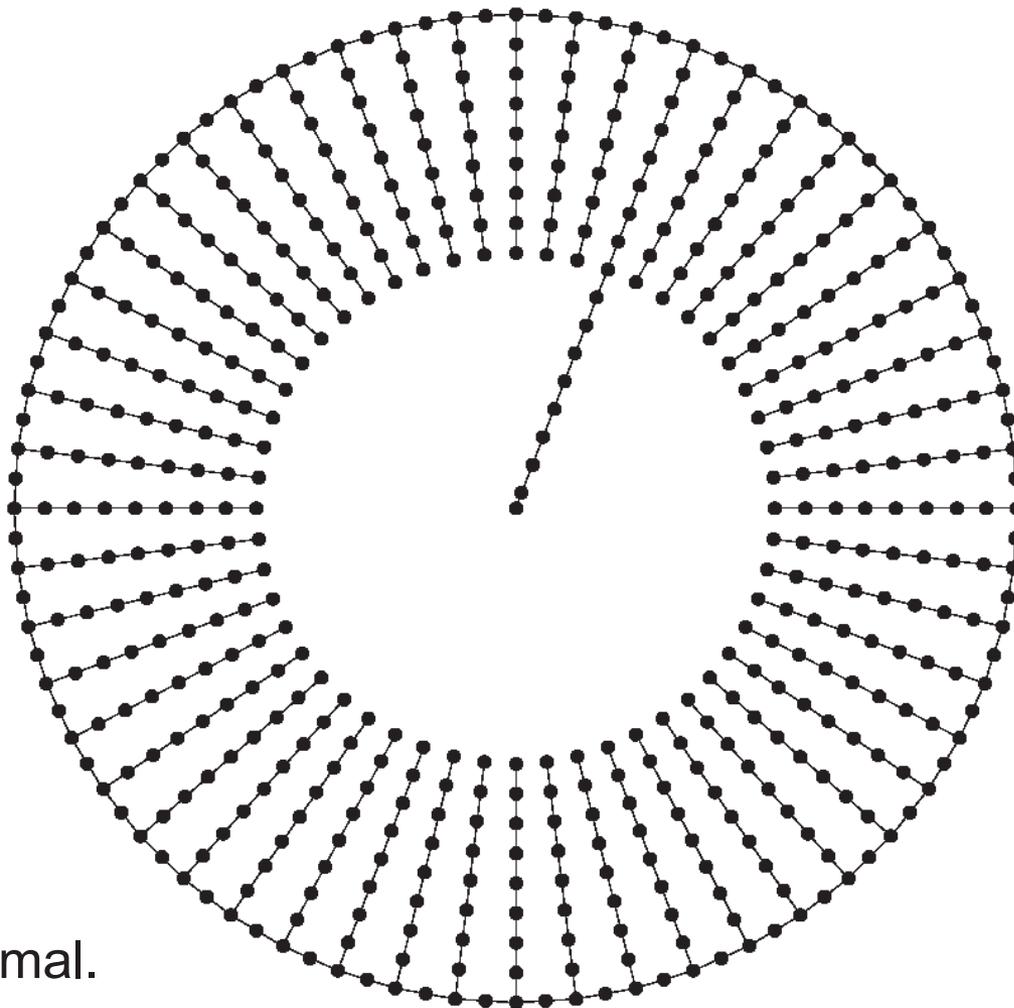
- Lemma 1: In an ellipse of size  $c$  there are at most  $O(c^2)$  nodes.
- Lemma 2: In an ellipse of size  $c$ , face routing terminates in  $O(c^2)$  steps, either by finding the destination, or by not finding a new face.
- Lemma 3: Let the optimal source—destination route in the UDG have cost  $c^*$ . Then this route  $c^*$  must be in any ellipse of size  $c^*$  or larger.
- Theorem: **AFR terminates with cost  $O(c^{*2})$ .**
- Proof: Summing up all the costs until we have the right ellipse size is bounded by the size of the cost of the right ellipse size.



