



## Distributed Systems Part II

### Solution to Exercise Sheet 6

### 1 Paxos Timeline

The timeline consists of two concurrent processes, one on the client  $Q$  and one on the client  $R$ . In Figure 1 you can see how both clients prepare and propose their values at first, but only the value of client  $Q$  gets accepted:

- $T_0 + 0.0$ :  $Q$  sends a prepare(22,1). As  $A$  and  $B$  have never accepted a value they reply with acc( $\emptyset$ ,0).
- $T_0 + 0.5$ :  $R$  sends a prepare(33,2). As  $B$  and  $C$  have never accepted a value they reply with acc( $\emptyset$ ,0).
- $T_0 + 1.0$ :  $Q$  sends a propose(22,1). This is acknowledged by  $A$  with ack(22,1) because its  $n_{max} = 0$ .  $B$  does not reply as its value  $n_{max} = 2$ .
- $T_0 + 2.0$ :  $Q$  sends a prepare(22,3). As  $B$  has never accepted a value it replies with acc( $\emptyset$ ,0).  $A$  returns the latest accepted value: acc(22,1).
- $T_0 + 2.5$ :  $R$  sends a propose(33,2). This is acknowledged by  $C$  with ack(33,2).  $B$  does not reply as its value  $n_{max}$  is 3.
- $T_0 + 3.0$ :  $Q$  sends a propose(22,3). This is acknowledged by  $A$  and  $B$  with ack(22,3).
- $T_0 + 4.5$ :  $R$  sends a prepare(33,4).  $C$  sends back its latest accepted value ack(33,2).  $B$  also sends back its latest accepted value acc(22,3)
- $T_0 + 6.5$ :  $R$  sends a propose(22,4) (It took the newest value from the prepare phase). Both clients  $B$  and  $C$  reply with an ack(22,4). All clients have accepted the same value. This means we have achieved consensus.

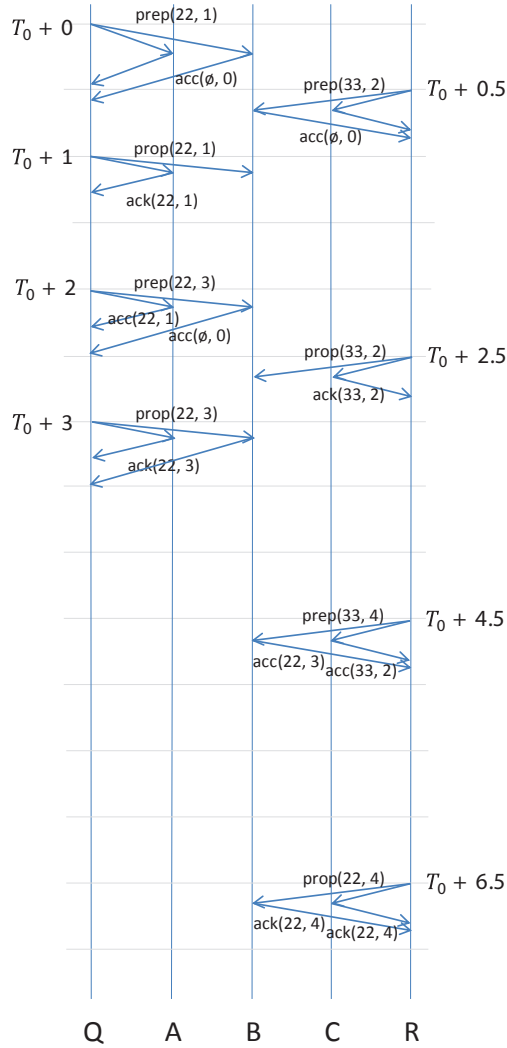


Figure 1: The timeline of the two clients running the given paxos-proposer-program with different timeout values

## 2 Paxos Acceptors

a) Figure 2 shows an example of how a byzantine client can lead to a failure of the Paxos protocol (i.e. why Paxos is not resilient against byzantine failures):

1. The red proposer sends a prepare with value 1.
2. The red acceptors (incl. the byzantine) send an  $ack(\emptyset, 0)$  back.
3. The blue proposer sends a prepare with its value.
4. The blue acceptors (incl. the byzantine) send an  $ack(\emptyset, 0)$  back. We assume that a read on the faulty register of the byzantine node returned  $n_{max} = 0$ .
5. The red proposer sends a propose with value 1.
6. The red acceptors (incl. the byzantine) send an  $ack(1, 3)$  back. We assume that a read on the faulty register of the byzantine node returned  $n_{max} = 3$ .
7. The blue proposer sends a propose with value 1.

8. The blue acceptors (incl. the byzantine) send an  $\text{ack}(2,4)$  back. We assume that a read on the faulty register of the byzantine node returned  $n_{max} = 4$ .

At the end of these 8 steps the red proposer thinks that a majority has accepted the value 1 and the blue proposer thinks that a majority has accepted value 2. Both proposers will start to disseminate their value as each of them thinks that they have achieved consensus.

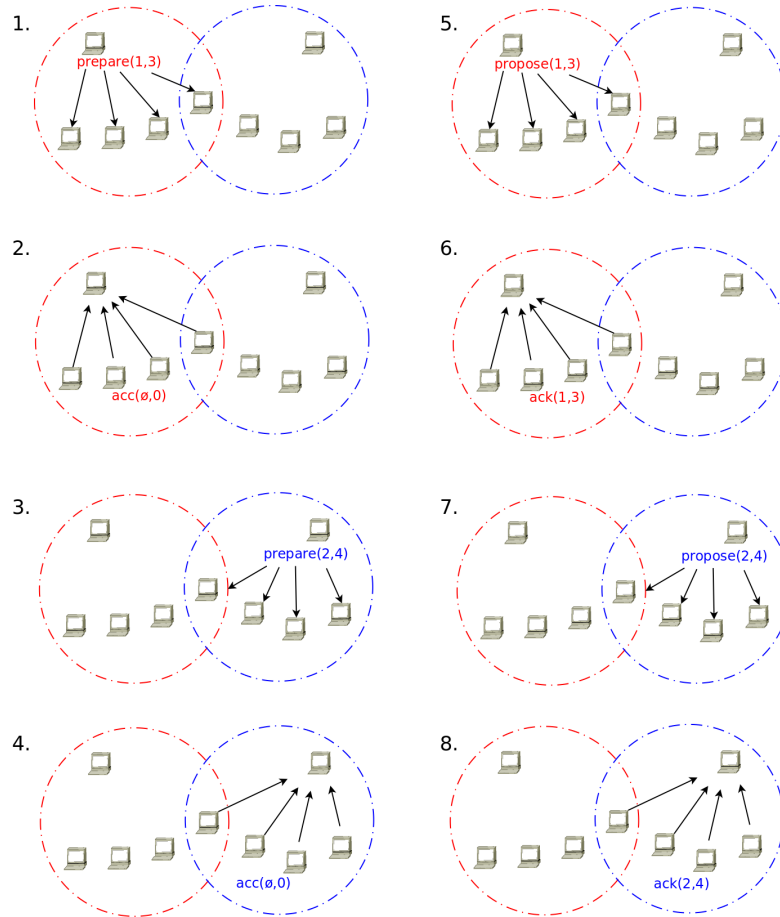


Figure 2: How a byzantine client can lead to different values that are accepted by a majority.

- b) The prepare step allows the proposer and the acceptor to agree on a lower bound of the proposal number that will be accepted. By sending an  $\text{ack}(x,y)$  message, the acceptor guarantees the proposer that it will never accept a proposed value that has a smaller timestamp than the one in the prepare message of the proposer.