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Distributed Systems Part II Solution to Exercise Sheet 3

Authentication 1

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a) The new algorithm looks like this:
if I am P then
  values \leftarrow \{input\}
  broadcast "P has input"
else
  values \leftarrow \{\}
end if
for r = 0 to f + 1 do
  for all received values x do
     if |values| < 2 and accepted r messages "P has x" with x \notin values then
       values \leftarrow values \cup \{x\}
       broadcast "P has x"
     end if
  end for
end for
if |values| = 1 then
  decide item in values
else
  decide "sender faulty"
end if
```

b) If P is correct: there is only one message in the system, which is accepted in the first round. There are no other messages, hence for all processes |values| = 1.

If P is Byzantine:

- Assume that a correct process **p** adds x to its value set in a round r < f + 1: Process \mathbf{p} has accepted r messages including the message from \mathbf{P} . Therefore all other correct processes accept the same r messages plus p's message and add x to their value set as well in round r + 1.
- Assume a correct process p adds x to its value set in round f + 1: In this case, p accepted f + 1 messages. At least one of those is sent by a correct process, which must have added x to its set in an earlier round. We are again in the previous case, i.e., all correct processes added x to its value set.

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2 Randomization

a) The algorithm can handle f < n/8 failures. To find this result we check the proofs for the validity condition, agreement, and termination for numbers that change:

Validity condition Nothing changes

Agreement Nothing changes

Termination If some process does not set its value randomly, all processes must set the same value, i.e. there must not be n - 4f proposals for 0 and n - 4f proposals for 1. This means that 2 * (n - 4f) > n, or f < n/8.

The reason why this property changes is that Byzantine processes can create two different messages, while simple crashing processes cannot.

- b) One solution is to replace "if at least n-4f proposals" by "if at least n-3f proposals". There are other correct solutions which will not be discussed in this master solution.
- c) We modify the proof from the lecture. For the agreement property we replace "Every other correct process must have received x at least n 4f times." by "... at least n 3f" times. Why? Because n 3f correct processes had to send their proposal in order for one process to decide. Meaning n 3f correct processes sent their proposal to any process.

Rewriting the termination property leads to 2 * (n - 3f) > n, or f < n/6.