

# Parallel Computing

## Part 2, Chapter 8

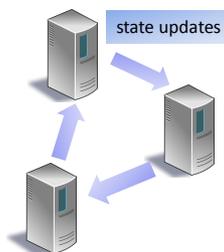
Roger Wattenhofer

### Overview

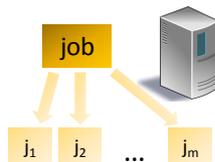
- Structure of a parallel computer
- Parallel Software for 16 cores (CPU)
- Parallel Software for 1,600 cores (GPU)

### Programming Parallel Systems

- So far, we talked (mainly) about storage systems
  - Main question: How can we guarantee a consistent system state

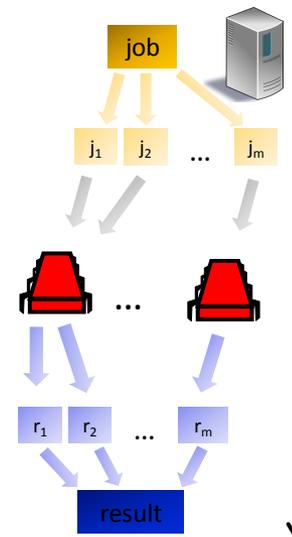


- Already desktop systems can be used for parallel computation
  - Distribute work load in the system!
  - How can we do this?
  - What's underneath the hood?

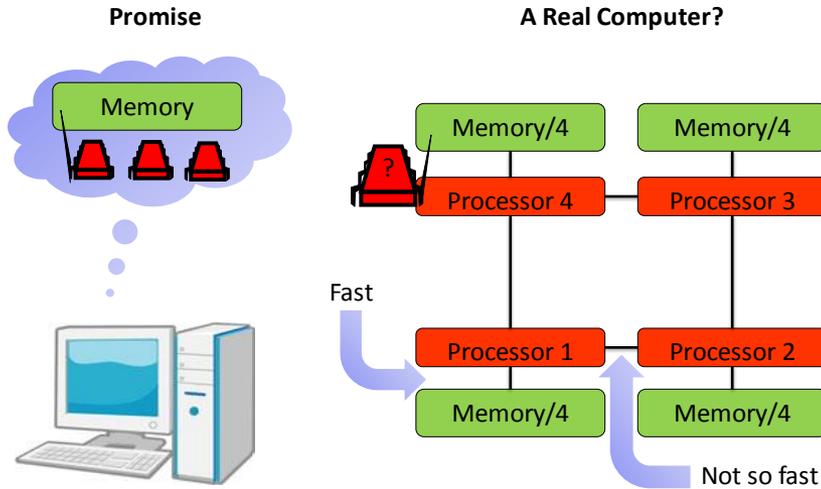


### Programming Parallel Systems: Basic Idea

- Our model for parallel programming:
  - A job is split into many small tasks
    - These tasks can be executed in parallel
  - The tasks can be distributed
    - Each „worker thread“ may get many tasks
  - The partial results may be merged
    - This is just another kind of “task”