# Lower Bound

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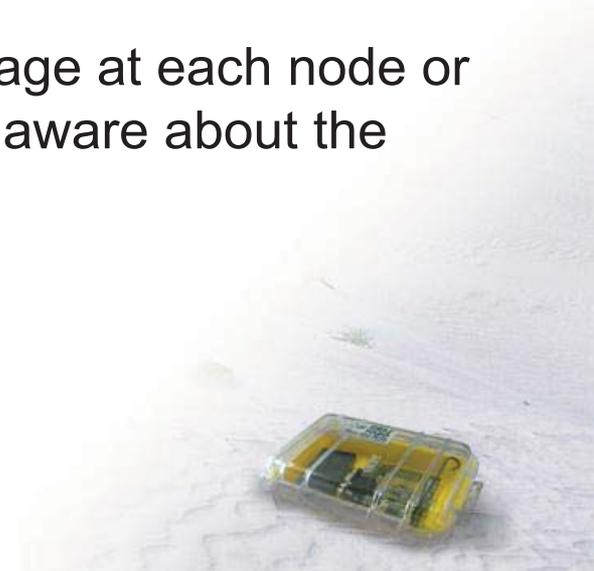
- The network on the right constructs a lower bound.
- The destination is the center of the circle, the source any node on the ring.
- Finding the right chain costs  $\Omega(c^*2)$ , even for randomized algorithms
- Theorem:  
AFR is asymptotically optimal.



# Non-geometric routing algorithms

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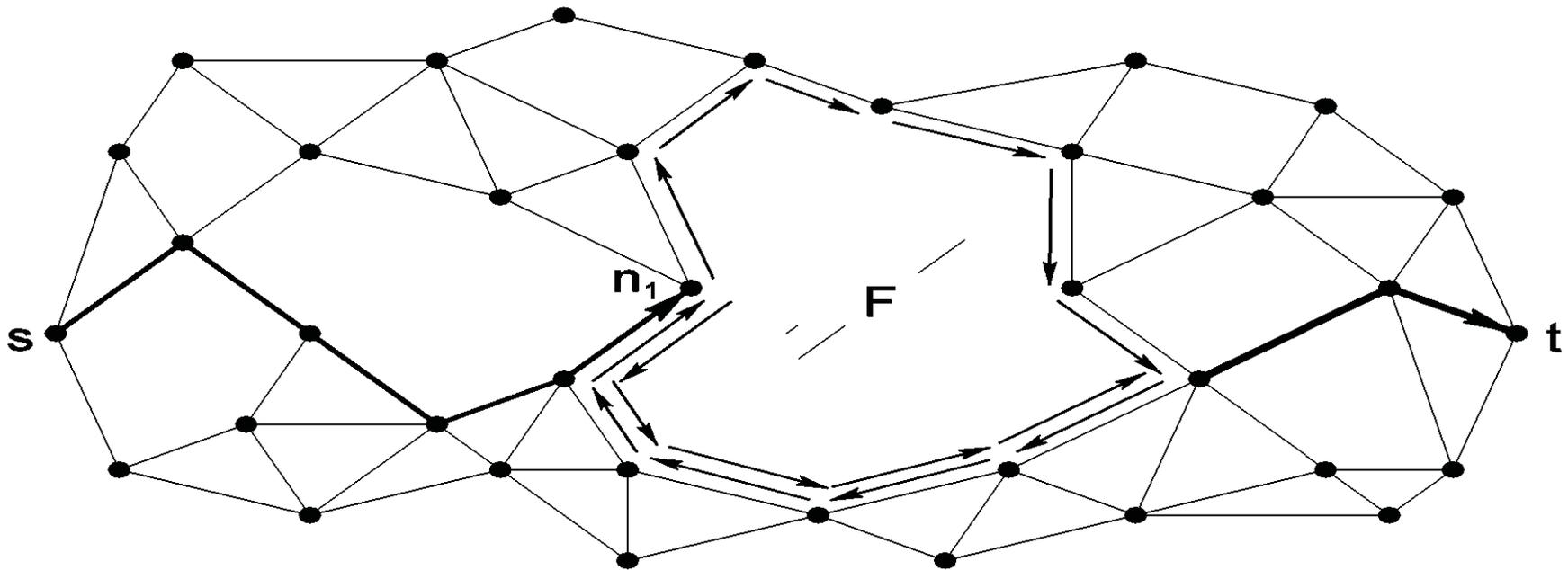
- In the  $\Omega(1)$  model, a standard flooding algorithm enhanced with growing search area idea will (for the same reasons) also cost  $O(c^2)$ .
- However, such a flooding algorithm needs  $O(1)$  **extra storage** at each node (a node needs to know whether it has already forwarded a message).
- Therefore, there is a trade-off between  $O(1)$  storage at each node or that nodes are location aware, and also location aware about the destination. This is intriguing.



