

Eidgenössische Technische Hochschule Zürich Swiss Federal Institute of Technology Zurich

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Discrete Event Systems

Exercise Sheet 3

1 Pumping Lemma [Exam]

Is the following language regular? Prove your claims!

$$L = \{0^a 1^b 0^c 1^d \mid a, b, c, d \ge 0 \text{ and } a = 1, b = 2 \text{ and } c = d\}$$

2 Deterministic Finite Automata [Exam]

Transform the NFA A in Figure 1 into an equivalent DFA using the powerset construction presented in the lecture, while assuming $\Sigma = \{0,1\}$. (*Hint:* Only construct states which are necessary!)

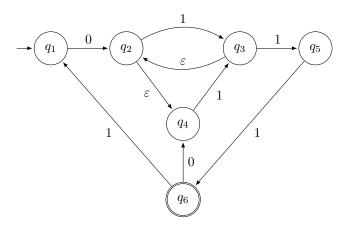


Figure 1: NFA A.

3 Transforming Automata [Exam]

Consider the DFA B in Figure 2 over the alphabet $\Sigma = \{0, 1\}$. Give a regular expression for the language L accepted by the automaton B. If you like, you can do this by ripping out states as presented in the lecture.

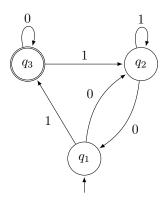


Figure 2: DFA B.

4 Regular and Context-Free Languages

- a) Consider the context-free grammar G with the production $S \to SS \mid 1S2 \mid 0$. Describe the language L(G) in words, and prove that L(G) is not regular.
- b) The regular languages are a subset of the context-free languages. Give the context-free grammar for an arbitrary language L that is regular.

5 Context-Free Grammars

Give context-free grammars for the following languages over the alphabet $\Sigma = \{0, 1\}$:

- a) $L_1 = \{w \mid \text{the length of } w \text{ is odd}\}$
- **b)** $L_2 = \{ w \mid \text{contains more 1s than 0s} \}$

6 Ambiguity

Consider the following context-free grammar G with non-terminals S and A, start symbol S, and terminals "(", ")", and "0":

$$S \rightarrow SA \mid \varepsilon$$

$$A \rightarrow AA \mid (S) \mid 0$$

- a) What are the eight shortest words produced by G?
- b) Context-free grammars can be ambiguous. Prove or disprove that G is unambiguous.
- c) Design a push-down automaton M that accepts the language L(G). If possible, make M deterministic.