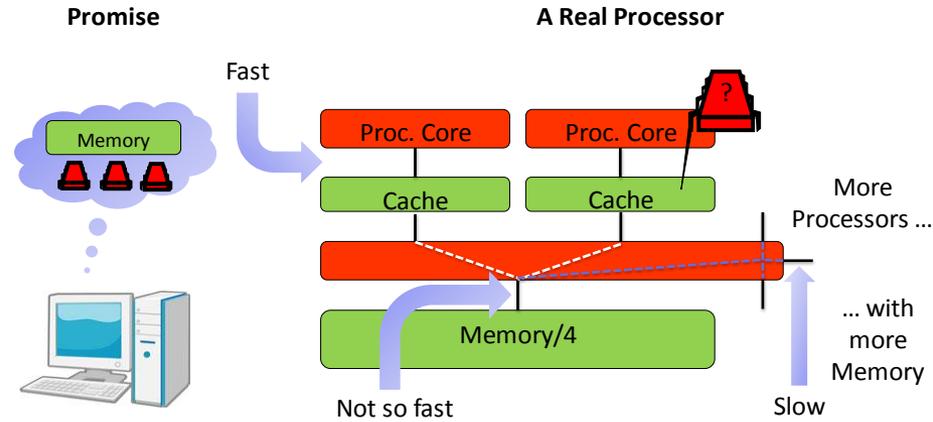


# Programming Parallel Systems: Promise and Reality



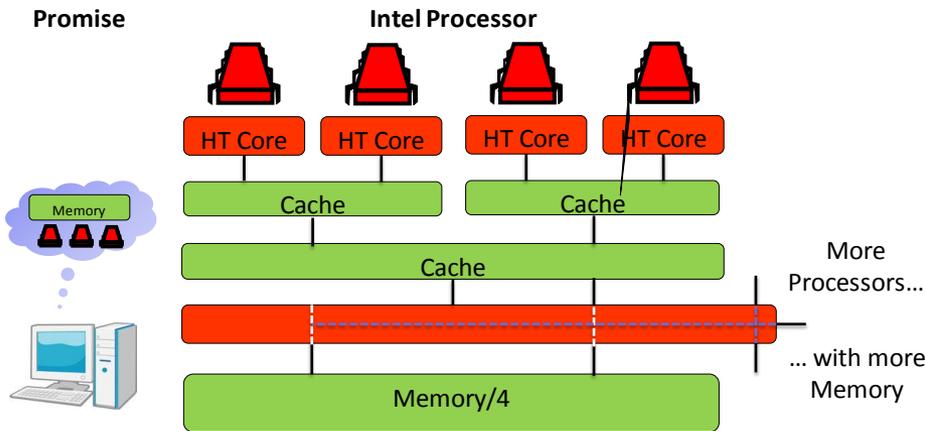
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# Programming Parallel Systems: Promise and Reality



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# Programming Parallel Systems: Promise and Reality



- Need to know your hardware for maximum efficiency
  - Cache Sizes, Topology & Bandwidth of Buses
  - Think: Data locality, (hidden!) communication cost

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# Programming Parallel Systems: A To-Do List

- We need to
  - **write code** for worker threads
  - **distribute** the threads to the cores
  - **split** the job into smaller tasks (how small?)
  - **assign** tasks to threads
  - **balance** the load on all threads
  - **collect** the (partial) results from the machines
  - **assembly** the results
- Should be fast as well, i.e., make use of **locality**
  - cache locality *and* prefer local memory over remote memory!
- The **complexity** of the program increases significantly!!!
- Solution?



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## OpenMP

- OpenMP is a specification developed by AMD, Cray, IBM, Intel, NVIDIA, ...
  - Parallelization
  - Load balancing
  - Implicit use of locality
    - If you know what you are doing
  - All in one library!
- Not really a library, but a language-extension
  - C, C++, Fortran (still used in scientific computing)
- Supports Basic Parallel Constructs
  - Loops, basic reductions, tasks, ...
  - Synchronization



## OpenMP: An Example

```
std::vector<int> a(N);  
std::vector<int> b(N);
```

a[i]\*b[i]?

```
void sequential()  
{  
    for (int i = 0; i < N; i++)  
        a[i] *= b[i];  
}
```

- Split loop into tasks
- Distribute tasks to workers

```
void parallel()  
{  
    #pragma omp parallel for  
    for (int i = 0; i < N; i++)  
        a[i] *= b[i];  
}
```

4 Procs x 4 Cores = 16 Threads  
Speedup: 3.1x

Only 3.1x?

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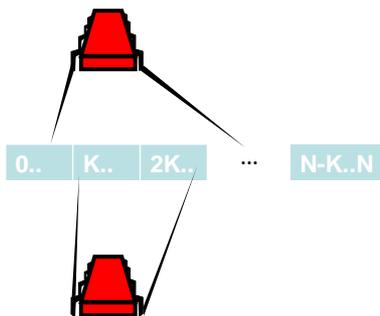
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## OpenMP: Under the Hood

```
void parallel()  
{  
    #pragma omp parallel for  
    for (int i = 0; i < N; i++)  
        a[i] *= b[i];  
}
```

When a worker is free:  
grab the next available task  
(block of iterations)

Iteration of for-loop:



Where are the memory cells accessed in iteration i?

## OpenMP: Digging Deeper

- Physical memory location depends on **Operating System**

```
std::vector<int> a(N);  
std::vector<int> b(N);
```

- **Virtual** Memory presented as continuous block
  - **Physical** Memory may be scattered
  - A single **page** of virtual/physical memory cannot be scattered
  - Typical page sizes: 4KB, SuperPage: 4MB
- Many OSes
  - Explicitly: Offer system call to pin a page to a physical processor by hand
  - Implicitly: Pin virtual pages to processor that first accesses it
  - How is this done?