# GOAFR – Greedy Other Adaptive Face Routing

- Back to geometric routing...
- AFR Algorithm is not very efficient (especially in dense graphs)
- Combine **G**reedy and (**O**ther **A**daptive) **F**ace **R**outing
  - Route greedily as long as possible
  - Circumvent “dead ends” by use of face routing
  - Then route greedily again

Other AFR: In each face proceed to point closest to destination

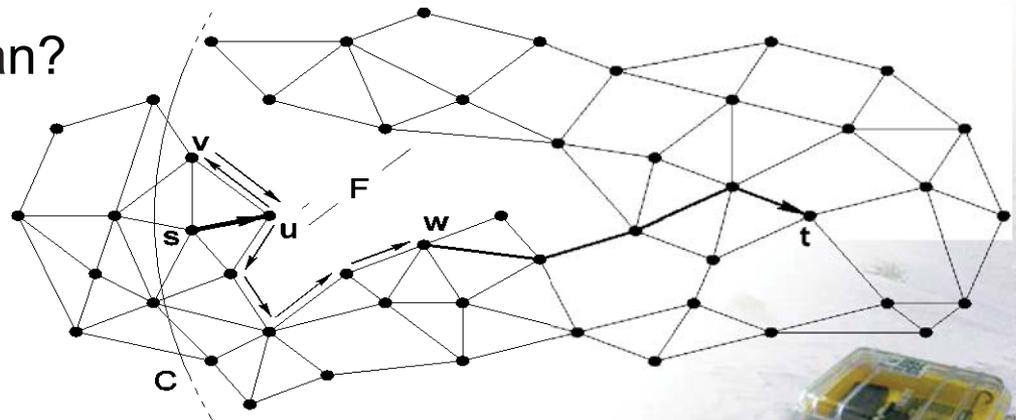


# GOAFR+ – Greedy Other Adaptive Face Routing

- Early fallback to greedy routing:
  - Use counters  $p$  and  $q$ . Let  $u$  be the node where the exploration of the current face  $F$  started
    - $p$  counts the nodes closer to  $t$  than  $u$
    - $q$  counts the nodes *not* closer to  $t$  than  $u$
  - Fall back to greedy routing as soon as  $p > \sigma \cdot q$  (constant  $\sigma > 0$ )

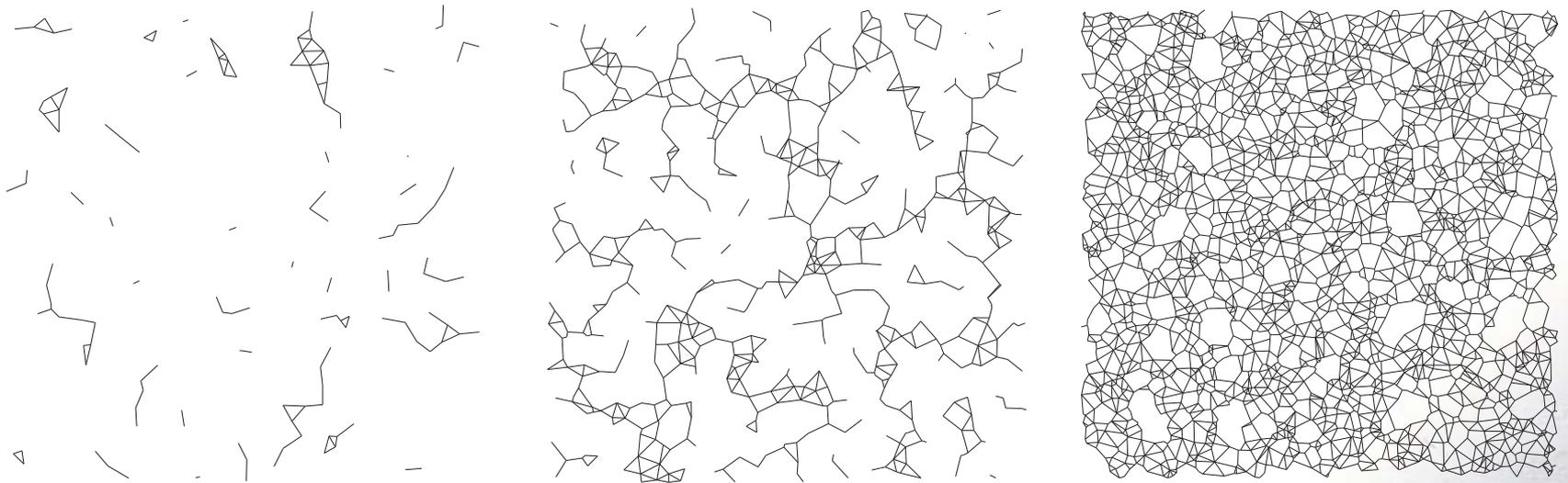
Theorem: GOAFR is still asymptotically worst-case optimal...  
...and it is efficient in practice, in the average-case.

