1 Paxos Timeline

The timeline consists of two concurrent processes, one on the client $Q$ and one on the client $R$. In Figure 1 you can see how both clients prepare and propose their values at first, but only the value of client $Q$ gets accepted:

- $T_0 + 0.0$: $Q$ sends a prepare(22,1). As $A$ and $B$ have never accepted a value they reply with $\text{acc}(\emptyset,0)$.

- $T_0 + 0.5$: $R$ sends a prepare(33,2). As $B$ and $C$ have never accepted a value they reply with $\text{acc}(\emptyset,0)$.

- $T_0 + 1.0$: $Q$ sends a propose(22,1). This is acknowledged by $A$ with $\text{ack}(22,1)$ because its $n_{\text{max}} = 0$. $B$ does not reply as its value $n_{\text{max}} = 2$.

- $T_0 + 2.0$: $Q$ sends a prepare(22,3). As $B$ has never accepted a value it replies with $\text{acc}(\emptyset,0)$. $A$ returns the latest accepted value: $\text{acc}(22,1)$.

- $T_0 + 2.5$: $R$ sends a propose(33,2). This is acknowledged by $C$ with $\text{ack}(33,2)$. $B$ does not reply as its value $n_{\text{max}}$ is 3.

- $T_0 + 3.0$: $Q$ sends a propose(22,3). This is acknowledged by $A$ and $B$ with $\text{ack}(22,3)$.

- $T_0 + 4.5$: $R$ sends a prepare(33,4). $C$ sends back its latest accepted value $\text{ack}(33,2)$. $B$ also sends back its latest accepted value $\text{acc}(22,3)$.

- $T_0 + 6.5$: $R$ sends a propose(22,4) (It took the newest value from the prepare phase). Both clients $B$ and $C$ reply with an $\text{ack}(22,4)$. All clients have accepted the same value. This means we have achieved consensus.
Figure 1: The timeline of the two clients running the given paxos-proposer-program with different timeout values

2 Paxos Acceptors

a) Figure 2 shows an example of how a byzantine client can lead to a failure of the Paxos protocol (i.e. why Paxos is not resilient against byzantine failures):

1. The red proposer sends a prepare with value 1.
2. The red acceptors (incl. the byzantine) send an ack(ø,0) back.
3. The blue proposer sends a prepare with its value.
4. The blue acceptors (incl. the byzantine) send an ack(ø,0) back. We assume that a read on the faulty register of the byzantine node returned $n_{max} = 0$.
5. The red proposer sends a propose with value 1.
6. The red acceptors (incl. the byzantine) send an ack(1,3) back. We assume that a read on the faulty register of the byzantine node returned $n_{max} = 3$.
7. The blue proposer sends a propose with value 1.
8. The blue acceptors (incl. the byzantine) send an ack(2,4) back. We assume that a read on the faulty register of the byzantine node returned $n_{max} = 4$.

At the end of these 8 steps the red proposer thinks that a majority has accepted the value 1 and the blue proposer thinks that a majority has accepted value 2. Both proposers will start to disseminate their value as each of them thinks that they have achieved consensus.

Figure 2: How a byzantine client can lead to different values that are accepted by a majority.

b) The prepare step allows the proposer and the acceptor to agree on a lower bound of the proposal number that will be accepted. By sending an ack(x,y) message, the acceptor guarantees the proposer that it will never accept a proposed value that has a smaller timestamp than the one in the prepare message of the proposer.