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## OpenMP: Static Scheduling

```
int *a, *b;
```

```
a = (int*)malloc(N*sizeof(int));  
b = (int*)malloc(N*sizeof(int));
```

```
void fill()
```

```
{  
#pragma omp parallel for schedule(static)  
for (int i = 0; i < N; ++i) {  
a[i] = a_value(i);  
b[i] = b_value(i);  
}  
}
```

Chunk x is assigned to thread x mod num\_threads

```
void parallel()
```

```
{  
#pragma omp parallel for schedule(static)  
for (int i = 0; i < N; ++i)  
a[i] *= b[i];  
}
```

4 Procs x 4 Cores = 16 Threads  
Speedup: 6.7x

Only 6.7x?

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## Not Every Parallel Program is a for-loop

- Barely scratched the surface of OpenMP
  - Reductions

```
int sum = 0;  
#pragma omp parallel for reduction(+:sum)  
for (int i = 0; i < N; i++) {  
sum += a[i] + b[i];  
}
```

## Not Every Parallel Program is a for-loop

- Barely scratched the surface of OpenMP

- Reductions
- Arbitrary task types

```
cout<<"A ";  
#pragma omp parallel  
{  
#pragma omp single  
{  
#pragma omp task  
{ cout<<"car "; }  
#pragma omp task  
{ cout<<"race "; }  
}  
} cout<<endl;
```

A race car car race  
(or)  
A car car race race  
(or...)

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## Not Every Parallel Program is a for-loop

- Barely scratched the surface of OpenMP

- Reductions
- Arbitrary task types
- Synchronization primitives

```
cout<<"A ";  
#pragma omp parallel  
{  
#pragma omp single  
{  
#pragma omp task  
{ cout<<"car "; }  
#pragma omp task  
{ cout<<"race "; }  
#pragma omp taskwait  
cout<<"is fun to watch";  
}  
} cout<<endl;
```

A car race is fun to watch  
(or)  
A race car is fun to watch

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## Not Every Parallel Program is a for-loop

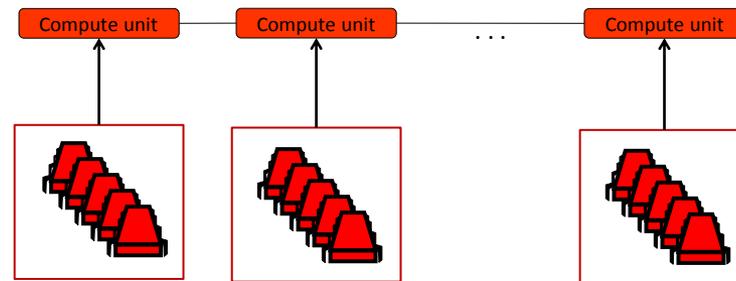
- Barely scratched the surface of OpenMP
  - Reductions
  - Arbitrary task types
  - Synchronization primitives
  - ...
- Already a simple loop can be tricky
- Simple loops are everywhere!
  - Think: Vectors, Matrix Multiplication
  - Simple loops deserve their own hardware



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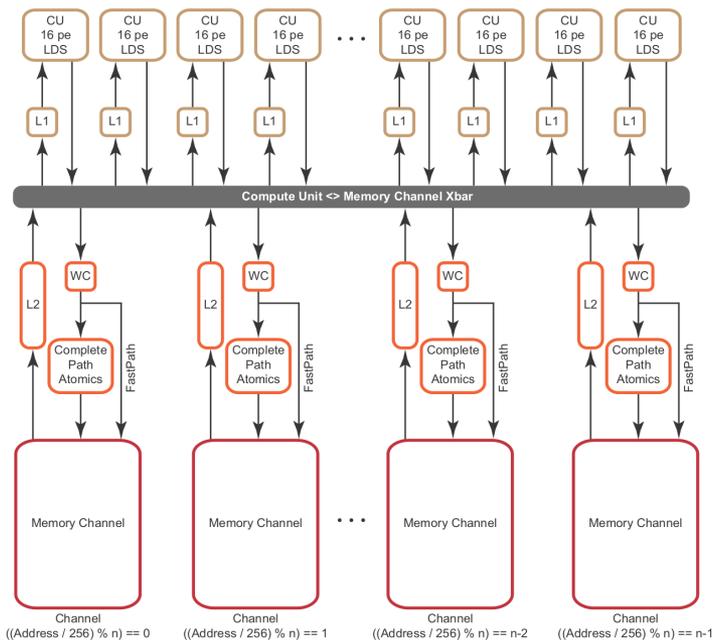
## Graphic Processing Unit (GPU)