- What does “practice” mean?
  - Usually nodes placed uniformly at random



# Average Case

- Not interesting when graph not dense enough
- Not interesting when graph is too dense
- **Critical density range** (“percolation”)
  - Shortest path is significantly longer than Euclidean distance



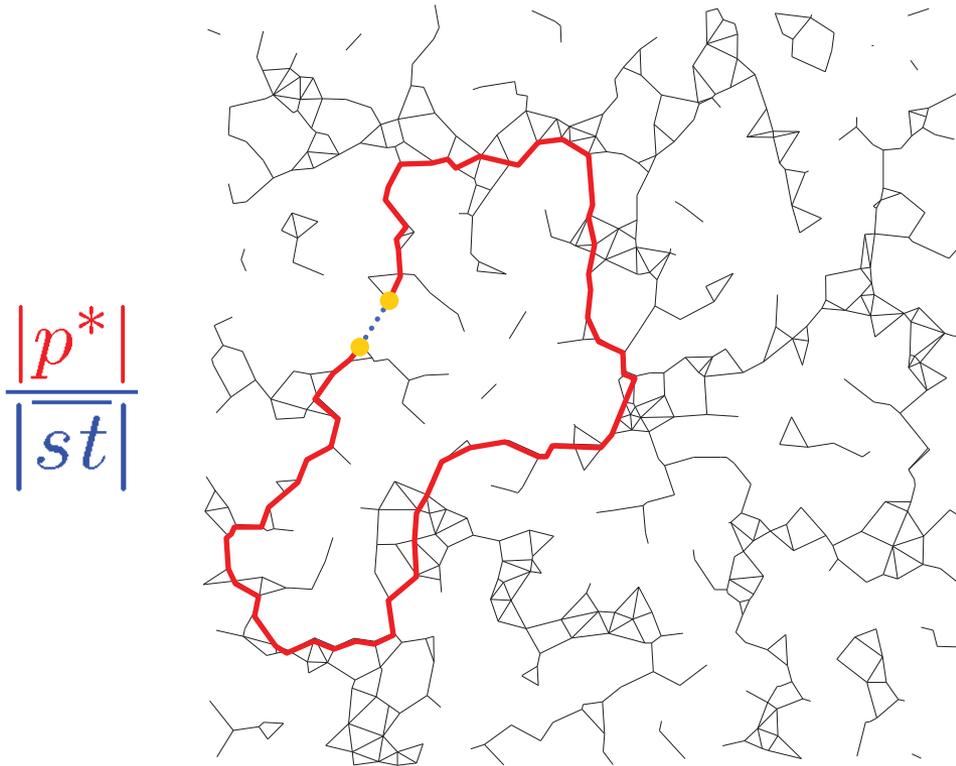
← too sparse

critical density

→ too dense

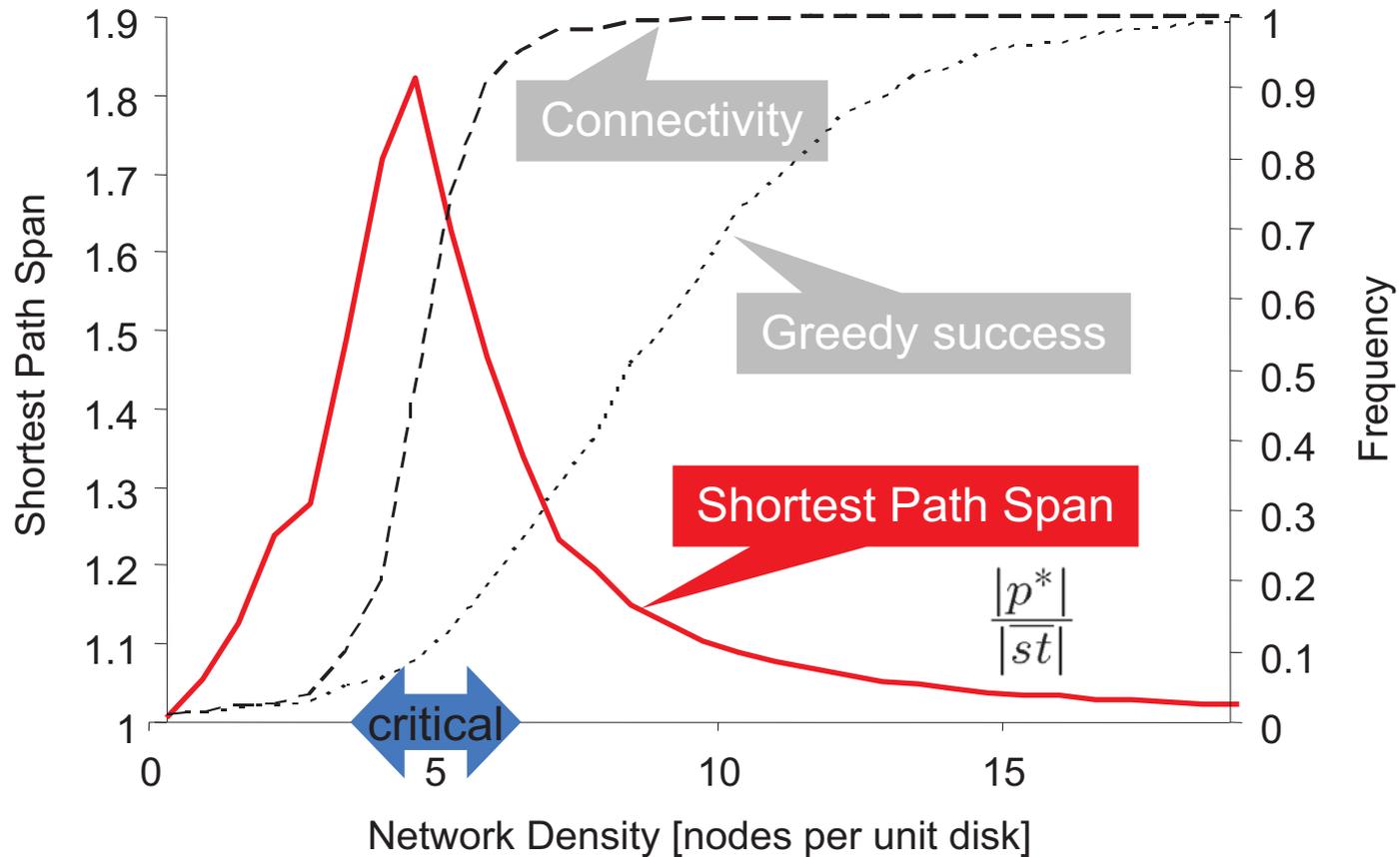
# Critical Density: Shortest Path vs. Euclidean Distance

- Shortest path is significantly longer than Euclidean distance

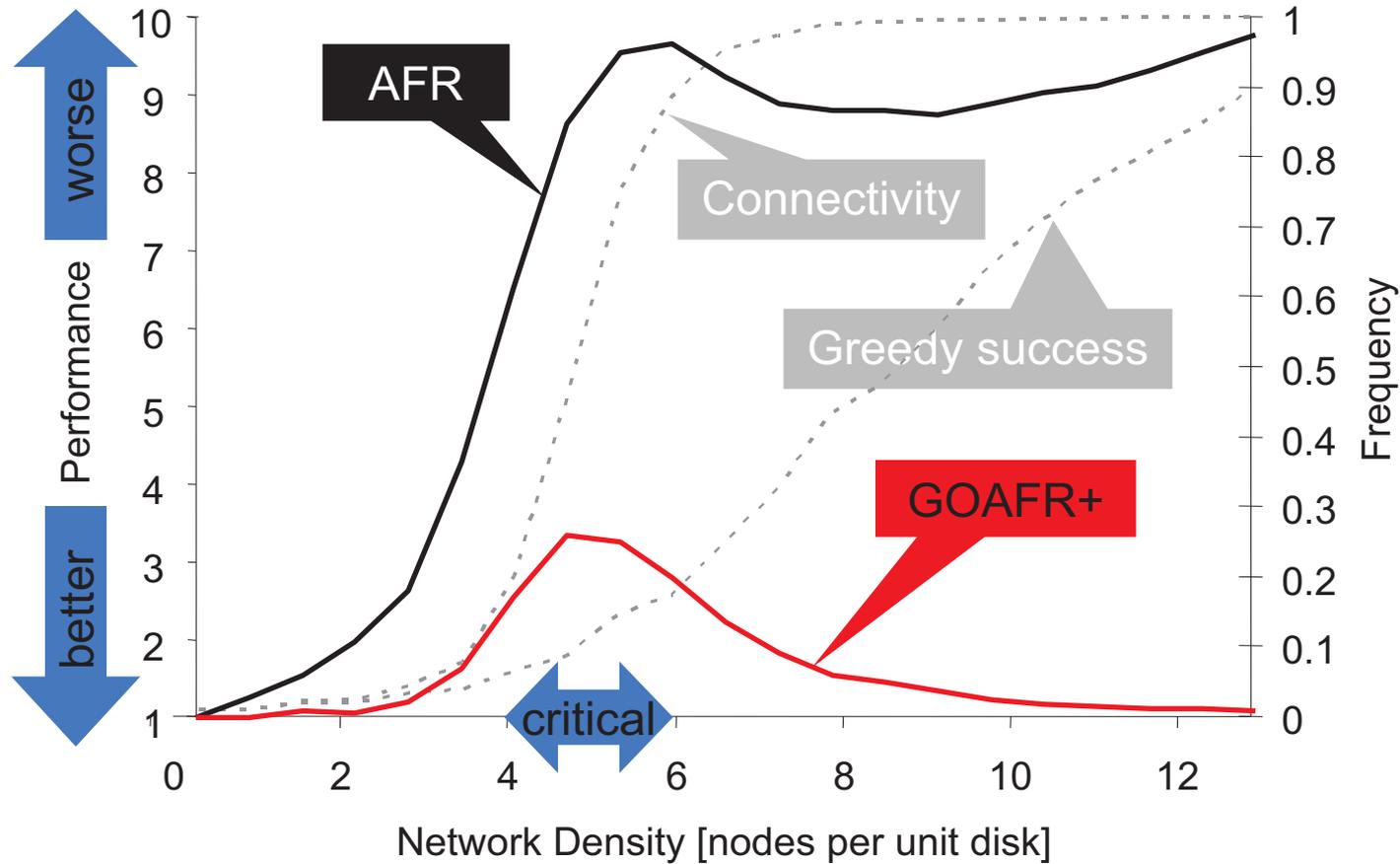


- Critical density range mandatory for the simulation of **any** routing algorithm (not only geographic)

# Randomly Generated Graphs: Critical Density Range



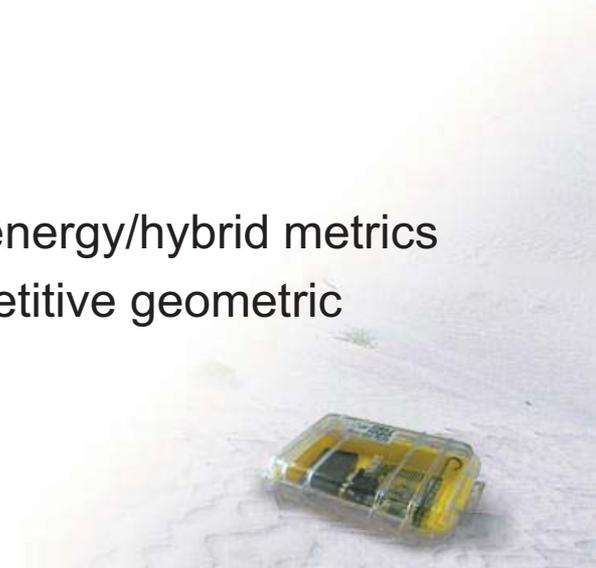
# Simulation on Randomly Generated Graphs