- The complexity of the architecture increases further
- The GPU consists of compute units, each with multiple stream cores
  - As an example, AMD Radeon R9 290X has 2816 stream cores



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## The Real Deal

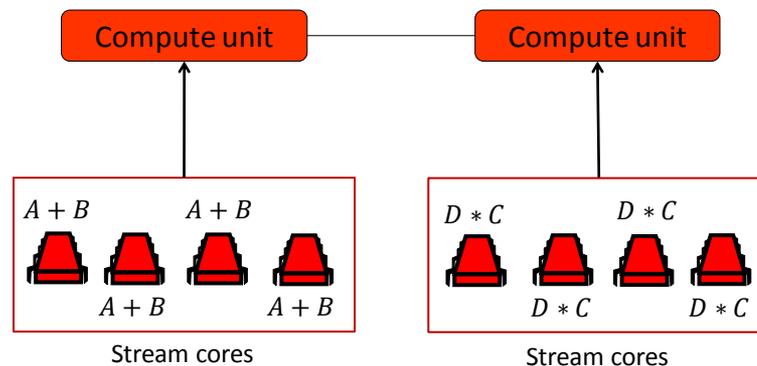


Programming Guide  
AMD Accelerated Parallel Processing  
OpenCL™

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## Graphic Processing Unit (GPU)

- Different compute units can do different things
- All stream cores execute the same instruction sequence
  - With separate local memories

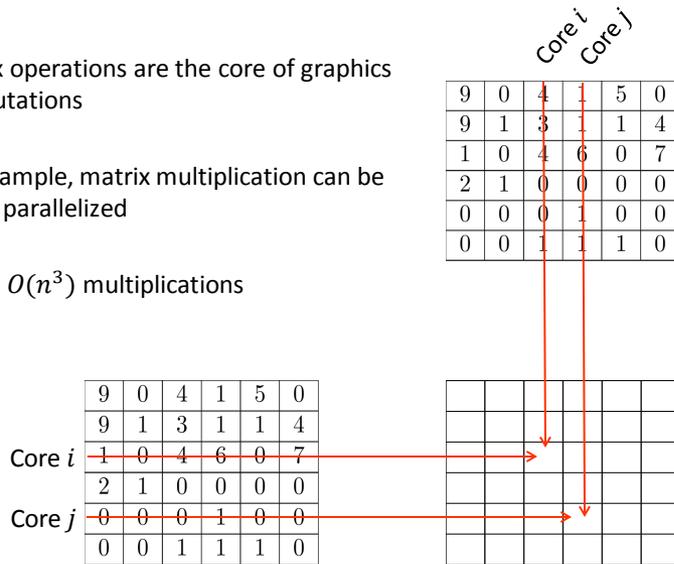


- What is this good for?

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## Matrix Operations

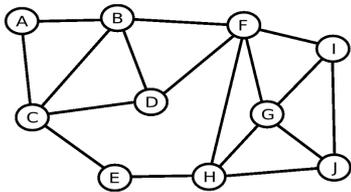
- Matrix operations are the core of graphics computations
- For example, matrix multiplication can be highly parallelized
- Naive:  $O(n^3)$  multiplications



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## All-Pairs Shortest Path

- Some problems can be represented nicely by matrices
- Let  $G = (V, E)$  be a connected graph. The adjacency matrix  $M$  of  $G$  has a 1-entry on  $M(u, v)$  if there is an edge between nodes  $u$  and  $v$



	A	B	C	D	E	F	G	H	I	J
A	0	1	1	0	0	0	0	0	0	0
B	1	0	1	1	0	1	0	0	0	0
C	1	1	0	1	1	0	0	0	0	0
D	0	1	1	0	0	1	0	0	0	0
E	0	0	1	0	0	0	0	1	0	0
F	0	1	0	1	0	0	1	1	1	0
G	0	0	0	0	0	1	0	1	1	1
H	0	0	0	0	1	1	1	0	0	1
I	0	0	0	0	0	1	1	0	0	1
J	0	0	0	0	0	0	1	1	1	0