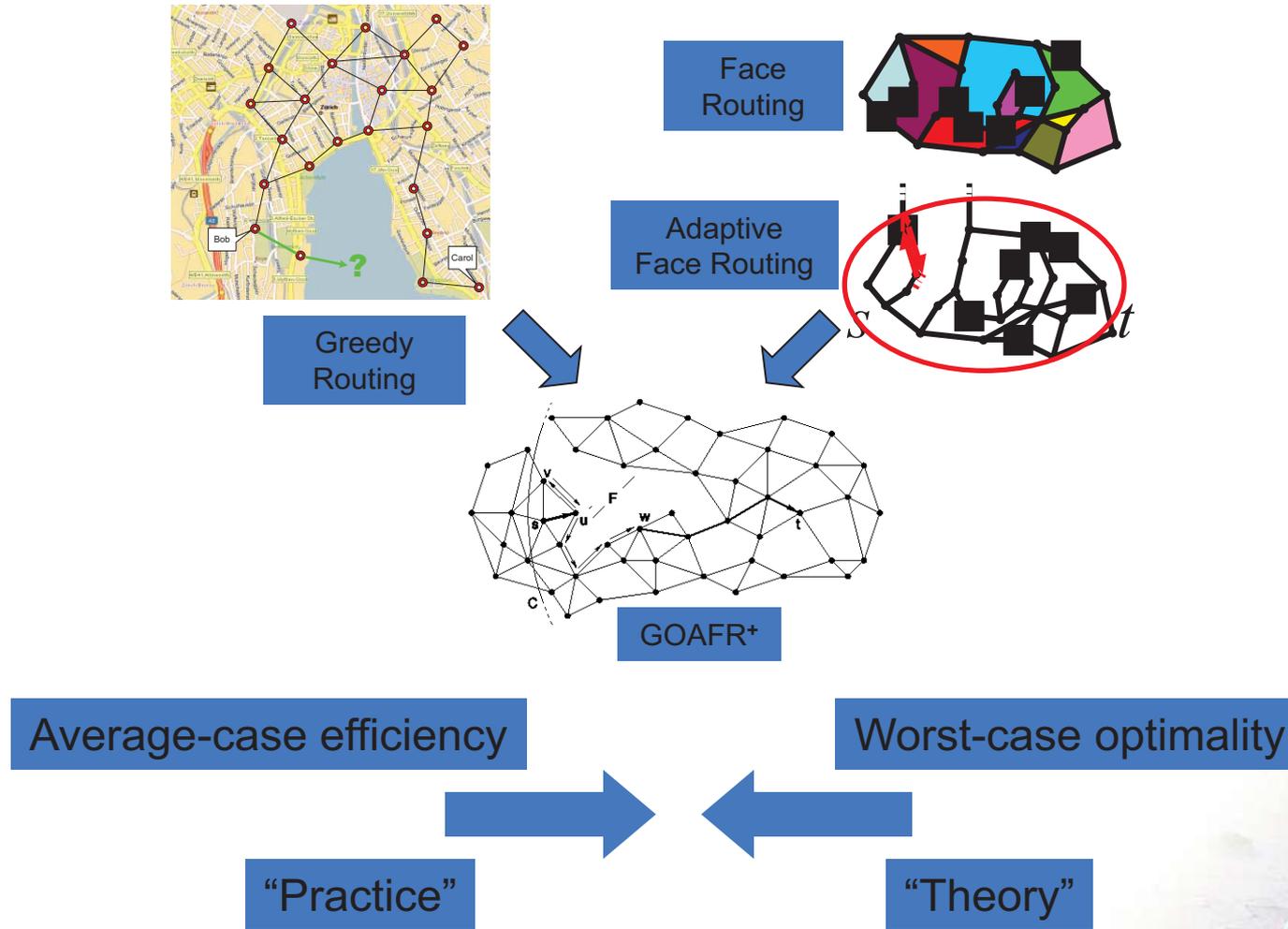
# A Word on Performance

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- What does a performance of 3.3 in the critical density range mean?
- If an **optimal path** (found by Dijkstra) has **cost  $c$** , then **GOAFR+** finds the destination **in  $3.3 \cdot c$  steps**.
- It does *not* mean that the *path* found is 3.3 times as long as the optimal path! The path found can be much smaller...
- Remarks about cost metrics
  - In this lecture “cost”  $c = c$  hops
  - There are other results, for instance on distance/energy/hybrid metrics
  - In particular: With energy metric there is no competitive geometric routing algorithm



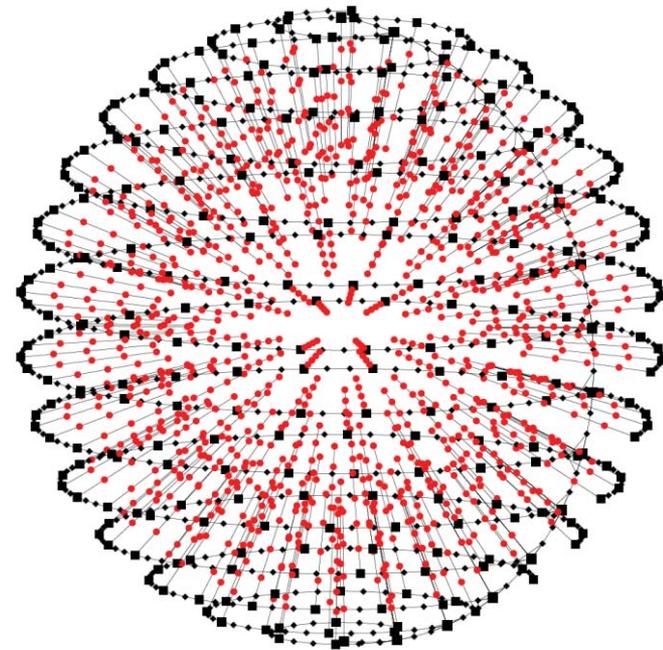
# GOAFR: Summary



# 3D Geo-Routing

---

- The world is not flat. We can certainly envision networks in 3D, e.g. in a large office building. Can we geo-route in three dimensions? Are the same techniques possible?
- Certainly, if the node density is high enough (and the node distribution is kind to us), we can simply use greedy routing. But what about those local minima?!?
- Is there something like a face in 3D?
- The picture on the right is the 3D equivalent of the 2D lower bound, proving that we need at least  $\text{OPT}^3$  steps.



# 3D Geo Routing

---

How would you do 3D routing?



# Routing with and without position information

---

- **Without** position information:
  - Flooding
    - **does not scale**
  - Distance Vector Routing
    - **does not scale**
  - Source Routing
    - **increased per-packet overhead**
    - **no theoretical results, only simulation**
- **With** position information:
  - Greedy Routing
    - **may fail**: message may get stuck in a “dead end”
  - Geometric Routing
    - It is assumed that each node **knows its position**



# Summary of Results

---

- If position information is available geo-routing is a feasible option.
- **Face routing** guarantees to deliver the message.
- By restricting the search area the efficiency is **OPT<sup>2</sup>**.
- Because of a lower bound this is asymptotically optimal.
- Combining greedy and face gives efficient algorithm.
- **3D** geo-routing is **impossible**.
- Even if there is no position information, some ideas might be helpful.
  
- Geo-routing is probably the only class of routing that is well understood.
- There are **many adjacent areas**: topology control, location services, routing in general, etc.



# Open problem

---

- Geo-routing is one of the best understood topics. In that sense it is hard to come up with a decent open problem. Let's try something wishy-washy.
- We have seen that for a 2D UDG the efficiency of geo-routing can be quadratic to an optimal algorithm (with routing tables). However, the worst-case example is quite special.
- Open problem: How much information does one need to store in the network to guarantee only **constant overhead**?
  - Variant: Instead of UDG some more realistic model
  - How can one maintain this information if the network is dynamic?