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## Matrix Multiplication

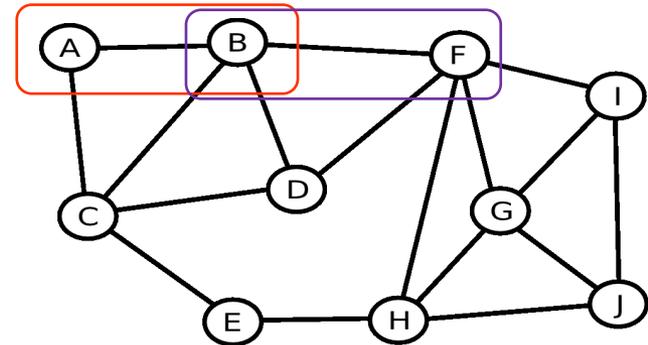
- Naive:  $O(n^3)$  multiplications
  - Small rounding errors
- Better: Strassen  $O(n^{2.807})$  multiplications
  - Re-use partial results
  - Can also be done in parallel
- Even better? Coppersmith-Winograd  $O(n^{2.375477})$  multiplications
  - Asymptotically better
  - But not for practical matrix sizes



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## All-Pairs Shortest Path

- The adjacency matrix gives us all nodes at distance 1
- To get nodes at distance 2, multiply the adjacency matrix by itself
- $M^2(A, F) = M(A, A)M(A, F) + M(A, B)M(B, F) + \dots + M(A, F)M(F, F) \geq 1$

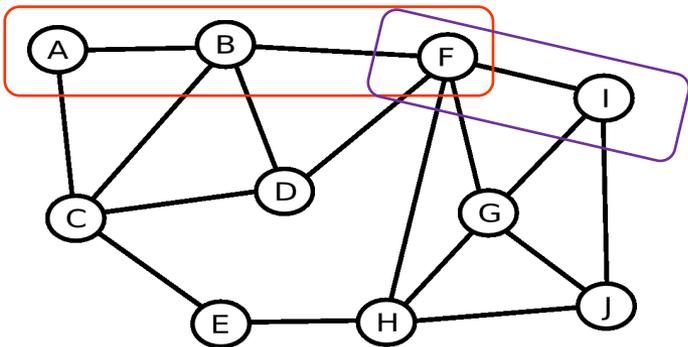


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## Solving the All-Pairs Shortest Path Problem

- Similarly, get nodes at distance 3 by multiplying  $M^2$  by  $M$ :

$$M^3(A, I) = M^2(A, A)M(A, I) + M^2(A, F)M(F, I) + \dots \geq 1$$



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## Conclusion

- OpenMP
  - Widely used in scientific computing
  - CPUs execute 'real' threads
    - Don't have to execute the same line of code everywhere
- GPUs have way more cores than CPUs
  - Enables more parallelism
  - Cores execute the **same** instruction per clock cycle
  - Efficient for matrix operations
  - Can be programmed using
    - OpenCL
    - CUDA
    - possibly OpenMP in the future

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## All-Pairs Shortest Path

- After  $i$  multiplications,  $M(u, v) \neq 0$  if there is a path of length at most  $i + 1$  from  $u$  to  $v$
- After  $\text{diameter}(G) - 1$  multiplications, we have found all nodes
- The length of the shortest path between any two nodes  $u$  and  $v$  is the index of the step  $i$  for which,  $M^{(i-1)}(u, v) = 0$  and  $M^i(u, v) \geq 1$ 
  - Write distances to output matrix  $Q$
- We can store the partial paths found in the intermediate steps
  - get the actual shortest paths in the end

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## Outlook

- Faults
  - OpenMP, OpenCL, CUDA don't care about faults
  - Hadoop/MapReduce: Store all intermediate steps, for fault-tolerance
  - Apache Spark: Recompute intermediate steps in case of (rare) faults
- Bottlenecks
  - Solution to problem designed around the shortcomings of the hardware
  - Why don't we design the hardware around our problem?  
Remove bottlenecks, fine-tune relative speed of system components
  - «MinuteSort with Flat Datacenter Storage», MSR  
Disk reads can be a bottleneck as well → Design whole datacenter around it  
Overlap disk reads with asynchronous sorting-passes of already available data  
Unbeaten entry from 2012 for 'Number of elements sorted in 60 seconds'  
[www.sortbenchmark.org](http://www.sortbenchmark.org)

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# *That's all, folks!*

*Questions & Comments?*



*Roger Wattenhofer*